DIURNAL ENERGETICS OF A RESERVOIR SURFACE LAYER

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DIURNAL ENERGETICS OF A RESERVOIR SURFACE LAYER

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SYNOPSIS

Mixing of the surface waters of a reservoir, induced by meteorological forces, is a major factor determining the quality of the water throughout the full depth. The aim of the project described herein was to study the air-water interaction over the Wellington Reservoir and develop a theoretical description of the important observed features.

The epilimnion, or seasonal well mixed layer, was observed to undergo a diurnal cycle of heating and mixing, which in turn governed the seasonal cycle, including the formation and subsequent erosion of a seasonal thermocline. The diurnal cycle has been successfully simulated by a numerical model of integral well mixed layer energetics. The model has direct application in the study of biological production in reservoir surface waters. In addition, it is shown that the theory of well mixed layer energetics may be applied to a study of the seasonal cycle in reservoirs, and also to oceanic and atmospheric problems.

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CHAPTER 1

INTRODUCTION

In July 1974, a Study funded by the Australian Water Resources Council and entitled "Management of Water Quality in Reservoirs" was commenced within the Engineering School at the University of Western Australia. The Study concentrated on the Wellington Reservoir, situated some 160 km south of Perth, where increased salinity levels had resulted from clearing of the reservoir catchment's native forest for agricultural purposes. In addition to alleviating this specific problem, the objective of the Study was to develop management procedures applicable to a variety of water quality problems occurring in medium sized reservoirs. The Study was completed in 1980 with the publication of the final report by Imberger and Hebbert (1980).

The Project described in the present report was initiated, as part of the above Study, to investigate the interaction between meteorological processes and the reservoir surface layer. In particular, it was considered necessary to understand the heating and mixing cycles which lead to the formation of the seasonal thermocline, which itself has a profound effect on internal water movements and on the vertical transport of water constituents. The aims of the Project were:

(a) to experimentally observe and measure meteorological
 and water properties which modify the reservoir
 surface density structure,

(b) to develop theoretical and numerical descriptions of those observed processes considered to be important, and so attempt to simulate the observed surface density structure,

(c) to recommend procedures applicable to simulation o the seasonal reservoir surface density structure.

Over the summer months of 1975-76, a series of

intensive field investigations were conducted aboard a raft anchored near the centre of the main water body. The raft provided a platform for a permanent, continuously recording weather station and was also used during the field work to mount sensitive meteorological sensors. Profiles of temperature and salinity, measured hourly over four separate days, revealed a striking diurnal cycle of morning heating followed by afternoon and evening mixing, occurring within the epilimni which is normally considered to be well mixed. Integral descriptions of turbulent kinetic energy, heat, mass, momentum and salinity were developed and incorporated into a numerical model of the diurnal cycle. The model's description of turbulent transfers at the surface includes the effect of atmospheric stability, which is very important over a medium sized reservoir. The model has successfully simulated the diurnal cycle for the four field days, so meeting the above aims.

A brief guide to the contents of this report is as follows. Chapters 2 and 3 provide the methods for computing turbulent and radiative transfers at the reservoir surface; these are boundary conditions for the model. Chapter 4 detail

the measurement of temperature and salinity profiles which revealed the diurnal cycle. The integral formulation of well mixed layer energetics is presented in Chapter 5 and is incorporated into the framework of a numerical model in Chapter 6. Chapter 7 contains an analysis of the model results, with conclusions and recommendations for future work appearing in Chapter 8.

CHAPTER 2

THEORY OF ATMOSPHERIC SURFACE TRANSFERS

Over recent years, considerable research has focused on the physics of turbulent and radiative transfers in the atmospheric surface layer. In this chapter, a few established relatiships are presented, providing a basis for experimental methods and computations described in Chapter 3.

2.	1	TURBULENT	TRANSFERS	IN	THE	SURFACE	LAYER
	-						

2.1.1 Surface Layer Scaling and Parameterization

The Navier-Stokes equation for meteorological considerations is conventionally written in the form

$$\frac{d\underline{U}}{dt} + f \hat{\underline{k}} \times \overline{\underline{U}} = -\frac{1}{\rho} \nabla p + \frac{1}{\rho} \frac{\partial \underline{\tau}}{\partial z} , \qquad (2.1)$$

with \overline{U} horizontal mean velocity, with x and y components,

- k unit vertical vector,
- f Coriolis parameter,
- ρ density of air,
- ∇p horizontal pressure gradient $\frac{\partial p}{\partial x} + \frac{\partial p}{\partial y}$,

T Reynolds stress vector.

In deriving eq. 2.1 and other relations, properties of the flow are split into mean and fluctuating components, as follows:

horizontal velocity	$\underline{u} = \overline{\underline{v}} + \underline{u}',$	$\overline{u}^{\dagger} = 0$
vertical velocity	$w = \overline{W} + w'$,	$\overline{w}' = 0$
temperature	$T = \overline{T} + \theta',$	$\overline{\Theta}$ ' = 0
specific humidity	$q = \overline{q} + q',$	$\overline{q}' = 0$

The overbar denotes a time average (assuming stationarity of the turbulence). It will be retained in the following equations only for products of fluctuating quantities, e.g. the Reynolds stress is defined as

$$\frac{\tau}{\rho} = -u'w' =$$
friction velocity.
(2.2)

Kraus (1972) shows, by a scaling argument applied to eq. 2.1, that the Reynolds stress is effectively constant in the atmospheric surface layer up to a height of several tens of metres. In this layer, rotational effects are negligible and so the mean flow is considered in two dimensions only.

The heat equation may be written as

$$\begin{array}{ccc} dT & 1 \\ dt & \rho C_{p} \left(\frac{\partial H}{\partial z} + \frac{\partial Q}{\partial z} \right), \end{array}$$
(2.3)

 $C_{\rm p}$ specific heat of air,

H turbulent heat flux = $\rho C_p \overline{\theta' w'}$.

Finally, the equation for vertical momentum, neglecting frictional and Coriolis effects, is

$$\frac{dW}{dt} - \frac{1}{\rho} \frac{\partial p'}{\partial z} + \frac{g}{T} \Delta T , \qquad (2.4)$$

with p' dynamic pressure

 ΔT temperature difference between the parcel of air and its surroundings.

Monin-Obukhov Length

Monin and Obukhov (1954) examined the physical

quantities

from the above equations and by dimensional analysis defined a

length scale

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$$L = -\frac{u_{\star}^{3}}{k \frac{g}{T} \frac{H}{\rho C_{p}}}, \qquad (2.5)$$

with k von Kármán constant (defined later).

On the basis of dynamic similarity they proposed that any mean property of the turbulent flow may be described in terms of the dimensionless variable z/L. The Monin-Obukhov length, L, may be evaluated for a given set of meteorological conditions and is a measure of the height of the dynamic sublayer within which thermally induced effects are unimportant.

Moisture Correction

Air containing water vapour has a lower molecular wei than dry air and hence a higher gas contant R as it appears in the Ideal Gas Law

$$p = \rho R T.$$
 (2.6)

It is common meteorological practice, when dealing with mixtures of air and water vapour, to retain a constant value of R and include moisture correction in the temperature, giving virtual temperature

 $T_v = T(1 + 0.61q)$ in degrees Kelvin. (2.7) Eq. 2.7 is derived simply from Dalton's Law.

When investigating turbulent flow over water bodies, the buoyancy induced by water vapour excess close to the surface should be considered. Busch (1973) incorporates this effect into the Monin-Obukhov length

$$L = -\frac{u_*^{3}T_v}{kg\theta_v'w'}, \qquad (2.8)$$

where θ_v ' is the fluctuating component of virtual potential temper ature. The buoyancy flux term $\overline{\theta_v}'w'$ may be expanded using eq. 2.7

$$\overline{\theta_{\mathbf{v}}'\mathbf{w}'} = \overline{\theta'\mathbf{w}'}(1+0.61q) + 0.61T \overline{q'\mathbf{w}'} + 0.61 \overline{\theta'q'\mathbf{w}'},$$

$$\simeq \overline{\theta'\mathbf{w}'} + 0.61T \overline{q'\mathbf{w}'}, \text{ (neglecting minor terms)}$$

$$= \frac{1}{\rho C_p} H + 0.61 \frac{T}{\rho} E,$$

where E is the turbulent mass flux of water vapour.

So,
$$L = \frac{-\rho u_*^3 T_v}{kg[\frac{H}{C_p} + 0.61TE]}$$
 (2.9)

2.1.2 Flux - Profile Relationships

The theory of flux - profile relationships in the surface layer has been well documented by Dyer (1974), Businger (1973) and others. Although no profile measurements were conducted during this project, the theory covering such work will be utilized and is therefore summarised below.

Similarity Hypothesis

Monin and Obukhov (1954) parameterised the non-dimensional gradients of wind, potential temperature and specific humidity in terms of the stability parameter z/L:

 $\frac{kz}{u_{\star}} \frac{dU}{dz} = \phi_{M} \left(\frac{z}{L} \right), \qquad (2.10)$

$$\frac{kz}{\theta_{\star}} \frac{d\theta}{dz} = \phi_{\rm H} \left(\frac{z}{L} \right), \qquad (2.11)$$

$$\frac{\mathbf{k}\mathbf{z} \, \mathrm{d}\mathbf{q}}{\mathbf{q}_{\star} \, \mathrm{d}\mathbf{z}} = \phi_{W}\left(\frac{\mathbf{z}}{\mathbf{L}}\right), \qquad (2.12)$$

where $u_{\star} = \left(\frac{\tau}{\rho}\right)^{\frac{1}{2}}$, (2.13)

$$\theta_{\star} u_{\star} = -\frac{H}{\rho C_{p}} , \qquad (2.14)$$

$$q_* u_* = -\frac{E}{\rho}$$
 (2.15)

k is the von Kármán constant defined such that $\phi_{M,H,W} = 1$ for z/L = 0.

Over the last decade, the development of instrumentatic to directly measure turbulent fluxes of momentum, heat and moisture has permitted precise evaluation of the ϕ functions. Dyer (1974) summarises the various proposed forms and concludes that the following are most acceptable.

Unstable:

$$\phi_{\rm M} = (1 - \gamma \left(\frac{z}{L}\right))^{-\frac{1}{2}},$$
 (2.16)

$$\phi_{\rm H} = \phi_{\rm W} = (1 - \gamma \left(\frac{z}{L}\right))^{-\frac{1}{2}},$$
 (2.17)

where $\gamma \simeq 16$.

Stable:

$$\phi_{\rm M} = \phi_{\rm H} = \phi_{\rm W} = 1 + \alpha \left(\frac{z}{\rm L}\right), \qquad (2.18)$$

where $\alpha \approx 5$.

Hicks (1976), in a re-analysis of the Wangara data (Clarke *et al.*(1971)), found that eq. 2.18 holds only for slightly stable conditions (0 < z/L < 0.5). For higher stabilities he found that velocity profiles depart from the log-linear form of eq. 2.18 toward a purely logarithmic form ($\phi_{\rm M}$ constant), but that this state is never reached. He further observed that in very stable conditio the profile above a few metres becomes linear with height, indicating a decoupling of this air from that near the surface, i.e.:

$$\frac{\mathrm{d}U}{\mathrm{d}z} = \frac{\mathrm{cu}_*}{\mathrm{kL}}, \quad \frac{z}{\mathrm{L}} > 10 , \qquad (2.19)$$

so
$$\phi_{\underline{M}} = c(z/L)$$
 (2.20)

where c is a constant (c $\simeq 0.8$).

Carsons and Richards (1978) lend their support to Hicks' (1976) findings and provide an empirical formula for the transition between eq. 2.18 and eq. 2.20:

$$\phi_{\rm M} = \left(8 - 4.25(z/L)^{-1} + (z/L)^{-2}\right), \quad \left(0.5 < (z/L) < 10\right) \quad (2.21)$$

While it is well established that $\phi_{M} = \phi_{H} = \phi_{W}$ for (0<(z/L)<0.5) there is currently no information on the relationship between the ϕ 's at higher stabilities. It is assumed here that they are equal.

Profile Descriptions

Following Paulson (1970) eqs. 2.10 to 2.12 may be integrated to the form:

$$U = \frac{u_{\star}}{k} \left[\ln \left(\frac{z}{z_0} \right) - \psi_{M} \right] , \qquad (2.22)$$

$$\theta - \theta_{0} = \frac{\theta_{\star}}{k} \left[ln \left(\frac{z}{z_{H}} \right) - \psi_{H} \right], \qquad (2.23)$$

$$q-q_{o} = \frac{q_{\star}}{k} \left[\ln \left(\frac{z}{z_{W}} \right) - \psi_{W} \right], \qquad (2.24)$$

where z_0 , z_H and z_W are roughness lengths. The ψ functions have the form

$$\psi = \int_{\zeta_0}^{\zeta} \frac{1 - \phi(\zeta)}{\zeta} d\zeta, \qquad (2.25)$$

where $\zeta = z/L$.

In neutral conditions ($\phi = 1$), $\psi = 0$ and the eqs. 2.22 to 2.24 reduce to the familiar logarithmic profile.

Paulson (1970) gives analytical solutions to eq. 2.25. For the ϕ function of eq. 2.16 and eq. 2.17 integration yields

$$\psi_{\rm M} = 2 \ln \left[(1+x)/2 \right] + \ln \left[(1+x^2)/2 \right] - 2 \tan^{-1} x + \frac{\pi}{2} , \qquad (2.26)$$

$$\psi_{\rm H} = \psi_{\rm W} = 2\ln[(1+{\rm x}^2)/2],$$
(2.27)

where $x = (1 - \gamma \left(\frac{z}{L}\right))^{\frac{1}{4}}$. For ϕ given by eq. 2.18,

$$\psi_{\rm M} = \psi_{\rm H} = \psi_{\rm W} = -\alpha \left(\frac{z}{\rm L}\right) . \qquad (2.28)$$

Carson and Richards (1978) evaluated ψ numerically for the two regimes where (z/L) > 0.5, given by eq. 2.20 and eq. 2.21. Alternatively, to obtain an analytical solution, ψ may be evaluated separately for each regime.

For $(0.5 < \zeta \leq 10)$

$$\psi = \int_{\zeta_0}^{0.5} \frac{1-\phi(\zeta)}{\zeta} d\zeta + \int_{0.5}^{\zeta} \frac{1-\phi(\zeta)}{\zeta} d\zeta$$
$$= 0.5\zeta^{-2} - 4.25\zeta^{-1} - 7\ln(\zeta) - 0.852. \qquad (2.29)$$

For ζ > 10

$$\psi = \int_{\zeta_0}^{0.5} \frac{1-\phi(\zeta)}{\zeta} d\zeta + \int_{0.5}^{10} \frac{1-\phi(\zeta)}{\zeta} d\zeta + \int_{10}^{\zeta} \frac{1-\phi(\zeta)}{\zeta} d\zeta$$
$$= \ln \zeta - 0.76\zeta - 12.093. \tag{2.30}$$

In obtaining the above results the lower limit of integration, ζ_0 , has been taken as equal to zero. This approximation holds only for very small values of the roughness lengths z_0 , z_H and z_W such as those found over water.

2.1.3 Bulk Aerodynamic Formulae

Utilising the theory presented in the previous section it is feasible to make precise estimates of turbulent fluxes from measurements of the vertical profiles of wind, temperature and humidity over water. However, conducting such a measurement programme is a major undertaking and was considered beyond the scope of this project. For this and similar projects, where surface turbulent fluxes represent only part of the dynamics of the system under investigation, it is desirable to have a method of calculating these fluxes using only routinely available single height observations. The bulk aerodynamic formulae provide such a method.

Bulk aerodynamic formulae for stress, heat and moisture fluxes are written as follows:

$$-\frac{\tau}{\rho} = \overline{u'w'} = -u_{*}u_{*} = -C_{D}U^{2}.$$
(2.31)

$$\frac{\mathrm{H}}{\mathrm{\rho}\mathrm{C}_{\mathrm{p}}} = \overline{\theta' w'} = -\mathrm{u}_{\star} \theta_{\star} = -\mathrm{C}_{\mathrm{H}} \mathrm{U}(\theta - \theta_{\mathrm{s}}). \qquad (2.32)$$

$$\frac{E}{\rho} = \overline{q'w'} = -u_{*}q_{*} = -C_{W}U(q-q_{s}). \qquad (2.33)$$

 C_D , C_H and C_W are the respective bulk transfer coefficients. U, θ and q are measured at some reference height (usually 10 metres) and subscript s refers to surface measurement.

Considering the theory discussed in preceding sections it is obvious that the bulk transfer coefficients will not be constants, but will be strongly dependent on stability. Several authors (Deardorff (1968), Carson and Richards (1978)) have investigated this dependency. A similar analysis is presented here.

Neutral Conditions

For neutral conditions, eqs. 2.31 to 2.33 may be written in the general form

$$F_{a} = -u_{*}a_{*} = -C_{aN} U \Delta a \qquad (2.34)$$

where the subscript N refers to neutral stability and a is one of the variables U, θ or q.

A generalised form of eqs. 2.21 to 2.24 for neutral conditions is

$$\Delta a = \frac{a_{\star}}{k} \left[ln \left(\frac{z}{z_a} \right) \right], \text{ where } z_a \text{ is } z_o, z_H \text{ or } z_w \qquad (2.35)$$

and specifically

$$U = \frac{u_{\star}}{k} \left[\ln \left(\frac{z}{z_0} \right) \right].$$
 (2.36)

Substitution of eq. 2.35 and eq. 2.36 into eq. 2.34

yields

$$C_{aN} = k^2 / \left[\ln \left(\frac{z}{z_0} \right) \ln \left(\frac{z}{z_a} \right) \right] , \qquad (2.37)$$

and specifically

$$C_{\rm DN} = k^2 / (ln \left(\frac{z}{z_0}\right))^2$$
 (2.38)

Non-Neutral Conditions

Generalised forms of eq. 2.34 and eqs.2.22 to 2.24 are $F_a = -u_*a_* = -C_a U \Delta a$, (2.39)

$$\Delta a = \frac{a_{\star}}{k} \left[\ln \left(\frac{z}{z_a} \right) - \psi_a \right].$$
 (2.40)

Substitution into eq. 2.39 of eqs. 2.40, 2.22, 2.37

and 2.38 leads to the expression

$$\frac{C_a}{C_{aN}} = \left(1 + \frac{C_{aN}}{k^2} \left(\psi_M \psi_a - \frac{k\psi_a}{\sqrt{C_{DN}}} - \frac{k\psi_M}{C_{aN}} \right)\right)^{-1}, \qquad (2.41)$$

and specifically

$$\frac{C_{\rm D}}{C_{\rm DN}} = \left(1 + \frac{C_{\rm DN}}{k^2} \left(\psi_{\rm M}^2 - \frac{2k\psi_{\rm M}}{\sqrt{C_{\rm DN}}}\right)\right)^{-1}.$$
(2.42)

Eqs. 2.41 and 2.42 give the ratio of the transfer coefficients to their neutral value as a function of stability. For a given stability (z/L), ψ_a and ψ_M may be evaluated from eqs. 2.26 to 2.30.

Roughness lengths do not appear explicitly in eqs. 2.41 and 2.42, but they are implicitly specified by the selected neutral transfer coefficients.

Bulk Richardson Number

The stability length L, as defined by eq. 2.8, is difficult to estimate directly unless actual measurements of heat and moisture fluxes are available. From the established relations of Section 2.1.2 however, it is possible to obtain an expression for L in terms of a measurable bulk stability parameter called the Bulk Richardson Number, defined as

$$Ri_{B} = \frac{gz}{T_{v}} \frac{(\Delta \theta + 0.61T_{v} \Delta q)}{U^{2}} . \qquad (2.43)$$

The Monin-Obukhov similarity functions for temperature and moisture profiles are identical (see eq. 2.17 and eq. 2.18), indicating similar transfer mechanisms for heat and moisture. From now on the two will be considered together, assuming equality of bulk transfer coefficients and roughness lengths. Subscript HW will be used.

Substituting for $\Delta\theta$, Δq and U in eq. 2.43 from eq. 2.22, eq. 2.23 and eq. 2.24 gives

$$\operatorname{Ri}_{B} = \frac{gz}{T_{v}} \frac{\begin{pmatrix} \theta_{\star} \\ \overline{k} \end{pmatrix} + 0.61T_{v} & \frac{q_{\star}}{k} \end{pmatrix} \left(\ln \left(\frac{z}{z_{HW}} \right) - \psi_{HW} \right)}{\left(\frac{u_{\star}}{k} \left(\ln \left(\frac{z}{z_{O}} \right) - \psi_{M} \right) \right)^{2}}$$

Substituting eqs. 2.37 and 2.38 and rearranging gives

$$\mathrm{Ri}_{\mathrm{B}} = \frac{z \mathrm{kg}(\theta_{\star} \mathrm{u}_{\star} + 0.61 \mathrm{T}_{\mathrm{v}} \mathrm{q}_{\star} \mathrm{u}_{\star})}{\mathrm{u}_{\star}^{3} \mathrm{T}_{\mathrm{v}}} - \frac{\begin{pmatrix} \mathrm{k} \sqrt{C_{\mathrm{DN}}} \\ \mathrm{C}_{\mathrm{HWN}} \end{pmatrix}}{\begin{pmatrix} \mathrm{k} \\ \sqrt{C_{\mathrm{DN}}} \end{pmatrix}} - \frac{\psi_{\mathrm{HW}}}{\mathrm{HW}} + \frac{1}{\mathrm{HW}} + \frac{\mathrm{k} \mathrm{HW}}{\mathrm{HW}} + \frac{\mathrm{HW}}{\mathrm{HW}} + \frac{\mathrm{K} \mathrm{HW}}{\mathrm{HW}} + \frac{\mathrm{HW}}{\mathrm{HW}} + \frac{\mathrm$$

and the first term, by definition, is z/L, so

$$\operatorname{Ri}_{B} = \frac{z}{L} \quad \Phi\left(\frac{z}{L}\right) \qquad (2.44)$$
where $\Phi\left(\frac{z}{L}\right) = \frac{\left(\frac{k\sqrt{C_{DN}}}{C_{HWN}} - \psi_{HW}\right)}{\left(\frac{k}{\sqrt{C_{DN}}} - \psi_{M}\right)^{2}}$.

The relationship of C_a/C_{aN} to Ri_B has not been formally derived but is presented in graphical form in Figures 2.1 and 2.2. These are composite plots for the stable and unstable cases showing the relations:

(a) C_D/C_{DN} , $C_{HW}/C_{HWN} \sim f(Ri_B)$, (b) $\frac{z}{L} \sim f(Ri_B)$, (c) ϕ_M , $\phi_{HW} \sim f(\frac{z}{L})$.

In view of the uncertainty of the recent formulations of Hicks (1976) for $\phi_{M,H,W}$ at higher stability (eqs. 2.20 and 2.21), the log-linear form eq. 2.18 has been plotted over the whole range of (z/L) in Figure 2.1 for reference. Also plotted is the curve for C_D/C_{DN} resulting from the use of eq. 2.18 only; it can be seen that C_D (and hence stress) vanishes for low values of $\operatorname{Ri}_B(\sim 0.2)$. The curves for C_{HW}/C_{HWN} and ϕ_{HW} have not been plotted in Figure 2. since they are very similar to C_D/C_{DN} and ϕ_M respectively.

Neutral Transfer Coefficients at 10 m

Several authors provide estimates of the 10 m neutral transfer coefficients $C_{\rm DN}$, $C_{\rm HN}$ and $C_{\rm WN}$ arising from extensive fiel measurements of profiles and eddy fluxes over water bodies. These authors invariably warn against the use of neutral coefficients in non-neutral conditions.



FIGURE 2.1 Stability relationships - stable case. Dashed lines indicate use of the log-linear relation eq. 2.18 only



FIGURE 2.2 Stability relationships - unstable case



authors

Figure 2.3 shows four differing descriptions of $C_{\rm DN}$. The slight increase of $C_{\rm DN}$ with velocity is commonly observed. At low wind speeds the situation is unclear, however Hicks (1972) reports aerodynamically smooth behaviour with $C_{\rm DN} \sim 1.0 \times 10^{-3}$.

Values for $C_{\rm HN}$ and $C_{\rm WN}$ between 1.3 x 10^{-3} and 1.5 x 10^{-3} appear suitable for the range of wind speeds of interest (Hicks (1975), Hicks (1972), Pond, Fissel and Paulson (1974)). Francey and Garratt (1978) found a smaller value of $C_{\rm HN}$ exhibiting wind speed dependence. Even if this is the case, sensible heat transfer at the reservoir surface is insignificant when compared to latent heat transfer.

2.1.4 Internal Boundary Layers

When air from the land flows over a body of water, the flow is modified due to the change in surface roughness, temperature and humidity. An internal boundary layer develops over the water surface and equilibrium conditions are set up in the lower portion of this layer. Hence, in the bottom portion of the internal boundary layer, advective effects are small and the constant flux layer relations of the previous section are applicable

A number of models of internal boundary layer development and subsequent spatial distribution of fluxes have appeared in the atmospheric sciences literature. These models employ either a mixing length hypothesis (Taylor (1970), Weisman (1975)) or a turbulent energy closure scheme (Peterson (1969)). Both methods suffer limitations. Weisman assumes the similarity functions (eq. 2.10 to eq. 2.12) hold throughout the layer, thereby forcing the solution of layer development. He finds his solution to be strongly dependent on the mixing length scale height and although

he presents some justification for the "correct choice" of scale height, the results must be considered tentatively.

No solution to boundary layer development will be attempted here. However, it is necessary to recognise the existence of this layer in the reservoir situation and to ensure that measurements are conducted in the equilibrium sublayer where the established bulk transfer equations hold. Petersen (1969) indicates that the fetch must be 100 times the observation level for equilibrium to be assured. Hicks (1975) suggests a cautious fetch/height ratio of 1000 to ensure that the effect of upwind non-uniformities are minimised. On the basis of these and other guidelines, meteorological sensors described in the next chapter were mounted so as to have a minimum fetch/height ratio of 200. Lower measurement levels were precluded due to the possibility of the raft superstructure modifying the airflow.

2.2 RADIATION TRANSFERS BETWEEN AIR AND WATER

To enable an investigation of the diurnal cycle of heating and mixing in the reservoir surface layer, information on the diurnal cycle of radiative transfers between the air and the water is required. This contrasts with long term (seasonal) reservoir models which generally require only daily integrals of radiation.

Some simple expressions for radiation calculation are set out below. These are taken directly from the T.V.A. (1972) report to which the reader is referred for further detail. While there are more accurate formulations of radiation transfer available, the added complexity is not warranted here in view of the good results presented in the next chapter.

2.2.1 <u>Solar Radiation</u>

The T.V.A. (1972) report sets out in detail the formulae for computing solar radiation at the surface, incorporating atmospheric attenuation, reflection and cloud effects. A summary of these appears below, for use in subsequent chapters.

Extra-terrestrial Solar Radiation

The radiation Q_{so} impinging on a horizontal plane at the top of the atmosphere is

$$Q_{so} = \frac{I_o}{r} \sin \alpha,$$
 (2.45)
with I solar constant = 1353W/m²,

r radius vector, defined below,

α solar altitude (radians).

The solar altitude is determined from the expression

$$\sin \alpha = \sin \phi \sin \delta + \cos \phi \cos \delta \cosh,$$
 (2.46)

with ϕ latitude (radians),

δ declination of sun (radians),

h local hour angle of sun (radians).

The variables r and δ may be considered constant over a day and are given by:

$$r = 1 + 0.017 \cos\left(\frac{2\pi}{365}(186 - d)\right)$$
 (2.47)

$$\delta = 23.45 \left(\frac{\pi}{180}\right) \cos\left(\frac{2\pi}{365}(172 - D)\right)$$
 (2.48)

Computation of the local hour angle, h, requires a two part formula:

(a) for the sun east of the local meridian

$$h = ST + 12 - DTSL + ET$$
, (2.49)

(b) for the sun west of the local meridian h = ST - 12 - DTSL + ET (2.50)

with ST standard time of time zone,

DTSL difference between local and standard time,

ET the equation of time.

ET, accounting for the apparent irregular angular motion of the sun, is given by:

where d =
$$\frac{2\pi}{365.242}$$
 (D-1)
and D is the day number of the year. h must be converted to

and D is the day number of the year. h must be converted to radians for use in eq. 2.46.

Methods to compute atmospheric absorption and scattering are also provided in the T.V.A. (1972) report. An alternative approach, detailed in the next chapter, uses the geometric relationships above together with known daily maximum global radiation figures to compute approximately the global radiation throughout a day.

2.2.2 Water Surface Radiation

A water surface emits radiation in the wavelength range 6.8 μ to 100 μ for normal temperatures around 300K. Plancks' Law may be applied to determine the total emission (integrated over all wavelengths), i.e.

$$Q_{LR} = \varepsilon \sigma T^4$$
 (2.52),

with ε emissivity (~ 0.96)

 σ Stephan-Boltzman constant ($\sigma = 2.0411 \times 10^{-7} \text{kJ/m}^2 \text{ hr } \text{K}^4$),

T the absolute temperature of the water surface.

Water is practically opaque for wavelengths greater than 2.65 μ , so all long-wave transfers, including emissions, must come from a very thin surface layer. In this respect, long-wave radiation transfer is similar to turbulent, sensible and latent heat transfers which must also come from a surface conductive layer. In other words, their effects on the heat distribution in the water body will be similar.

2.2.3 Atmospheric Radiation

While some of the surface emitted long-wave radiation passes through the atmosphere into space, much is absorbed by atmospheric constituents (water vapour, carbon dioxide, ozone) and re-emitted back to earth. The T.V.A. (1972) report summarises a number of empirical formulae for calculating this atmospheric radiation for clear skies, based on surface vapour pressure and air temperature measurements. Swinbank's (1963) formula is preferred:

$$Q_{I,A} = 0.937 \times 10^{-5} \sigma T_2^{-6} (1 - R_a),$$
 (2.53)

with T_2 air temperature at 2 m height,

 R_a water surface reflectivity (~ 0.3). Field tests show this formula to be accurate to $\pm 12Wm^{-2}$.

Clouds emit long-wave radiation and are accounted for by a factor in eq. 2.53:

 $Q_{LAC} = (1+0.17C^2) Q_{LA}$ (2.54) where C is the part of the sky covered with clouds, measured in tenths of the total sky.

The atmospheric radiation spectrum has its maxima near

14 μ , compared to the solar spectrum maxima at about 0.7 μ . The two spectra are almost completely separate, and hence solar and atmospheric radiation may be treated quite independently. Atmospheric radiation may be treated identically to water surface radiation, as described in the previous section.

2.2.4 Absorption of Solar Radiation in Water

Solar radiation penetrating the surface is absorbed within the water body, thereby heating it. Absorption of longer wavelengths occurs more rapidly so only the visible part of the solar spectrum (0.36 to 0.76 μ) penetrates below one metre. For depths greater than one metre the attentuation profile is well described by Beer's Law:

$$q(z) = Q_{s}e^{-bz}$$
 (2.55)

with Q solar radiation at the surface,

z depth,

b bulk extinction coefficient dependent on the turbidity
of the water.

To describe attenuation over the full depth of water, account must be taken of the wavelength dependency. The T.V.A. (1972) report recommends use of three extinction coefficients, i.e.:

$$q(z) = Q_{s}(a_{1}e^{-b_{1}z} - b_{2}z^{-b_{3}z} + a_{3}e^{-b_{3}z})$$
(2.56)

where the a and b coefficients vary depending on water turbidity.
CHAPTER 3

FIELD MEASUREMENTS OF METEOROLOGY

3.1 BACKGROUND

As discussed in Chapter 1, the overall aim of the Wellington Reservoir Study was to develop a numerical model incorporating all important mechanisms, including meteorological forcing. An initial task of this Project was to install a meteorological station on the reservoir to service the Study as a whole. A set of RIMCO meteorological sensors and a RIMCO Event Recorder were purchased for this purpose. These were installed with the assistance of staff from the CSIRO Division of Land Resources Management, on a raft constructed in the Civil Engineering workshop at the University of Western Australia (U.W.A.). Plate 3.1(a) shows the raft with event recorder, and Plate 3.1(b) shows a jarrah tree used as an anchor point and meteorological platform. A brief description of this system is given below.

The RIMCO Event Recorder is a data logging system designed to have very low power requirements, making it suitable for unattended operations at remote sites. Data are punched as ASCII characters onto paper tape and are readable at most computer installations. The normal mode of operation is to record events as they occur on any one of the 14 channels. The appearance of a particular channel code on the tape indicates that an event has occurred on that channel. One such event is the lapse of a time interval (5 or 6 minutes) as measured by a mechanical clock. Time



- PLATE 3.1(a) Raft and RIMCO system: Event Recorder, sensors for air temperature, water temperature and relative humidity, plus a solar charger for the recorder battery
- PLATE 3.1(b) Tree platform with RIMCO sensors for wind speed, wind direction and solar radiation



channel marks are thus interspersed with other channel marks on the tape. The Event Recorder is housed in a sealed cylinder and can be seen in the centre of the raft (Plate 3.1(a)) protected by a bullet-proof shield. A bank of solar cells, seen at the top of the 2 metre post, provides a charging current for the Recorder's Ni-Cad battery.

Whilst attractive in concept the Event Recorder system has some fundamental problems. Meteorological sensors designed to provide events for recording are generally deficient in both resolution and accuracy. Temperature and humidity sensors on the two metre post (Plate 3.1(a)) and wind speed, wind direction and solar radiation sensors (Plate 3.1(b)) all rely on mechanical movement to actuate reed relay closures. Understandably, these are not capable of achieving the accuracies attained by electronic sensors. If system failure occurs between visits, data recovery is often very difficult, since the time base must be inferred from an analysis of time marks.

Whilst the Event Recorder system was capable of providing useful data for the Study, requirements of high accuracy and resolution in this Project led to the assembling of a second complete set of instruments for use during the intensive fieldwork. This included construction of some of the sensors and most of the signal handling circuits. These instruments are described in detail in Sections 3.2 and 3.3. Sections 3.4 and 3.5 describe the processing of field data and subsequent computation of meteorological fluxes.

3.2 GENERAL EQUIPMENT FOR FIELDWORK

A brief description of the data recording equipment

and the power source used throughout the fieldwork is given below.

3.2.1 Data Recording

During the fieldwork phase of this Project, no sophisticated digital data acquisition system was available for recording meteorological or other data. The author was fortunate to procure on loan, from the CSIRO Division of Atmospheric Physics, a set of six Messmotors. A Messmotor is a precision DC motor which drives a six digit decade counter. The increment of the counter over a set interval (say one hour) is a measure of the integral of the input voltage. The box of Messmotors is shown in Plate 3.2 (No. 1).

A set of six high stability amplifiers was included (No. 2 in Plate 3.2) to provide buffering for meteorological sensor outputs and to amplify these outputs to the required 0-5 Volt range.

Multiple-point calibrations were conducted on each Messmotor-amplifier pair, giving operating expressions of the form: Input voltage = a x (counts/minute) + b.

Linearity was excellent. Subsequent calibrations and single-point checks throughout the fieldwork revealed high stability. An overall accuracy of ±1% can be assumed for the Messmotor system.

In the field, the counters were read and recorded manually once every hour. Readings were staggered by 30 seconds to ensure a precise hourly integral for each input. Errors introduced by this method of reading are negligible.

3.2.2 <u>Power</u>

Where possible instruments were purchased or constructed to run off batteries. Two heavy duty 12 **v**olt lead accumulator



PLATE 3.2

Raft - based instruments:

- 1. Messmotors
- 2. Amplifiers
- Anemometer pulse counterVAISALA relative humidity meter
- 4. VAISALA relative humidity 5. A.L.E. conductivity meter

batteries supplied ±12 volts to the amplifiers and also 24 volts to an inverter which, as required, supplied 240 VAC to a Digital Voltmeter (DVM) and other equipment. Other dry cells were used to power meteorological sensors, avoiding earth loops in the recording system.

3.3

METEOROLOGICAL INSTRUMENTATION FOR FIELDWORK

The meteorological instruments and associated data recording methods are described below for each of the parameters measured.

3.3.1 Wind Speed

A $3^{3}/_{4}$ " RIMCO cup anemometer was installed at a height of four metres on an aluminium mast, as seen in Plate 3.3 (No. 1). This instrument operates on the light-chopper principle with the output pulse train being integrated on a decade counter supplied with the anemometer (see Plate 3.2 No. 3). The counter readings were recorded and reset hourly. Relevant instrument specifications are:

- (a) starting speed 0.1 m/sec,
- (b) flow coefficient 1.74 m/rev.

The counter readings for the RIMCO Event Recorder anemometer mounted on the tree were also recorded manually for checking. The two units were in good agreement throughout the fieldwork. No independent calibrations were performed on either instrument.

3.3.2 Air Temperature

Air temperature was measured by a nominal $5k\Omega$ thermistor



PLATE 3.3

- Meteorological sensors: 1. RIMCO sensitive cup anemometer
- 2. Air temperature probe and shield
- 3. VAISALA relative humidity probe and shield
- 4. Net radiometer
- 5. Dry nitrogen supply

mounted at a height of three metres on the mast cross arm. The radiation shield seen in Plate 3.3 (No. 2) consisted of four horizontal discs separated by PVC spacers and painted black and white on inside and outside surfaces respectively. Disc size and spacing was determined in order to give radiation protection for sun angles > 5° , while causing no interference to natural ventilation.

This thermistor, like all thermistors in the system, was incorporated in a Wheatstone Bridge circuit. The output voltage was linearised by placing a $5k\Omega$ shunt resistance across the thermistor arm of the bridge and balancing the bridge at the bottom of the temperature range.

Extensive multiple-point calibrations were performed prior to field days to determine the operating expression for the thermistor circuit. Two-point (hot and cold) calibrations were also performed on the raft at the start and end of field days. Over the full period, accuracy was maintained within $\pm 0.2^{\circ}$ C.

3.3.3 Water Surface Temperature

Water surface temperature was measured with circuitry similar to that used for air temperature.

The water temperature probe mounting seen in Plate 3.4 (No. 1) was carefully designed to ensure that the probe remained just beneath the surface. The radiation shield was connected via hinged arms to the raft, giving the shield vertical and rotational freedom. Three buoys supported the shield at its corners. These in turn were weighted by a single submerged lead sinker attached with three nylon cords. The weight ensured that the buoys (and hence the



PLATE 3.4

Water temperature sensor:

 Probe and radiation shield
 Extension arm and pulley for conductivity/ temperature probe

probe) always followed wave troughs, but provided no upward inertia which would have caused the probe to surface.

Calibration of the water temperature probe was conducted simultaneously with that for air temperature. On only one occasion did observed errors fall outside the range $\pm 0.1^{\circ}$ C.

3.3.4 Relative Humidity

A VAISALA HM11 humidity meter was purchased for the Project. It uses a thin film capacitive sensor which responds rapidly to relative humidity over the full 0 to 100% range. The manufacturer gives the following specifications:

(a) humidity range - 0 to 100% RH,

- (b) temperature range -40° C to 80° C,
- (c) response time 1 sec for 90% response,
- (d) temperature coeff. 0.05% per $1^{\circ}C$,
- (e) overall accuracy ±2%.

The humidity probe was mounted adjacent to the air temperature probe in an identical radiation shield (see Plate 3.3 No. 3). No signal conditioning was required prior to amplification and recording by a Messmotor.

Instrument calibration was performed prior to fieldwork by adjusting the meter output at known humidities over saturated salt solutions, namely Lithium Chloride and Potassium Sulphate. Overall, the instrument functioned very well and within the manufacturer's specifications, except for a tendency to drift slowly upward when humidity was high. The meter is seen in Plate 3.2 (No. 4).

3.3.5 <u>Net Radiation</u>

A SOLAR RADIATION INSTRUMENTS LTD. Net Radiometer (seen in Plate 3.3 No. 4) was obtained on loan from the CSIRO Division of Land Resources Management for the duration of the fieldwork. The operating principles of this type of instrument are given by Funk (1959). The CSIRO calibration certificate details are:

(a) sensitivity at 20⁰C -

short-wave: 0.332 mV/mWcm²

long-wave: 0.331 mV/mWcm²,

(b) accuracy of calibration $- \pm 2.5\%$

The thin polythene hemispheres which act as a windshield for the upper and lower thermopiles were inflated with dry nitrogen gas. The nitrogen bottle and gas lines are seen in Plate 3.3 (No. 5). A slow flow of gas was regulated by a needle valve, adjusted to give several bubbles of exhaust gas per minute through a jar filled with water.

The net radiometer functioned well over the experimental period. No direct calibration was carried out and the CSIRO calibration data were used. Calculations detailed in the next section show that the net radiation data agree with available formulae for both short-wave and long-wave radiation. No significant absolute errors are apparent, however, a small relative (percentage) error, in the range +0 to -4%, has been estimated from the calculations. This is quite acceptable and may be due to instrument aging or slight opacity of the polythene caused by photo-oxidation by ultra-violet light (see Funk (1959)).

3.3.6 Solar Radiation Absorption

Results from the January and February field days indicated that the form of solar radiation absorption in the reservoir was a major factor in the subsequent behaviour of the surface layer. As it was not possible to purchase or borrow an underwater solarimeter at that stage, a unit was designed and manufactured. This is shown in Plate 3.5.

The thermopile, originally from a solarimeter, was obtained from the CSIRO. It was seated on a PVC base and encased in a brass cylinder. The glass faceplate was sealed with an 0 ring.

The unit was held horizontally by three arms suspended from a point on the signal cable which was also used to lower the probe. To avoid noise and signal loss in the cable, an operational amplifier was incorporated in the cylinder.

A test was performed on two faceplates of different thickness to determine their transmittance characteristics and hence whether they might modify the solar spectrum being measured beneath the water. Figure 3.1 shows copies of the plots produced by a Grating Spectrophotometer. They show the transmittance or absorbance of the two faceplates over the wavelength ranges $0.8 - 2.5 \mu$ and 2.5 to 3.4 μ . Also shown is the true 100% line of the instrument. Absolute values are of little interest but the important points are:

 the transmittance is high and varies little over the range 0.8 to 2.7 μ. It is obviously also high in the visible range, 0.3 to 0.8 μ,

ii) the transmittance falls sharply after 2.7 μ.
 Comparing these results with Table 3.1, taken from
 Irvin and Pollack (1968), it can be seen that the glass faceplates



PLATE 3.5 Underwater solarimeter showing: (a) signal cable, suspension arm and wire (b) thermopile, amplifier circuit card





FIGURE 3.1 Spectrophotometer plots of transmittance (absorbance) for two glass faceplates for the underwater solarimeter

.

λ (μ)	Re	k	11.6	λ (μ)	nr	k	n;
0.20	1.424	8×10^{-2}	1.3×10^{-7}	2.25	1.290	17	0.0003(
0.25	1.377	3×10^{-2}	$6.0 imes 10^{-8}$	2.30	1.286	23	0.00042
0.30	1.359	$1.5 imes 10^{-2}$	3.6×10^{-8}	2.35	1.282	30	0.00056
0.35	1.349	3×10^{-3}	8×10^{-9}	2.40	1.276	42	0.00080
0.40	1.343	1×10^{-3}	$3 imes 10^{-9}$	2.45	1.270	61	0.00118
0.45	1.339	2×10^{-4}	7×10^{-10}	2.50	1.246	83	0.00165
0.50	1.336	$2.5 imes 10^{-4}$	8×10^{-10}	2.55	1.213	97	0.00196
0.55	1.334	$3.5 imes 10^{-4}$	$1.5 imes 10^{-9}$	2.60	1.180	99	0.00204
0.60	1.332	$1.5 imes 10^{-3}$	7×10^{-9}	2.625	1.160	109	0.00227
0.65	1.331	$2.5 imes 10^{-3}$	$1.3 imes 10^{-s}$	2.65	1.140	131	0.00276
0.70	1.330	0.006	$3.3 imes 10^{-8}$	2.70	1.134	235	0.00504
0.75	1.329	0,025	1.49×10^{-7}	2.75	1.133	1 100	0.02401
0.76	1.329	0.026	1.5×10^{-7}	2.80	1.232	4 212	0.09361
0.80	1.328	0.021	1.34×10^{-7}	2.90	1.310	10 580	0.2435
0.806	1.328	0.020	1.2×10^{-7}	2.95	1.325	11 700	0.2740
0.85	1.327	0.041	2.77×10^{-7}	3.00	1.351	10 860	0.2586
0.90	1.328	0.067	4.80×10^{-7}	3.10	1.426	7 430	0.1828
0.95	1.327	0.365	2.76×10^{-6}	3.20	1.509	3 700	0.09422
0.97	1.327	0.46	3.55×10^{-6}	3.30	1.470	1 650	0.04333
1.00	1.326	0.355	2.82×10^{-6}	3.40	1,449	698	0.01888
1.05	1.325	0.131	1.10×10^{-5}	3.50	1.423	334	0.00930
1.06	1.325	0.128	1.07×10^{-6}	3,60	1.402	198	0.00567
1.10	1.324	0.190	1.66×10^{-6}	3.75	1.372	119	0.00355
1.15	1.3225	0.800	7.32×10^{-6}	3.83	1.358	111	0.00338
1.19	1.323	1.05	9.9×10^{-6}	4.00	1.349	151	0.00481
1.20	1.323	1.020	9.74×10^{-6}	4.50	1.341	411	0.01472
1.25	1.322	0.890	8.85×10^{-6}	4.66	1.338	468	6.00173
1.258	1.322	0.85	8.8×10^{-6}	4.50	1.336	431	0.01647
1.30	1.321	1.08	11.17×10^{-6}	5.0	1.331	308	0.01225
1.35	1.320	2.70	29.0×10^{-6}	5.26	1.318	229	0.00959
1.40	1.320	13	14.48×10^{-5}	5.5	1.303	276	0.01208
1.45	1.319	26.0	3.00×10^{-4}	5.8	1.266	699	0.03226
1.50	1.318	17.3	0.0002065	6.0	1.313	2 138	0.10208
1 55	1.317	9.6	0.0001184	6.05	1.324	2 328	0.11208
1.60	1.316	6.2	Na 0.0000789	6.4	1.347	852	0 04339
1 65	1.316	5 1	NO.0000670	6.5	1.338	794	0.04107
1 66	1.315	5.0	0.000066	7.0	1 323	618	0 03443
1 70	1.315	5.15	0.0000697	7 5	1.303	579	0 03456
1.75	1 314	6 4	0.0000591	8.0	1 203	566	0 03603
1.80	1 312	8.0	0.0001146	S 5	1 286	557	0.03768
1.85	1 311	9.5	0.0001399	9.0	1 269	566	0 04054
1 90	1 309	80.5	0.001217	9.5	1 245	579	0 04377
1.00	1 307	114 0	0 00176	10 0	1 914	668	0 05316
1.95	1 307	110	0 001707	10.5	1 185	826	0.0690
2.00	1,304	68	0.001082	11	1,151	1 165	0.1021
2.05	1 302	41	0.0006689	11 5	1 1.15	1 672	0 1530
2 10	1 300	26	0 0004345	12	1 160	2 101	0 2092
2.15	1 296	10	0 000325	12 5	1 10	2 451	0 2438
2.10	1 200	16	0.00020	12.0	1 200	2 201	0.2403
2.20	1 200	15 5	0.000.200	12 5	1 915	2 021	0 3909
	1.202	10.0		1.1.0	1.210	- 000	0.0102

Water: Absorption Coefficient k and Real (n_r) and Imaginart (n_i) Parts of Index of Refraction versus Wavelength λ

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TABLE 3.1

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Absorption coefficients for water (Irvine and Pollack (1968)) will transmit all wavelengths of interest below the water. The absorption coefficient in water increases rapidly for wavelengths > 2.6 μ , just before the corresponding increase for glass. Furthermore, almost all the power in the solar spectrum is contained at wavelengths below this level.

Unfortunately, due to failure of the thermopile, it was possible to obtain only one data set for the absorption profile and then not without complication. The thermopile was not temperature compensated and consequently, due to solar heating of the sealed cylinder prior to use, the output showed a large negative offset at a depth of three metres as seen in Figure 3.2. Nevertheless, the offset was constant over the period of investigation (checked by consistency of successive profiles) and so some useful analysis is still possible.

Because only a small amount of radiation reaches the three metre level (5% to 12% from the T.V.A. (1972) report) the overall shape of the attenuation curve is relatively insensitive to even large percentage errors at that depth. Therefore, for the purposes of analysing Figure 3.2 it can be reasonably assumed that 10% of the solar flux penetrates to three metres. This allows definition of a new origin and re-scaling of the data, taking the surface reading as 100%.

A simple procedure may now be used to determine an attenuation profile of the form given by eq. 2.56:

- (a) plot the data $q(z)/Q_s$ vs. z on a log-linear graph,
- (b) determine the values of a₁ and b₁ for the lowest linear portion of the plot,
- (c) subtract the curve $a_1 e^{-b_1 z}$ from the original data. Replot the remaining flux values to determine a_2 and b_2 etc.



FIGURE 3.2 Solar radiation attenuation profile measured by the underwater solarimeter. Error bars indicate the reading accuracy

The resultant expression for the data collected is

$$q(z)/Q_s = 0.54e^{-0.561z} + 0.30e^{-6.89z} + 0.16e^{-69z}$$
 (3.1)

The value of b_3 is tentative; it indicates that 16% of radiation is absorbed essentially in the first 2 cm.

Whilst the expression has been determined with reasonable confidence, this aspect of field measurement should receive close attention in any future studies.

3.4 DATA PROCESSING

The fieldwork associated with this Project was conducted in the early months of 1976. Reliable data sets were obtained for four separate days during this period, namely January 15 (15 01 76), February 3 (03 02 76), February 5 (05 02 76) and April 5 (05 04 76). The methods employed to process these data are described below.

3.4.1 Data Storage

In the field, the meteorological data in the form of hourly Messmotor counter readings were entered onto coded data sheets. Also recorded were hourly spot readings of meteorological sensor outputs to provide a check for, and supplement to, the Messmotor recordings. Periodically, observations of wave height, cloud cover and wind direction was also recorded.

Data from coded sheets were punched onto cards and then transferred to disc on a large mainframe computer, where some minor editing was performed.

3.4.2 Data Reduction

From the calibration information obtained, as described

in Section 3.3, calibration expressions were determined for each instrument for individual field days. Checks were performed where redundant calibration information was available, resulting in estimates of measurement accuracy summarised below:

Parameter	Accuracy
Wind speed	±0.2 m/sec
Air temperature	±0.2°C
Water temperature	±0.15 ⁰ C
Relative Humidity	±3%
Net Radiation	+0, -3 mW/cm ²

Processed meteorological data for the four field days appear in Appendix Al. Included in the data are readings from the Event Recorder anemometer, pyranometer and a Kipp Solarimeter which was used in the April fieldwork.

To facilitate examination of the data, computer plots of individual parameters were produced. Examples of these plots for the day 050276 are displayed in Figure 3.3(a) and (b). The timebase on all plots was in hours, starting either from midnight or 0400 hours. Varying vertical scales and zeros were used to enhance the plots. Points to note when viewing them are as follows

- 1. The stepped plots indicate that data were averaged over the various periods (usually hourly). Crosses represent the spot readings taken. The accuracy of the spot readings varies depending on the parameter fluctuations and the instruments response. In particular, readings taken from the humidity meter may be quite unrepresentative of the mean humidity.
- The dashed stepped line on the wind speed plots indicates data from the Event Recorder anemometer.





averages for 05 02 70 short-wave radiation

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- 3. Errors in the data averages become obvious when viewing the plots. Identification of these errors was the fundamental reason for plotting the data. These errors may be due to instrument failure or reading error. They have been corrected as far as possible, as described in the next section.
- 4. Inspection of the short-wave radiation plots reveals that, as expected, the Event Recorder pyranometer resolution is too coarse for the present application.

3.4.3 Time Series Synthesis

Monin and Kolesnikova (1968) indicate that micrometeorological fluctuations tend to have a spectral gap at a period of about 10 minutes: turbulent eddies have timescales somewhat shorter than 10 minutes and large scale circulations have timescales somewhat larger than 10 minutes. On this basis it may be considered optimal to measure 10 minute averages of meteorological variables. This was unfortunately not practical during the labour-intensive field experiments of this Project.

From inspection of the data (hourly averages and spot readings) plus additional processed data from the Event Recorder system, it proved possible to synthesise time series of the meteorological variables. The latter source of data is of doubtful quality and so was used primarily to provide time base information for wind speed, the most variable parameter.

The method of time series synthesis was as follows. Large transparent copies of individual plots (as displayed in Figure 3.3) were overlaid with transparent graph paper and, where applicable, underlaid with plots of the Event Recorder data. Any available supplementary data were marked on the overlay (e.g. profiling probe surface temperature data). Conserving the integral of verified Messmotor averages and giving appropriate attention to all the additional information, a smooth sequence of line segments was then drawn to fit the data. Points from these new representations were subsequently fed back into the computer. The resultant data set contained mostly half hourly values but in a few cases this interval was decreased to 15 minutes in order to describe changes observed on the Event Recorder plots. Copies of these data files appear in Appendix A2.

To a small degree this double handling of data may have degraded overall accuracy. However, the procedure provided a reasonably accurate representation of the daily cycle of meteorological variables, making it possible to compute the corresponding cycles of fluxes. Step changes, which may possibly cause problems in numerical simulation models, have been removed. Importantly, the resolutions of wind speed changes in the data has been improved In following chapters, terms dependent on the third power of the wind speed are computed; neglect of short term peak values would introduce large errors.

3.5 FLUX COMPUTATIONS

From the processed meteorological data the various radiative and turbulent fluxes may be computed, as described in Chapter 2. Although a numerical model of a reservoir will incorporate its own flux computation, it is instructive to calculate these here in order to examine the importance of atmospheric stability effects in the reservoir situation.

3.5.1 Radiative Fluxes

From an inspection of the data it is evident that net radiation is the only radiation measurement with sufficient resolution to describe diurnal variability. In view of this the following computations were performed in order to predict the various radiation components plotted in Figures 3.4(a) to (d).

Net radiation may be expressed in terms of its various components as defined in Section 2.2:

$$Q_{N} = (1-R) Q_{S} + Q_{LAC} - Q_{LR}$$
 (3.2)

The short-wave reflectance, R, is defined below .

 $(1-R)Q_{\rm S}$ is the main term in the balance; it is that part of the incoming short-wave radiation which penetrates the water surface and is absorbed below. This term was evaluated from eq. 3.2 using measured $Q_{\rm N}$, with $Q_{\rm LAC}$ and $Q_{\rm LR}$ calculated from eq. 2.54 and eq. 2.52. It is plotted in Figures 3.4(a) to (d) as a diamond symbol. Also plotted as dotted lines are $Q_{\rm LAC}$ and $Q_{\rm LR}$. Note that downward radiation fluxes are considered here as being positive.

As a check on the estimate of the short-wave component, a simplified independent calculation was performed. Values for the normal and diffuse components of short-wave (Q_{sN} and Q_{sD} respectively) were obtained from Spencer (1976). These were used in the formulae of eq. 2.46 to eq. 2.51 to produce a diurnal cycle of short-wave at Wellington Reservoir. After subtracting the reflected component, given in the T.V.A. (1972) report as R Q_s where

$$R = 1.18a^{-0.77}$$
(3.3)

for clear skys, the results were plotted in Figures 3.4(a) to (d) as the dashed line. Agreement between this curve and the values





(b) Radiation fluxes for 03 02 76

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from eq. 3.2 is good for clear days (eg. 05 02 76). The curve also serves as a reference for days when cloud or smoke were present

An encouraging feature of the plots is the behaviour of the two long-wave radiation formulae. It was not necessary to force the night-time zero for short-wave; it resulted from the balance of eq. 3.2. The method slightly under predicts the shortwave during daytime hours, however for this Project the accuracy is acceptable.

The Event Recorder pyranometer was designed to give one count per 14.8 mW Hr cm⁻². This resolution was too coarse to provide a time representation similar to those of Figure 3.4(a) to (d). It was decided however to check the integrated values of this instrument against the integral of the calculated and predicted curves. For the day 05 02 76 between the times 0800 and 1300 the pyranometer, predicted (eq. 3.2), and calculated integrals were respectively

414 433 448 mW Hr cm⁻².

Other comparisons confirmed the 4% difference between values, although the pyranometer exhibited poor cosine response for low solar altitudes.

3.5.2 Turbulent Fluxes

Bulk aerodynamic formulae described in Section 2.1.3 are suitable for computing turbulent fluxes of heat, water vapour and momentum from the meteorological data. As there are a number of interesting aspects to this computation, a flow diagram of the program has been included in Appendix Bl and a copy of the program appears in Appendix Cl.

Neutral Transfer Coefficients

Following the discussion in Section 2.1.3, the choice of neutral transfer coefficients applicable to a measurement height of ten metres was as follows:

$$C_{DN10} = 1.0 \times 10^{-3}$$
 U $\leq 5m/sec$
= (1.0 - 0.07(U-5)) x 10⁻³ U > 5m/sec
 $C_{HWN10} = 1.35 \times 10^{-3}$

The relatively low wind speeds experience on the four field days have been taken into account in the above choice

Effect of Measurement Height

The transfer coefficients must be altered if measurements are made at other than the standard ten metre height. In view of the discussion in Section 2.1.4 regarding the internal boundary layer problem, measurement heights for wind speeds and air temperature/ humidity were chosen to be four and three metres respectively.

The neutral drag coefficient for four metres is given

$$C_{DN4} = C_{DN10} \left[\left(\ln \left(\frac{10}{z_0} \right) \right)^2 / \left(\ln \left(\frac{4}{z_0} \right) \right)^2 \right]$$
(3.4)

with zo computed from eq. 2.38. Similarly

$$C_{\text{HWN3}} = C_{\text{HWN10}} \begin{bmatrix} \ln\left(\frac{10}{z_{o}}\right) & \ln\left(\frac{10}{z_{\text{HW}}}\right) \\ \frac{\ln\left(\frac{3}{z_{o}}\right) & \ln\left(\frac{3}{z_{\text{HW}}}\right) \end{bmatrix}}{\ln\left(\frac{3}{z_{\text{HW}}}\right)} \end{bmatrix}$$
(3.5)

with z_{HW} from eq. 2.37.

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[®] Vapour Pressure and Specific Humidity Calculations

Wigley (1974) gives a formula for the saturation vapour pressure e_s:

$$e_s = 1013.25 \exp[13.3185t - 1.9760t^2 - 0.6445t^3 - 0.1299t^4]$$

(3.6)
where $t = 1 - \frac{T_s}{T}$.

T and T_s are the air temperature and steampoint temperature respectively (both in O K). He shows this formula to be accurate to within 0.1% over the wide range (- $50^{O}C < T < 140^{O}C$).

The vapour pressure of unsaturated air is then

$$e = \frac{\phi e_s}{100} \tag{3.7}$$

where ϕ is relative humidity (%). Specific humidity is given by

$$q = \frac{0.662e}{p}$$
 (3.8)

where p is atmospheric pressure.

Stability Correction to Transfer Coefficients

Figures 2.1 and 2.2 show the correction to the drag coefficient as Ri_{B} varies. These graphs (corrected for measurement height) are useful for manual flux calculations; Ri_{B} may be calculated from field observations via eq. 2.43. The graphs are not useful for computing purposes however unless empirical expressions for the relations $C_a/C_{aN} \sim f(\text{Ri}_{B})$ are obtained.

Hicks (1975) suggests an alternative method of stability correction which is attractive from a computing viewpoint. The fluxes may be calculated using an estimate of the transfer coefficients C_D and C_{HW} . A provisional estimate of z/L may then be obtained from eq. 2.9 and using this, C_D and C_{HW} may be corrected with eq. 2.41 and eq. 2.42. The process is repeated iteratively until z/L converges to a constant value.

This procedure (see Appendices Bl and Cl) was found to perform very well. After starting the coefficients at their neutral values, satisfactory convergence usually occurred within five steps. For sequential calculations, it would be more efficient to use the previously determined coefficients as commencement values for a new iteration.

Results of Calculations

Figure 3.5(a) to (d) are plots presenting the results of calculations for the four field days.

Examining first the plots of transfer coefficient and stabilities it can be seen that both of these vary markedly over any day. The horizontal lines on the plots represent (from bottom up) the level of C_{DN4} , C_{HWN3} and $Ri_{B} = z/L = 0$. During early and mid-morning the atmospheric layer is very unstable in some cases (see Figure 3.5(b)). This is due to the combined effect of light winds, a negative air-water temperature differential and the buoyancy of water vapour. During calm hot afternoon the stability is reversed, with a positive temperature differential dominating the vapour buoyancy. Corresponding to the stability variations, the transfer coefficients vary by a factor of three or more, leading to enhanced transfers (eg. evaporation) in the morning and suppressed transfers on hot afternoons. If the calculations are correct there are serious implications regarding the practice of using constant transfer coefficients for all calculations. Hicks (1975), discussing unstable oceanic conditions, concludes that,

"... in winds of less than about 2 m s⁻¹, greatly enhanced transfer coefficients should be common. In such light winds, it is quite probable that the atmospheric stability exceeds the limits imposed by our present knowledge of the flux-gradient relationships. This, in itself, is sufficient reason to argue against the blind adoption of the conventional 10 m reference level for the deduction of eddy fluxes from bulk aerodynamic data; the use of lower elevations when the magnitude of L is small might be more advisable". (1975, 522)





FIGURE 3.5(a) Turbulent fluxes, transfer coefficients and stability parameters for 15 01 76





(b) Turbulent fluxes, transfer coefficients and stability parameters for 03 02 76





(c) Turbulent fluxes, transfer coefficients and stability parameters for 05 02 76







In considering the applicability of the foregoing method of calculation, two observations can be made. Firstly, in the reservoir case it is of paramount importance that measurements be made within the equilibrium sublayer of the internal boundary layer. In retrospect, lower measurement heights would have been preferable, although proximity to the raft may have caused problems Secondly and of importance, the water surface temperature measured and used in the stability calculation may not represent the actual 'skin temperature' of the surface in light wind conditions. This skin temperature will be closer to the air temperature for all stabilities, reducing the temperature differential and hence also the stability effect. The only tangible means of obtaining the skin temperature would be by direct measurement of the emitted long-wave radiation with a Barnes Radiometer or a similar instrument. For the purpose of this Project it must be accepted that stability effects may be over-estimated.

In view of the latter point, one modification to the flux computations was considered necessary. Little is known about the surface layer similarity functions ($\phi_{M,H,W}$ from eq. 2.16 and eq. 2.17) for instabilities beyond $z/L \sim -1$. Considering the uncertainly of stability determination beyond this point and the likelihood of obtaining unrealistically high results, fluxes were re-computed with values of the transfer coefficients held below the value appropriate to z/L = -1. Hence the fluxes plotted in the early mornings and some evenings have been slightly suppressed.

As a check on the iteration procedure and on all of the surface layer relations stated or derived in Section 2.1, Ri_B was calculated by two methods:
- i) from the meteorological data via eq. 2.43.
- ii) from the derived relation eq. 2.44.

The agreement between the two was excellent for the unstable and slightly stable regimes (within 3%) and reasonable for higher stabilities (within 10%). The high stabilities involve use of the similarity function eq. 2.21 which may be inaccurate.

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CHAPTER 4

RESERVOIR SURFACE LAYER OBSERVATIONS

In this chapter, surface layer temperature and salinity profiles measured at the Wellington raft station are presented, together with a general description of the diurnal cycle apparent in these profiles. This chapter should therefore provide a qualitative understanding of reservoir surface behaviour prior to the theoretical treatment in Chapter 5.

On each of the four field days selected for analysis, the reservoir surface layer observations consisted of hourly profil of temperature and salinity. These profiles and the meteorological recordings were staggered by 30 minutes for operational reasons.

No fixed point velocity measurements within the surface layer were conducted as no instrumentation with the required resolution was available.

4.1 WATER TEMPERATURE PROFILES

Plate 4.1 is a photograph of the probe used for most of the fieldwork. The thermistor is located at the bottom of the probe stem where it is well exposed but sheltered from solar radiation. On the raft, the probe cable was threaded over the pulley on the hinged wooden arm (shown in Plate 3.4, No. 2) thus keeping the measurements free from raft interference. Depth of the probe was measured by matching cable markings to a base mark on the arm.



PLATE 4.1 Conductivity/temperature profiling probe

The circuitry for the thermistor was as for other thermistors; a stable linearised Wheatstone Bridge. The bridge output was fed directly to a DVM. A fast response thermistor was chosen (τ < one second) to allow rapid profiles to be taken. This introduced the problem of correctly reading the DVM when the probe was not held perfectly still in a region of marked temperature gradient (the readings became quite variable). Electrical or thermal filtering was not a satisfactory solution in view of the requirement to complete profiles rapidly. In retrospect, the ideal measurement system would be one which integrates the signal over a specified period (1-10 seconds say).

Calibration of the thermistor circuit was performed prior to field trips in a laboratory controlled temperature bath. Prior to each field day a multiple-point calibration was again performed and this provided the operating expressions for the field day. Prior to each profiling drop, the temperature of a bucket of surface water was measured by the thermistor and a thermometer. These values were recorded for subsequent analysis and can be seen in the processing output (Appendix A3).

The limit of absolute accuracy of thermistor measurements must be taken as 0.1° C, corresponding to the smallest graduation on the thermometers used. Calibration expressions were determined to this accuracy and normally appear as a combination of two linear expressions spanning the temperature range of interest. The bucket checks indicate that, apart from obvious reading errors, 0.1° C absolute accuracy was usually obtained.

Relative accuracy of measurements within a profile would be as high as 0.01° C if calibration drift was the only

consideration. However, the uncertainty introduced by the temperature fluctuations described above degrades this relative accuracy where strong temperature gradients exist.

The data collection procedure will be described in Section 4.3.

4.2 WATER SALINITY PROFILES

Salinity was determined from a measure of water conductivity as described below. The conductivity cell, being the core of a Philips PW 9510 cell is shown in Plate 4.1. It consists of two platinum coated plates separated by about 0.7 cm with electrical connections to each. The cell is orientated at an angle away from the probe stem to ensure adequate flushing as the probe is lowered. The probe assembly was designed to cause minimal disturbance at the point of measurement while being lowered.

Conductivity was measured by one of two meters manufactured locally by Automated Laboratory Equipment. One such meter is shown in Plate 3.2 (No. 5). It applies an AC potential across the cell and measures the resulting conductivity in µmhos/cm. To improve measurement precision during the fieldwork, the meter's analog output was also measured by the DVM.

Early experience with the meters highlighted the need for great care in order to obtain meaningful results. Measurements tended to drift over a short period and temperature compensation built into the meter circuit proved to be quite inadequate. Described below are the calibration procedures adopted in order to obtain reasonably accurate salinity data.

Standard solutions of reagent grade NaCl in distilled

and de-ionized water were prepared, covering the concentration range 200 - 700 ppm. These solutions were immersed in a controlled temperature bath which was cycled over a wide range of expected water temperatures, with solution conductivity being measured at specific stable temperatures. The results were then plotted as shown in Figure 4.1 for Meter 2. From the individual lines, the slopes were determined which in turn specified the temperature coefficients

$$\alpha = \left(\frac{\text{slope x 100}}{C_{25}}\right) \ \%/^{\circ}C$$

 C_{25} is the conductivity at $25^{\circ}C$, the reference temperature for conductivity measurement. Values of α so determined are printed against the plots. These values of α were then plotted as a function of salinity. Two such plots are shown in Figures 4.2. The plot for Meter 2 shows the desirable result; α is practically independent of salinity. The plot for Meter 1 shows α strongly dependent on salinity, for reasons unknown. Fortunately, Meter 2 was used for all but the January fieldwork.

With a value of α determined from Figure 4.2, conductivity may be corrected to a 25^oC equivalent by

$$C_{25} = \frac{C}{(1 - \alpha \frac{T}{100})}$$
(4.1)

Conductivity is also a linear function of salinity. From Figure 4.1 we may obtain values of C₂₅ for each solution, giving the required relation. Due to the tendency of the meters to drift however, a two point calibration (conductivity and temperature for two solutions) was performed on the raft immediately prior to each profile. This information is tabulated in the processing output (Appendix A3).



FIGURE 4.1 Conductivity vs temperature for Meter 2 for various salinities



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4.3 DATA ACQUISITION AND PROCESSING

4.3.1 Profile Data Collection and Storage

The hourly profiling procedure consisted of lowering and holding the probe at pre-determined depths, then reading, from the DVM, the values of conductivity and thermistor output. These values were entered manually on a coded sheet and subsequently transferred to a computer together with the meteorological data.

To obtain the required resolution in regions of possible strong gradients, the depth increments were chosen as follows; 0.2 m for the first metre, 0.5 m from one to five metres and one metre increments thereafter, stopping at some depth within the seasonal thermocline.

4.3.2 Data Reduction

When processing the temperature profile data, the calibration expressions were not modified to reflect bucket calibrations, in view of the generally good agreement.

To process conductivity data, a new calibration expression was determined from the two-point salinity/conductivity calibration for each profile. These expressions appear in the processing output (Appendix A3). The temperature coefficient α was taken as 2% for Meter 2 and 1.7% for Meter 1. The latter value was chosen from Figure 4.2 for an average value of surface layer salinity (450 ppm).

The resultant processed profiles are presented as printouts in Appendix A4 and computer plots of temperature in Appendix A5. Several profiles appear in each plot to highlight the diurnal cycle. Note that the last profile on one plot appears as the first on the next plot to aid comparison.

At the commencement of this Project, it was intended to observe the surface salinity profile carefully in order to relate residual salt measurements to evaporation. Inspection of Appendices A3 and A4 reveals however that lack of measurement accuracy and resolution precludes any meaningful analysis. The task was simply beyond the capability of the conductivity meter and calibration system. As there is no structure of interest in the surface salinity profiles they have not been plotted.

4.4 RESERVOIR SURFACE LAYER BEHAVIOUR

4.4.1 A Qualitative Examination

From a perusal of the temperature plots of Appendix A5 and of the profile listings of Appendix A4 (which contain information for depths below 12 metres) it is possible to gain an understanding of the structure of the reservoir surface during summer. The essential features of the structure have been included in the schematic in Figure 4.3. Close to the surface, the temperature structure varies on a diurnal timescale whereas the temperature and salinity structure below a depth of several metres is stable, varying only on a seasonal timescale.

A qualitative examination of the plots of Appendix A5 and the meteorological fluxes (Figure 3.5) reveals the following typical summer daily pattern. In the early morning there is a deep homogenous surface layer, sometimes as deep as the seasonal well mixed layer itself. Solar heating in light wind conditions (with small evaporative and sensible heat losses) results in the cessation of mixing throughout most of this layer by mid-morning. At this



stage there is not enough mixing energy available from wind stirring or surface convection to overcome the stable buoyancy gradient induced by solar heating. Continued solar heating results in the formation of a temperature profile, the form of which is determined by the solar attenuation profile eq. 3.1. The diurnal well mixed layer may have practically disappeared. The picture changes in the afternoon if the wind strength increases (see Appendix A5.2) Wind stirring, surface convective overturn due to evaporative cooling, and internal shear instability now override the decreasing solar input and so the diurnal well mixed layer deepens for the remainder of the day. If stirring and/or cooling are strong enough (e.g. a storm or cold night) mixing may proceed to the base of the seasonal well mixed layer, following which, erosion of the seasonal thermocline will commence. This was observed in the April field day (050476) (see Appendix A5.10).

It is quite evident that the seasonal temperature structure represents the cumulative effect of the diurnal heating and mixing cycles over many successive days. In early summer, intensifying solar radiation heats the upper waters, forming a stable density structure which resists mixing. When significant mixing does occur, it penetrates only to a medium depth and serves only to sharpen the temperature gradient at that depth. Over time, this leads to the formation of the seasonal thermocline, which in mid-summer may be quite thick (e.g. three metres) and very strong (e.g. 5°C). Evening convective mixing becomes stronger in autumn, causing the diurnal well mixed layer to deepen to the full seasonal well mixed layer depth and then encroach on the seasonal thermocline which is consequently sharpened. The seasonal

structure is destroyed completely by mid-winter.

4.4.2 Significance of the Reservoir Temperature Structure

The temperature structure of a reservoir, as determined by its diurnal and seasonal cycles, is important for a number of reasons. These are discussed below.

Biological production (phytoplankton and zooplankton) is dependent on the concentration of nutrients and on light intensity. Under favourable conditions, blooms may occur over periods as short as a few hours. Such conditions occur near the surface on hot, still days where the diurnal well mixed layer is very shallow and hence downward mixing of the biological constituents is limited. An investigation of these biological processes in a reservoir necessitates a sound understanding of the diurnal cycle.

The seasonal thermocline acts as a strong barrier to mixing, impeding the movement of water and its dissolved constituents between the epilimnion and hypolimnion. Dissolved oxygen, which is replenished at the surface, may become depleted in the hypolimnion due to bacterial action, with a subsequent degeneration of water quality. In the Wellington Reservoir it is also observed that cold, high salinity inflows remain in the hypolimnion, being prevented from mixing upward by the seasonal thermocline. A similar phenomenon is found in the atmosphere where pollutants may be trapped in a neutral layer beneath a temperature inversion.

Reservoir flows which occur within a temperature stratified region are modified by the effects of buoyancy. Imberger et al.(1979) summarize the theory which describes selective withdrawal and inflow of water in the stratified waters within or below the seasonal thermocline.

In order to manage the quality of water in a reservoir where the above effects are present, it is necessary to be able to predict the behaviour of the temperature and salinity structure on both daily and seasonal timescales. With the data presented in Chapters 3 and 4, an analysis of the diurnal cycle is possible. During any one of the field days the seasonal thermocline may be considered to be stationary. All the mechanisms which act together to form the seasonal thermocline and well mixed layer are present and active in the diurnal cycle. It is therefore proposed to develop, in the following chapters, a model of the diurnal cycle, the predictions of which will be compared against the observed profiles. If validated for the diurnal case, the model may then be used for seasonal predictions where averaged meteorological data are used.

CHAPTER 5

THEORY OF MIXED LAYER ENERGETICS

In recent years, well mixed layers have been modelled by two distinctly different methods. Mellor and Durbin (1975) and others have obtained solutions to the fundamental equations based upon simplifications of second order closure schemes. The main body of work, however, has concentrated on the development of models in which the vertical distributions of temperature, velocity and other constituents are specified. As Niiler and Kraus (1977) point out, the simplicity and physical insight afforded by this integral approach is adequate justification for pursuing it.

In the following sections a general well mixed layer model is developed. Firstly, in Section 5.1, a set of equations describing the energetics of a well mixed layer are derived. In Section 5.2, existing models and specifically the assumptions employed by those models are surveyed. Finally, in Section 5.3, a complete description of selected parameterization schemes with an evaluation of the various coefficients is presented. This section also deals with problems specific to a medium sized reservoir.

5.1 WELL MIXED LAYER INTEGRAL RELATIONS

Figure 5.1 shows schematically a well mixed layer in a body of water. The various parameters shown are

τ surface wind stress



FIGURE 5.1 Features of a well mixed laver in a water

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^н s	surface sensible heat flux
H _L	latent heat loss
W	evaporation rate
Q_{L}	net long-wave radiation
Q _S	net short-wave radiation
q(z)	short-wave penetration profile
тs	well mixed layer temperature
ss.	well mixed layer salinity
U _S	well mixed layer velocity
ΔT	thermocline temperature jump
۵S	thermocline salinity jump
ΔU	thermocline velocity jump
h	well mixed layer depth
δ	thermocline thickness
	In terms of previously defined parameters,
i)	$Q_{L} = Q_{LR} - Q_{LAC}$
ii)	$Q_{S} = \{-(1-R)Q_{s}\}$ from eq. 3.2

iii)
$$W = \frac{E}{1000}$$
 (with units of m s⁻¹)

In Figure 5.1, two possible co-ordinate systems are shown. All fluxes are positive upward. Hereafter, the name well mixed layer will be abbreviated to WML.

Assumptions implicit in the formulation of WML models are:

- The WML is uniformly mixed with constituent profiles as shown in Figure 5.1, and moves as a slab.
- Horizontal advection of temperature or salinity differences may be ignored; hence the model is one-dimensional.

-

It is not strictly necessary to specify uniform profiles of temperature, salinity and velocity in order to use the integral approach described below. Instead it is necessary that, at every level within the WML, the appropriate temperature, salinity and velocity scales are the layer averages of each variable, so that the integral method will correctly describe the various physical mechanisms involved in WML formation.

To obtain a solution giving the WML temperature, salinity, velocity and depth over time, the one-dimensional equations for heat, mass, salt, momentum and turbulent kinetic energy must be solved throughout the layer. With the assumed structure of Figure 5.1 it is possible to integrate these equations over the full depth ($0 \le z \le H$) and so include the integrated influence of all the relevant terms. The origin (z = 0) may be at the reservoir bed, or at some level in the water below which no surface effects penetrate.

The following procedure is employed in the evaluation of integrals. The integral of a parameter f(z,t) over $(0 \le z \le H)$ may be separately evaluated for three regions; the epilimnion $(\xi \le z \le H)$, the thermocline $(\xi - \delta \le z \le \xi)$ and the hypolimnion $(0 \le z \le \xi - \delta)$, giving three integrals

$$\int_{0}^{H} f dz = \int_{0}^{\xi - \delta} f dz + \int_{\xi - \delta}^{\xi} f dz + \int_{\xi}^{H} f dz$$

If f(z,t) is itself a time derivative and the limits of integration. ξ and $\xi-\delta$, also vary with time, then the integration must obey Leibnitz's Rule.

5.1.1 Heat

The one-dimensional equation of heat may be written as $\frac{\partial T}{\partial t} = -\frac{\partial}{\partial z} \frac{\partial}{\partial t'w'} - \frac{1}{\rho_0 C_p} \frac{\partial q(z)}{\partial z}.$ (5.1)

where ρ_{0} is a reference water density.

As an example of the integration procedure described above, the three integrals are evaluated below, term by term. (A) Hypolimnion $(0 \rightarrow \xi - \delta)$

$$\int_{0}^{\xi-\delta} \frac{\partial T}{\partial t} dz = \frac{\partial}{\partial t} \int_{0}^{\xi-\delta} T dz - T(\xi-\delta) \frac{d(\xi-\delta)}{dt}$$
$$\int_{0}^{\xi-\delta} \frac{\partial}{\partial z} \overline{\theta'w'} dz = \overline{\theta'w'}(0) - \overline{\theta'w'}(\xi-\delta)$$
$$\int_{0}^{\xi-\delta} -\frac{1}{\rho_{0}C_{p}} \frac{dq}{dz} dz = -\frac{1}{\rho_{0}C_{p}} \left[q(\xi-\delta) - q(0)\right]$$

The heat balance is therefore

$$\frac{\partial}{\partial t} \int_{0}^{\xi-\delta} T \, dz = T(\xi-\delta) \frac{d(\xi-\delta)}{dt} + \overline{\theta'w'}(0) - \overline{\theta'w'}(\xi-\delta) - \frac{1}{\rho_{0}C_{p}} \left[q(\xi-\delta) - q(0)\right]$$
(5.2)

The first right hand side (RHS) term represents the loss of heat in that fluid being entrained from the hypolimnion into the epilimnion. The other RHS terms are flux boundary conditions.

(B) Thermocline $(\xi - \delta \rightarrow \xi)$

$$\int_{\xi-\delta}^{\xi} \frac{\partial T}{\partial t} dz = \frac{\partial}{\partial t} \int_{\xi-\delta}^{\xi} T dz - T(\xi) \frac{d\xi}{dt} + T(\xi-\delta) \frac{d(\xi-\delta)}{dt}$$
(1) (2) (3)

For the purposes of the model, use is made of the observation that the thermocline is often very thin (i.e. δ and $\frac{d\delta}{dt} \rightarrow 0$). So, (1) vanishes and (2) and (3) together reduce to

-
$$\Delta T \frac{d\xi}{dt}$$
, where $\Delta T = T(\xi) - T(\xi-\delta)$

next,
$$\int_{\xi-\delta}^{\xi} - \frac{\partial}{\partial z} \overline{\theta' w'} dz = \overline{\theta' w'} (\xi-\delta) - \overline{\theta' w'} (\xi)$$

and
$$\int_{\xi-\delta}^{\xi} -\frac{1}{\rho_{o}C_{p}} \frac{\partial q}{\partial z} dz = -\frac{1}{\rho_{o}C_{p}} \left[q(\xi) - q(\xi-\delta)\right]$$

For the type of profile q(z) shown in Figure 5.1,

$$[q(\xi) - q(\xi - \delta)] \rightarrow 0 \text{ as } \delta \rightarrow 0 \text{ , so}$$

$$\overline{\theta'w'}(\xi) - \overline{\theta'w'}(\xi - \delta) = \Delta T \frac{d\xi}{dt}$$
(5.3)

This is often called the heat flux jump condition across the thermocline.

(C) Epilimnion $(\xi \rightarrow h)$

$$\int_{\xi}^{H} \frac{\partial T}{\partial t} dz = \frac{\partial}{\partial t} \int_{\xi}^{H} T dz - T(H) \frac{dH}{dt} + T(\xi) \frac{d\xi}{dt}$$
(1) (2) (3)

Now T = T(H) = T(ξ) = T_S in the epilimnion so (1) becomes

$$\frac{\mathrm{d}}{\mathrm{d}t} (\mathrm{T}_{\mathrm{S}}\mathrm{H} - \mathrm{T}_{\mathrm{S}}\xi),$$

Expanding via the chain rule and adding (2) and (3) gives

h
$$\frac{dT_S}{dt}$$
, where h = H - ξ .
next, $\int_{\xi}^{H} - \frac{\partial}{\partial z} \overline{\theta' w'} dz = \overline{\theta' w'}(\xi) - \overline{\theta' w'}(H)$
and $\int_{\xi}^{H} - \frac{1}{\rho_o C_p} \frac{dq}{dz} = -\frac{1}{\rho_o C_p} [q(H) - q(\xi)]$

Combining the terms gives

$$h \frac{dT_{S}}{dt} = \overline{\theta' w'}(\xi) - \overline{\theta' w'}(H) - \frac{1}{\rho_{o}C_{p}} [q(H) - q(\xi)]$$
(5.4)

Eq. 5.3 and eq. 5.4 together describe the heat balance of the WML. Eq. 5.2, included for completeness, is not explicitly required in a WML model, although a solution to eq. 5.1 below the thermocline is required in order to evaluate ΔT over time.

5.1.2 <u>Momentum</u>

The form of the momentum equation for horizontal plane flow follows from eq. 2.1:

$$\frac{\partial U}{\partial t} = -f\hat{k} \times U - \frac{\partial}{\partial z} \overline{u'w'} - \frac{1}{\rho_0} \nabla p$$
(5.5)

2L
$$\Omega \sin \phi < \sqrt{\frac{\Delta \rho}{\rho_1} g \frac{h_1 h_2}{H}}$$

with Ω

earth's angular velocity,

h₁ & h₂ thickness of top and bottom layers,

H total depth,

 $\Delta \rho$ density jump $(\rho_2 - \rho_1)$,

L basin length.

This criterion is marginally satisfied in the Wellington Reservoir, that is, the reservoir is small enough for rotational effects to be unimportant. The first RHS term will therefore be neglected and only the horizontal velocity u = U + u' in the direction of the flow will be considered.

Eq. 5.5 may be integrated as follows:

(a) Thermocline $(\xi - \delta \rightarrow \xi)$

 $\overline{u'w'}(\xi) - \overline{u'w'}(\xi - \delta) = \Delta U \frac{d\xi}{dt}$ (5.6)

If flows beneath the thermocline are neglected, then the velocity difference across the thermocline $\Delta U = \Delta U_{\rm S} = U_{\rm S}$. The term $\overline{u'w'}(\xi-\delta)$ represents loss of momentum from the WML into the stable hypolimmion, the major mechanism being radiation of internal waves which will be discussed in the next section.

(B) Epilimnion
$$(\xi \rightarrow H)$$

$$h \frac{dU}{dt} = \overline{u'w'}(\xi) - \overline{u'w'}(H) - PGRAD$$
(5.7)

Discussion on the possible effects of horizontal pressure gradients in a finite length reservoir will be deferred until Section 5.3 5.1.3 Mass

A one-dimensional mass conservation equation for the configuration of Figure 5.1 is

$$\frac{\partial \rho}{\partial t} = -\frac{\partial}{\partial z} \overline{\rho' w'} + \frac{\alpha}{C_p} \frac{\partial q(z)}{\partial z}$$
(5.8)

where α is the thermal expansion coefficient of water. The last term represent density variations induced by internal absorption of heat from solar short-wave radiation (note that q(z) is negative downward).

For the sake of rigour it is necessary to consider the total depth ($0 \le z \le H$) plus an infinitesimal conductive sublayer ($H < z \le H+d$) through which heat and mass transfers occur by molecular processes; it is not stated a priori that turbulent fluxes are continuous across the interface.

Integrating eq. 5.8 over (0 \leq z \leq H) and neglecting q(0) gives

$$\frac{\partial}{\partial t} \int_{0}^{H} \rho \, dz = \rho(H) \, \frac{dH}{dt} - \overline{\rho' w'}(H) + \frac{\alpha}{C_{p}} q(H)$$

The LHS is the rate of change of total mass of a column which, intuitively, is due only to evaporation or precipitation. In the case of evaporation, fresh water is removed leaving a salt residue so that

$$\frac{\partial}{\partial t} \int_{0}^{H} \rho \, dz = -\rho(H) W (1 - \beta S_{S})$$

where $\boldsymbol{\beta}$ is the mass coefficient for salt.

The quantity dH/dt may be independently evaluated. It is the vertical expansion or contraction of the column due to net heating or cooling, minus evaporation, so that

$$\frac{dH}{dt} = -\frac{\alpha H}{\rho(H)C_{p}} - W$$
(5.9)

with H sum of all atmospheric turbulent and radiative heat transfers at the surface.

As before, bottom transfers (z = 0) are neglected.

Combining the foregoing equations gives

$$\overline{\rho'w'}(H) = -\rho(H) \left[\frac{\alpha(H-q(H))}{\rho(H)C_p} + W\beta S_S \right]$$

or, expressed in terms of heat and salt components, and density $\boldsymbol{\rho}_{o},$

$$-\alpha g \overline{\theta' w'}(H) = -\frac{\alpha g}{\rho_{o} C_{p}} (H - q(H))$$
(5.10)

$$\beta g \overline{s'w'}(H) = -\beta g WS_{S}$$
(5.11)

These are the jump conditions for heat and salt flux at the surface.

The derivation above shows that $\overline{\rho'w'}$ is not constant and continuous across the interface, but is determined, below the conductive sublayer, by the rate at which the mass of the column is falling (rising) due to thermal contraction (expansion), with an extra contribution from salt residue. The work of some previous authors, who use surface based co-ordinates, is misleading as they are obliged to consider that $\overline{\rho'w'}$ is continuous across the air-water interface.

5.1.4 Salt

Conservation of salt or any other tracer in the fluid can be written as

$$\frac{\partial S}{\partial t} = -\frac{\partial}{\partial z} \overline{s'w'}$$
(5.12)

with s' salinity fluctuation. No sources or sinks are considered.

Integrating across the WML gives:

(A) Thermocline $(\xi - \delta \rightarrow \xi)$

$$\overline{s'w'}(\xi) - \overline{s'w'}(\xi - \delta) = \Delta S \frac{d\xi}{dt}$$
(5.13)

(B) Epilimnion $(\xi \rightarrow H)$

$$h \frac{dS_{S}}{dt} = \overline{s'w'}(\xi) - \overline{s'w'}(H)$$
(5.14)

5.1.5 <u>Turbulent Kinetic Energy</u>

Following Denman (1973), the equation for turbulent kinetic energy (hereafter TKE) may be written as

$$\frac{1}{2} \frac{\partial \overline{E}}{\partial t} = - \overline{u'w'} \frac{\partial U}{\partial z} - \frac{\partial}{\partial z} \left[\overline{w' \left(\frac{p'}{\rho_o} + \frac{E}{2} \right)} \right] - \frac{g}{\rho_o} \overline{\rho'w'} - \varepsilon$$
(5.15)
(1) (2) (3) (4) (5)

The various numbered term are defined below:

- (1) time rate of change of TKE, $\frac{1}{2}\overline{E}$ in the WML, where $\overline{E} = (\overline{u'^2 + v'^2 + w'^2}),$
- (2) production of TKE due to the working of the Reynolds stress (-u'w') on the mean shear,
- (3) divergence of the vertical flux of TKE induced by pressure (p and velocity fluctuations at the upper and lower boundaries,
- (4) TKE expended in working against buoyancy forces

$$\left(\frac{g}{\rho_{o}} \overline{\rho' w'} = - \alpha g \overline{\theta' w'} + \beta g \overline{s' w'}\right)$$

(5) rate of destruction of TKE by viscous dissipation.

Eq. 5.15 is also integrated across the WML as follows (A) Thermocline $(\xi - \delta \rightarrow \xi)$

$$\int_{\xi-\delta}^{\xi} \frac{1}{2} \frac{\partial \overline{E}}{\partial t} dz = \frac{\partial}{\partial t} \int_{\xi-\delta}^{\xi} \frac{\overline{E}}{2} dz - \frac{1}{2} \overline{E}(\xi) \frac{d\xi}{dt} + \frac{1}{2} \overline{E}(\xi-\delta) \frac{d(\xi-\delta)}{dt}$$
(1)
(2)
(3)

Denman (1973) found that m = 1 gave the best results for his model which essentially follows Kraus and Turner's (1967) formulation. Larger values for m are deduced from analysis of storm deepening events, however the influence of shear deepening may invalidate these.

- (b) Ball (1960) proposed that n = 1, arguing that large convective eddies would be little affected by dissipation. Other workers have provided estimates in the range $0 \le n < 0.113$.
- (c) The shear energy conversion factor s, accounting for dissipation and, to some extent, leakage via internal waves, has received little attention from researchers. A tentative estimate is s = 0.7.

5.2.5 Sherman Imberger & Corcos (1978), Fischer et al. (1979)

These authors have presented a generalised entrainment relation which includes all the various mechanisms proposed by KT, PRT, and ZT. Although there are some differences in approach to the problem, their results will be seen to be a special case of the analysis to follow; for this reason a separate description is not presented here. other two, because $|dH/dt| << |d\xi/dt|$ or |dh/dt| and $\overline{E}(H) < E_{S}$ (from Willis and Deardorff (1974)).

Expanding the first term by the chain rule gives

$$\int_{\xi}^{H} \frac{1}{2} \frac{\partial \overline{E}}{\partial t} dz = \frac{1}{2} h \frac{dE_{S}}{dt} - \frac{E_{S} d\xi}{2 dt} + \frac{1}{2} \overline{E}(\xi) \frac{d\xi}{dt}$$

The next integrated term is

$$\int_{\xi}^{H} \alpha \overline{g\theta'w'} dz = \frac{\alpha gh}{2} \overline{\theta'w'}(\xi) + \frac{\alpha gh}{2\rho_{0}C_{p}} \widetilde{H}_{*}$$
where $\widetilde{H}_{*} = \left[\rho_{0}C_{p}\overline{\theta'w'}(H) + q(H) + q(\xi) - \frac{2}{h}\int_{\xi}^{H} q(z) dz\right]$

The first RHS term, after substitution of eq. 5.3, is seen to be the increase of column potential energy due to entrainment of heavier fluid through the thermocline. The second RHS term is the change of column potential energy due to the surface heat flux term \tilde{H}_{\star} . The form of \tilde{H}_{\star} indicates the dependence of potential energy on the distribution of heating and cooling within the layer in particular, the form of q(z) must be accurately specified.

The remaining integrated terms are

$$\int_{\xi}^{H} - \beta g \overline{s'w'} dz = -\frac{\beta g h}{2} \left(\overline{s'w'}(\xi) + \overline{s'w'}(H) \right)$$
$$\int_{\xi}^{H} - \frac{\partial}{\partial z} \left[\overline{w'} \left(\frac{p'}{\rho_{o}} + \frac{E}{2} \right) \right] dz = - \left[\overline{w'} \left(\frac{p'}{\rho_{o}} + \frac{E}{2} \right) \right]_{\xi}^{H}$$
$$= K(\xi) - K(H) \text{ for simplicity.}$$
$$\int_{\xi}^{H} - \overline{u'w'} \frac{\partial U}{\partial z} dz = SH(H) \text{ for simplicity.}$$

A vertically averaged WML dissipation rate may be defined as $\epsilon_{\rm S}$ = 1/h $\int^{\rm H}_{\xi}$ ϵ dz.

Then

$$\int_{\xi}^{H} - \varepsilon \, dz = -\varepsilon_{S}h$$

The terms from the thermocline and epilimnion TKE balances may be added to give a total WML balance:

$$\frac{h}{2} \frac{dE_{S}}{dt} = \frac{E_{S}}{2} \frac{d\xi}{dt} + SH(\xi) + SH(H) + K(\xi - \delta) - K(H)$$
(1a) (1b) (2a) (2b) (3a) (3b)
$$+ \frac{\alpha gh}{2} \left[\overline{\theta'w'}(\xi) + \frac{\tilde{H}_{*}}{\rho_{o}C_{p}}\right] - \frac{\beta gh}{2} \left[\overline{s'w'}(\xi) + \overline{s'w'}(H)\right] - \varepsilon_{S}h$$
(4a) (4b) (4c) (4d) (5) (5.17)

Numbering of terms conforms to that of eq. 5.14. Eqs. 5.3, 5.4, 5.6, 5.7, 5.10, 5.11, 5.13, 5.14 and 5.17 form the equation set which must be solved in order to describe the behaviour of the WML.

5.2 REVIEW OF EXISTING MODELS.

The above set of equations are intractable as they stand. In order to solve them it is necessary to make a number of simplifications and to parameterize some of the turbulent flux quantities in terms of mean flow quantities. In this section a review of models proposed by other authors is presented. Attention is drawn to the mixing/deepening mechanisms included or neglected and the closure hypotheses employed.

5.2.1 <u>Kraus and Turner (1967)</u> (KT)

These authors consider the following mechanisms from eq. 5.17:

hanical energy input at the surface from wind

stirring, (terms 2b, 3b),

ii) potential energy change by entrainment plus surfaceheating or cooling (terms 4a, 4b).

KT also note the possible importance of dissipation but do not attempt to include a parameterization of this term. The proposed balance is therefore

SH(H) - K(H) +
$$\frac{\alpha g h}{2} \left[\theta' w' (\xi) + \frac{\tilde{H}}{\rho_o C_p} \right] = 0$$

Without reference to the specific forms of SH(H) and K(H) they propose that the wind working rate must be proportional to the stress times a water velocity scale,

SH(H) - K(H)
$$\propto \tau u_{*} = \rho_{a} u_{*a}^{3} \sqrt{\rho_{a}/\rho}$$

u, is the water friction velocity and subscript a refers to air.

5.2.2 Pollard, Rhines and Thompson (1973) (PRT)

Errors exist in the formulation of these authors' model, as pointed out by Niiler (1975). For this reason their derivation will not be discussed here. However, the model they propose can be shown to represent a balance of the following terms:

- shear production of TKE in the entrainment zone (term 2a),
- ii) potential energy increase associated with entrainment (term 4a).

i.e.
$$SH(\xi) + \frac{\alpha gh}{2} \overline{\theta' w'}(\xi) = 0$$

If, as shown in Section 5.3.1,

$$SH(\xi) = \frac{C_S}{2} \Delta U_S^2 \frac{d\xi}{dt} ,$$

the above balance after substitution of eq. 5.3 becomes

$$\alpha gh \frac{\Delta T}{\Delta U_S^2} = C_S$$
(5.18)

which is these authors' Richardson No. criterion for marginal stability, with $C_S = 1$. The WML velocity ΔU_S is computed from the momentum equation 5.7. This model therefore predicts that, following the onset of wind, the layer depth will adjust to maintain the balance of eq. 5.18, so that

$$h = \frac{C_{\rm S} \Delta U_{\rm S}^2}{\alpha g \Delta T}$$
(5.19)

5.2.3 <u>Tennekes (1973)</u>, Zeman and Tennekes (1977) (ZT)

The original work of Tennekes (1973) was corrected and expanded by Zeman and Tennekes (1977); most of the following summary refers to this latter work.

These authors attempt to solve the TKE eq. 5.15 locally at the inversion base rather than integrating eq. 5.15 and the other equations as has been done in Section 5.1. Unlike the integral formulations where terms are formally derived, their approach has necessitated a number of hypotheses and parameterizations of surface to inversion base transfers.

The flux convergence is parameterized in terms of σ_w , the average standard derivation of vertical velocity fluctuations:

$$\frac{\partial}{\partial z} \left[\overline{w' \left(\frac{p'}{\rho} + \frac{E}{2} \right)} \right] = -C_F' \frac{\sigma_w^3}{h}$$
(5.20)

Implicit in this is the tendency of the turbulence towards isotropy so that at all times $\mathbf{\tilde{E}} \propto \sigma_w^2$ (recall $\mathbf{\tilde{E}} = \sigma_u^2 + \sigma_v^2 + \sigma_w^2$) where $\sigma_u^2 = \mathbf{\tilde{u}'}^2$, $\sigma_v^2 = \mathbf{\tilde{v}'}^2$, $\sigma_w^2 = \mathbf{\tilde{w}'}^2$). It is assumed that energy is re-partitioned between the three components as fast as it is consumed through σ_w^2 by work against buoyancy.

Tennekes (1973) proposes a balance between flux convergence and entrainment potential energy at the inversion base:

$$\frac{g}{\rho} \left(\overline{\theta' w'}\right)_{i} + C_{F}' \frac{\sigma_{w}^{3}}{h} = 0$$
(5.2)

Following Deardorff (1970), ZT set σ_{w} proportional to the convective velocity scale

$$w_{\star} = \left(\frac{g}{T_{o}} \left(\overline{\theta' w'}\right)_{o} h\right)^{1/3} , \qquad (5.2)$$

consistent with their initial assumption that the turbulence is always in equilibrium with boundary conditions (surface fluxes). Substitution of eq. 5.22 into eq. 5.21 gives

$$(\overline{\theta'w'})_{i} / (\overline{\theta'w'})_{0} = C_{F}'$$
(5.2)

This relation holds in steady-state convective conditions.

They derive a temporal term

$$\frac{1}{2} \frac{\partial E}{\partial t} = C_{\rm T} \frac{\sigma_{\rm w}^2}{h} \frac{dh}{dt}$$
(5.2)

by appealing to an independent argument. No such argument is required if the TKE equation is integrated with the use of Leibniz Rule at the inversion boundary (see eq. 5.17(1b)). For boundary layer growth in a neutral atmosphere they derive the relation

$$C_{\rm F}'/C_{\rm T} = 0.3u_{\star}/\sigma_{\rm W}$$
 (5.25)

ZT attribute some (or for large Δ T, all) of the TKE flux convergence at the inversion to dissipation, identifying

internal wave radiation as the energy sink. From the integration of the TKE equation it is evident that the term $K(\xi-\delta)$ (eq. 5.17 (3a)) accounts for this sink. ZT attempt to parameterize their dissipation term but with limited success.

For the case where surface wind working is important, σ_{W} must be a function of both w_{\star} and u_{\star} .ZT hypothesise a linear combination of convective and mechanical contributions:

i.e.
$$(\sigma_w^2)_i \propto w_*^2 + \eta^2 u_*^2$$

This hypothesis breaks down if w_* goes negative (e.g. solar heating of a reservoir) as the above relation still predicts a positive contribution of TKE from w_*^2 . The correct hypothesis should specify that the flux of TKE be determined by some combination of the power per unit area available from surface wind stirring and cooling, as proposed by Sherman, Imberger and Corcos (1978):

$$(\sigma_{w}^{3})_{i} \propto w_{*}^{3} + \eta^{3}u_{*}^{3}$$
 (5.26)

Although ZT parameterize σ_{W} incorrectly, the coefficients of interest here are determined correctly. Analysis of laboratory data by ZT yields

$$C_{\rm F}' = 0.5$$
 $C_{\rm T} = 3.55$
 $\eta = 2.15$

netic)

ZT include a mechanical production term due to shear at the inversion base but the argument involves their concept of inversion base dissipation and so will not be considered here.

5.2.4 <u>Niiler (1975), Niiler and Kraus (1977)</u> (NK)

The reader is referred to the latter of these papers for a good up-to-date discussion of well mixed layer modelling.

NK employ integrated forms of the WML equations

but use a surface based co-ordinate system which complicates the derivation of terms like the surface buoyancy flux $g/\rho_0 \ \overline{\rho'w'}(H)$ and the entrained fluid agitation term $1/2 E_c d\xi/dt$.

Important parameterization schemes introduced by NK are summarised below:

i) the Reynolds stress at the thermocline base, $\overline{u'w'}(\xi-\delta)$ is given the form $\overline{u'w'}(\xi-\delta) = -C \Delta U_S^2$ (5.27)

where C is a drag coefficient. The term accounts for momentum loss via internal wave radiation and acts against the build up of layer mean velocity. However, due to lack of information, no value of C is given; it is expected to be a function of hypolimnion stratification.

- ii) They omit the leakage flux of TKE, $K(\xi-\delta)$, representing (in the main) the work of pressure fluctuations in the formation of internal waves in the hypolimnion.
- iii) K(H), the surface flux of TKE, is taken as proportional to wind working in the atmospheric surface layer, that is, a stress times a wind velocity, so

- K(H) ∝ u_{*a}³

or in terms of the water friction velocity (where $u_* = \sqrt{\rho_a/\rho_o} u_*$ - K(H) = $m_1 u_*^3$, where m_1 is a constant. (5.28)

iv) SH(H), the production of TKE in the surface shear layer is also taken as proportional to wind working and therefore incorporated in eq. 5.28. Kraus and Turner's (1967) formulation (stress times a water velocity scale) amounts to the same result.

The result is derived as follows. SH(H) was defined in

Section 5.1 as

SH(H) =
$$\int_{\xi}^{H} - \overline{u'w'} \frac{\partial U}{\partial z} dz$$
.
Considering a thin surface shear layer superimposed over the mean flow, with applied surface stress $\tau = \rho_0 u_*^2$,

SH(H) =
$$u_{\star}^{2} \int_{\xi}^{\pi} \frac{\partial U}{\partial z} dz = u_{\star}^{2} [U(H) - U(\xi)]$$

The surface drift current U(H) - U(\xi) is known to be proportional to u_{\star_a} so

SH(H) ∝ u_{*}³

This may be incorporated in eq. 5.28

v) Using eq. 5.6 and their drag relation of eq. 5.27, NK evaluate the thermocline shear term

$$SH(\xi) = \lim_{\delta \to 0} \int_{\xi-\delta}^{\xi} -\frac{1}{u'w'} \frac{\partial U}{\partial z} dz = \frac{1}{2} \Delta U_{S}^{2} \frac{dh}{dt} - \frac{1}{3} C \Delta U_{S}^{3}$$
(5.29)

vi) NK indicate that dissipation is the most arbitrary link in the formulation. Dimensionally it is expected that $h\epsilon_{\rm S} \propto \sigma_{\rm w}^{-3}$ (5.30)

On intuitive grounds, they propose that dissipation acts to reduce the efficiency of individual TKE production mechanisms, and can therefore be accounted for by introducing efficiency coefficients or reducing the value of existing coefficients. With coefficients m, n and s, the net TKE production is

$$mu_{\star}^{3} + \frac{h}{4} \left[(1+n)B_{0}^{} - (1-n)|B_{0}^{} \right] + \frac{s}{2} \Delta U_{S}^{2} \frac{dh}{dt}$$
 (5.31)

In this Project, $B_0 \equiv \alpha g \tilde{H}_* / \rho_0 C_p - \beta g s' w'(H)$. The peculiar form of the second term ensures that if B_0 is -ve (strong solar heating) dissipation does not affect it.

Whilst this seems logical its application to a WML is questionable. Eq. 5.31 implies that, if wind stirring dominates over surface heating, only that part of wind stirring energy remaining, after depth integrated dissipation, is available to first overcome the heating potential energy deficit and then deepen the layer further. However, most of the work to increase the potential energy (to drive the negative buoyancy flux $\alpha g \overline{\theta' w'}$) is accomplished high in the layer. (For the simple case where solar penetration is absent, $\overline{\theta' w'}$ decreases linearly with depth in the well mixed model). It is reasonable to expect that the efficiency of wind working will be greater for this 'surface work', implying that m should be larger in this situation.

The internal wave radiation loss term 1/3 C ΔU_S^{3} from eq. 5.29 is deduced to be small and is included in the shear production efficiency s.

NK assume that steady-state conditions prevail, so $dE_S/dt = 0$. They further assume that the fluid agitation flux $1/2E_Sd\xi/dt$ is small compared to the entrainment working rate for most oceanic conditions and hence may be neglected. The applicability of these assumptions to the reservoir case will be discuss in the next section.

Determination of the coefficients m, n and s involves great uncertainty and is made difficult by a lack of experimental data. Limited evidence available indicates that the coefficients m and n are not constant, but are decreasing functions of the ration of the energy consuming and producing terms. Evidence offered by NK for the possible magnitude of these terms is as follows: (a) Laboratory experiments of Kato and Phillips (1969) gave m = 1

Denman (1973) found that m = 1 gave the best results for his model which essentially follows Kraus and Turner's (1967) formulation. Larger values for m are deduced from analysis of storm deepening events, however the influence of shear deepening may invalidate these.

- (b) Ball (1960) proposed that n = 1, arguing that large convective eddies would be little affected by dissipation. Other workers have provided estimates in the range 0 ≤ n < 0.113.</p>
- (c) The shear energy conversion factor s, accounting for dissipation and, to some extent, leakage via internal waves, has received little attention from researchers. A tentative estimate is s = 0.7.

5.2.5 Sherman Imberger & Corcos (1978), Fischer et al. (1979)

These authors have presented a generalised entrainment relation which includes all the various mechanisms proposed by KT, PRT, and ZT. Although there are some differences in approach to the problem, their results will be seen to be a special case of the analysis to follow; for this reason a separate description is not presented here.

5.3 SELECTED PARAMETERIZATION SCHEMES

Based on the work of other researchers summarised in the previous section, plus some new hypotheses, simplifications and parameterizations of terms necessary for closure of the WML equations are presented here.

5.3.1 Individual Mechanisms

Internal Wave Effects

Too little is understood about energy and momentum transfer via internal waves in the hypolimnion to explicitly include these terms. Like NK, it must be assumed here that energy losses are to some extent accounted for by a reduction in the efficiency of entrainment work.

Consequently, the following terms are neglected: $\overline{u'w'}(\xi-\delta)$ from eq. 5.6 and $K(\xi-\delta)$ from eq. 5.17.

Other Leakage Terms

Based on the reasonable assumption that all turbulent fluxes vanish at the thermocline base, the heat and salt fluxes

 $\overline{\theta' w'}(\xi - \delta)$ from eq. 5.3 and $\overline{s' w'}(\xi - \delta)$ from eq. 5.13. are set to zero.

Surface Wind Working

Following KT and NK, the surface TKE fluxes and the surface shear production are jointly parameterized as

$$SH(H) - K(H) = m_1 u_*^3$$
 (5.32)
Thermocline Shear

Niller (1975) obtained an expression for shear production of TKE at the thermocline:

$$SH(\xi) = \frac{1}{2} \Delta U_S^2 \frac{dh}{dt} = -\frac{1}{2} \Delta U_S^2 \frac{d\xi}{dt}$$
(5.33)

This indicates that the mean kinetic energy lost due to entrainment of quiescent fluid becomes available to work locally to further deepen the layer. However, it is expected that a significant portion of this energy will be fed into the well mixed layer (via the term $K(\xi)$) and there be dissipated. Hence it is necessary to include an efficiency coefficient C_g analogous to NK's s.

Surface Heat and Salt Buoyancy

ZT introduced the buoyancy velocity scale defined in eq. 5.22. Combining the surface heat and salt buoyancy terms (4b) and (4d) from eq. 5.17 gives a modified buoyancy velocity scale,

$$\frac{\mathbf{w_{\star}}^{3}}{2} = \frac{gh}{2} \left[\frac{\alpha \tilde{H}_{\star}}{\rho_{o} C_{p}} - \beta WS_{s} \right]$$
(5.34)

Dissipation

As seen in eq. 5.31, Niiler and Kraus (1977) include the effects of dissipation as a reduction of individual energy source terms, claiming that this approach is most consistent with the current understanding of dissipation processes. The approach is limited however by a lack of information from which to determin the various efficiency coefficients. In view of this, and in orde to simplify the current model, the alternative parameterization of Mahrt and Lenschow is used:

$$\epsilon_{\rm S}h = \frac{c_{\rm E}}{2} E_{\rm S}^{3/2}$$
 (5.35)

This expression is obtained from dimensional analysis. Similar forms are used by Zeman and Tennekes (1977) and Garwood (1977). Laboratory results of Willis and Deardorff (1974) support this parameterization.

Net Surface Energy Production

It is convenient to combine the buoyancy and wind drive surface production terms in the following form:

$$\frac{q_{*}^{3}}{2} = \frac{1}{2} \left[w_{*}^{3} + 2m_{1}u_{*}^{3} \right] .$$
 (5.36)

5.3.2 <u>Turbulent Kinetic Energy Convergence at the Thermocline</u>

The vertical integral models of NK and others have neglected the energy storage terms (1a) and (1b) of eq. 5.17 in orde to close the equation set. However the formulation of ZT suggests a closure scheme whereby E_S may be explicitly retained. Eq. 5.20 expresses the TKE flux converging below the inversion in terms of the vertical component of TKE, σ_w^2 , and a vertical velocity scale σ_w . This flux provides the energy for the local sinks, identified individually by ZT as entrainment work (eq. 5.21) and entrained fluid agitation (eq. 5.24). Considering now the integrated energy balance of eq. 5.17, it is possible to hypothesise a similar energy transfer mechanism to provide closure. This is stated here in two parts:

- i) The flux of TKE directly above the thermocline may be modelled by - $C_F/2 E_S^{3/2}$ where $E_S \propto \sigma_w^2$
- ii) This flux, together with any local TKE production, supplies all energy sinks at the thermocline.

From inspection of eq. 5.17 the following expression satisfies (i) and (ii) above:

$$-\frac{C_F}{2}E_S^{3/2} = \frac{\alpha gh}{2}\frac{\partial w'}{\partial w'}(\xi) - \frac{\beta gh}{2}\overline{s'w'}(\xi) + \frac{E_S}{2}\frac{d\xi}{dt} + SH(\xi) \quad (5.37)$$

5.3.3 Restatement of Well Mixed Layer Equations

Eq. 5.17 may be rewritten, introducing the various parameterizations and jump condition, to give

$$\frac{1}{2} h \frac{dE_{S}}{dt} = \frac{d\xi}{dt} \left[\frac{E_{S}}{2} - \frac{C_{S}}{2} \Delta U_{S}^{2} + \frac{\alpha g h \Delta T}{2} - \frac{\beta g h \Delta S}{2} \right] + \frac{q_{\star}^{3}}{2} - \frac{C_{E}}{2} E_{S}^{3/2}$$
(5.38)

Rearrangement of eq. 5.37 and eq. 5.38 yields two new equations:

$$\frac{h}{2}\frac{dE_{S}}{dt} = \frac{q_{*}^{3}}{2} - \frac{1}{2}(C_{F} + C_{E})E_{S}^{3/2}$$
(5.39)

$$\frac{\mathrm{d}\xi}{\mathrm{d}t}\left[-\frac{\mathrm{E}_{\mathrm{S}}}{2}-\frac{\alpha\mathrm{gh}\Delta\mathrm{T}}{2}+\frac{\beta\mathrm{gh}\Delta\mathrm{S}}{2}+\frac{\mathrm{C}_{\mathrm{S}}\Delta\mathrm{U}_{\mathrm{S}}^{2}}{2}\right] = \frac{\mathrm{C}_{\mathrm{F}}}{2}\mathrm{E}_{\mathrm{S}}^{3/2} \tag{5.40}$$

The remaining equations are set out below, again with jump conditions for heat, salt and momentum introduced.

$$h \frac{dT_S}{dt} = \Delta T \frac{d\xi}{dt} - \frac{1}{\rho_0 C_p} [H_S + H_L + Q_L + Q_S - q(\xi)]$$
(5.41)

$$h \frac{d\Delta U_S}{dt} = \Delta U_S \frac{d\xi}{dt} + u_{\star}^2 - PGRAD$$
 (5.42)

$$h \frac{dS_{S}}{dt} = \Delta S \frac{d\xi}{dt} + W S_{S}$$
(5.43)

$$\frac{dH}{dt} = -\frac{\alpha}{\rho_{o}C_{p}} \left[H_{S} + H_{L} + Q_{S} + Q_{L}\right] - W$$
(5.44)

$$h = H - \xi \tag{5.45}$$

$$\Delta T = T_c - T(\xi - \delta)$$
 (5.46)

$$\Delta S = S_{S} - S(\xi - \delta)$$
(5.47)

Below the thermocline,

$$\frac{\partial T}{\partial t} = -\frac{1}{\rho_0 C_p} \frac{\partial q(z)}{\partial z}$$
 (5.48)

5.3.4 Evaluation of Coefficients

To obtain a solution of the equation set 5.39 to 5.48, it is necessary first to specify the coefficients $C_F^{}$, $C_E^{}$, m and $C_S^{}$. These must be evaluated from the results of relevant laboratory and field experiments.

The following experimental results allow determination of $\rm C_{\rm F},~C_{\rm E}$ and m, with some redundancy for checking purposes.

a) Willis and Deardorff (1974):

 $\frac{1}{2} E_{\rm S} = K_{\rm ES} w_{\star}^2, \quad K_{\rm ES} \approx 0.4$

for steady-state, free convection conditions. Steady-state, in the present context, means constant surface inputs (i.e. q_{\star}^{3} constant).

b) Willis and Deardorff (1974), Kaimal et al. (1976), Mahrt and Lenschow (1976):

$$\varepsilon_{\rm S}h = K_{\rm E} w_{\star}^3, \quad K_{\rm E} \approx 0.4 \rightarrow 0.5$$

for steady-state, free convection conditions.

c) Willis and Deardorff (1974), Stull (1976) and others: $\overline{\theta'w'}(\xi)/\overline{\theta'w'}(H) = K_A, K_A \approx 0.1 \rightarrow 0.3$

for steady-state, free convection entrainment of a strong

density jump.

d) Deardorff (1974):

 $\frac{dh}{dt} = K_W w_*, K_W \approx 0.2$

for steady-state growth of a convective layer into a neutral environment.

e) Wu (1973), Kato and Phillips (1969):

$$\frac{dh}{dt} = K_p \frac{u_*^3}{\alpha gh\Delta T}, \quad K_p = 0.234 \quad (Wu)$$
$$= 2.5 \quad (Kato and Phillips)$$

for steady-state growth of a layer with a strong density jump. In Wu's experiment, turbulence was generated by wind shear in a wind/wave tank, with negligible internal shear. The Kato and Phillips experiments were conducted in an annular tank with surface shear. Internal shear generation of TKE was important in this case.

f) Tennekes and Lumley (1972):

$$\frac{dh}{dt} = K_{U}u_{*}, \quad K_{U} \approx 0.3$$

for growth of a layer into a neutral environment with turbulence generated by surface wind shear.

Relationships between C_F , C_E , m and the various K constants are set out below in algebraic form, to allow modification of constants if new experimental data become available.

For steady-state, eq. 5.39 becomes

$$0 = q_{\star}^{3} + (C_{F} + C_{E})E_{S}^{3/2}$$

$$E_{S}^{3/2} = q_{\star}^{3}/(C_{F} + C_{E}).$$
 (5.49)

so

Then eq. 5.40 becomes

$$\frac{d\xi}{dt} \left[-E_{\rm S} - \alpha gh\Delta T + \beta gh\Delta S + C_{\rm S} \Delta U_{\rm S}^2 \right] = \frac{C_{\rm F}}{(C_{\rm F} + C_{\rm E})} q_{\star}^3 \qquad (5.50)$$

eq. 5.50 reduces to

$$- \alpha gh\Delta T \frac{d\xi}{dt} = C_F w_*^3 / (C_F + C_E)$$

and so from (c) above

$$C_{\rm F} / (C_{\rm F} + C_{\rm E}) = K_{\rm A}$$
 (5.51)

or
$$C_{\rm F} = \frac{K_{\rm A}}{(1-K_{\rm A})} C_{\rm E}$$
. (5.52)

Note that (b) above is not independent of (c). It is easily shown from eq. 5.49 that

$$K_{\rm E} = \frac{(1 - K_{\rm A})}{2}$$
(5.53)

Hence the choice of K_A must satisfy both criteria (c) and (b).

Comparing item (a) with eq. 5.49, where $q_*^3 = w_*^3$ in

convective conditions, it may be shown that

$$C_{\rm F} + C_{\rm E} = (2K_{\rm ES})^{-3/2}.$$
 (5.54)

Simultaneous solution of eq. 5.52 and eq. 5.54 gives

$$C_{E} = (1-K_{A}) (2K_{ES})^{-3/2}$$
 (5.55)

$$C_{\rm F} = K_{\rm A} (2K_{\rm ES})^{-3/2}.$$
 (5.56)

Item (d) above is now redundant information for convective conditions, allowing a check on the estimates of C_F and C_E . For the stated conditons of (d), eq. 5.50 reduces to

$$E_{S} \frac{dh}{dt} = \frac{C_{F}}{(C_{F}+C_{E})} w_{*}^{3}$$
 (5.57)

and so, using eq. 5.49,

$$K_{W} = C_{F}(C_{F} + C_{E})^{-1/3}$$
(5.58)

Calculated values of $\rm K_{\ensuremath{W}}$ from eq. 5.58 may be compared with the estimate in (d).

As universal coefficients, the values determined for C_F and C_E should hold for both convective and surface shear dominated conditions. Turning to the latter, an estimate of m may be obtained from (e) above as follows: eq. 5.50 is now

(5.59)

so from (e)

(5.60)

For convenience, a new parameter $\mathbf{C}_{_{\!\mathbf{N}}}$ is defined as

(5.61)

so
$$q_*^3 = w_*^3 + C_N^3 u_*^3$$
 (5.62)

Item (f) above is now redundant, allowing a check on the value of $\rm C_N.~K_U$ may be calculated from

(5.63)

Alternatively, $\rm C_N$ may be computed from an accepted value of $\rm K_{\rm H}$:

$$\frac{(C_{\rm F} + C_{\rm E})^{1/3}}{F}$$
(5.64)

making (e) redundant, so

$$K_{\rm p} = K_{\rm A} C_{\rm N}^{3}$$
(5.65)

A comprehensive analysis of the various combinations of these coefficients was carried out, bearing in mind the experimental uncertainty of values stated in (a) to (f) above. A selfconsistant set, choosen as a result of this analysis, is as follows:

$$K_{ES} = 0.4, K_E = 0.41, K_A = 0.18$$

 $C_F = 0.25, C_E = 1.15, K_W = 0.22$
Eq. 5.60 and eq. 5.61 give (for $K_p = 0.234$)
 $C_N = 1.09, K_U = 0.25$
Eq. 5.64 and eq. 5.65 give
 $C_N = 1.33, K_p = 0.42$

These values of K_{ES} , K_E , K_A and K_W are within 10% of their expected values, giving confidence to the method of determination. K_U calculated from eq. 5.61 is somewhat lower than the expected value. Alternatively, the calculated value of K_p from eq. 5.65 is somewhat larger than Wu's estimate from (e). The latter is accepted as correct on the basis that in Wu's experiment, the wind/wave interaction would not have been fully developed in his small (2.3 m long) tank. The chosen value is much smaller than that for the Kato and Phillips experiment, as would be expecte if internal shear was dominant in their case. Model results described in Chapter 7 support the choice.

The only coefficient as yet undetermined is C_S . Experimental evidence from which to determine C_S is sparse. Sherman, Imberger and Corcos (1978) summarise the available information, concluding that $C_S = 0.3$ is the best available estimate. From this and other papers it appears that C_S may fall between 0.2 and 0.5.

Spigel (1978) analyses the timescales of the various processes within a reservoir and provides a classification scheme for determining whether surface wind mixing or internal shear will be dominant. Diurnal mixing can be shown to fall into his regime 2

 $1 < \text{Ri} < (L/2h) (H/(H-h))^{\frac{1}{2}}$

where $Ri = \alpha gh \Delta T/u_{\star}^2$, H is reservoir depth and L is the length of the reservoir basin. Typically, an hour after the onset of afternoon deepening,

Ri \approx 20, (L/2h)(H/(H-h))¹/₂ \approx 200

In regime 2, deepening is dominated by interfacial shear with Kelvin-Helmholtz billows present and interfacial displacements important. As afternoon deepening commences close to the surface, shear effects will rapidly dominate. In evaluating C_S then, it is reasonable to adjust the value between the above limits to correctly simulate observed deepening during the shear dominated periods. This adjustment is not an overall manipulation of results; on the contrary, the shear dominated mixing observed in the diurnal mixed layer should provide a valuable independent estimate of C_g .

The Kelvin-Helmholtz billows typical of regime 2 will lead to a smeared rather than sharp interface. Spigel and Imberger (1979) provide a formula for the stable interface thickness:

$$\delta = \frac{0.3(\Delta U_{\rm S})^2}{g\alpha\Delta T}$$
(5.66)

5.3.5 <u>Horizontal Pressure Gradients</u>

Spigel (1978) and Spigel and Imberger (1979) provide the basis for computation of the pressure gradient term in eq. 5.42. Figure 5.2, reproduced from Spigel and Imberger (1979), shows the response of a two-layered body of water to an applied surface stress. The interfacial velocity jump at the centre of the water body, ΔU , increases until time $T_i/4$, where T_i is the fundamental internal wave period given by





Interface shape ζ_{12} and velocity shear ΔU at five instants in time during initial half wave period.

Interface displacement ζ_{12} at downwind end of basin, showing oscillatory motion about steady state set up position; (b) velocity shear ΔU at center of basin. T_i is lowest mode internal wave period.

$$T_{i} = 2L(\alpha g \Delta T h_{1}h_{2}/H)^{-\frac{1}{2}} \approx \frac{2L}{\sqrt{\alpha g h_{1} \Delta T}} \quad (h_{1} \text{ small}) \quad (5.67)$$

At this time the waves travelling toward the centre from the end walls have set up an interface slope

$$\frac{d\zeta_{12}}{dx} = \frac{u_{\star}^2}{\alpha gh_1 \Delta T}$$
(5.68)

representing a balance between the applied stress and the horizontal pressure gradient. Damped oscillations with period T_i follow i this initial set-up, as shown in Figure 5.2, leading to a final steady-state interface slope given by eq. 5.68, with baroclinic circulation in the top and bottom layers.

For the half wave period after time $T_i/4$, water above and below the interface will undergo negative acceleration under the influence of the pressure gradients associated with free surface tilt and interfacial tilt respectively. The net effect on ΔU_S is seen in Figure 5.2, and may be described by the term PGRAD in eq. 5.42, given by

$$PGRAD = \nabla p = \frac{2\rho_0 u_{*}^2}{h_1}$$
(5.69)

The algorithm for computing PGRAD for the appropriate half wave periods is described in Chapter 6.

5.3.6 Model Response to Changing Inputs

Eq. 5.39 and eq. 5.40 together describe the response of the WML to changing inputs. If q_* suddenly increases, E_S will grow smoothly with time. Similarly the deepening response of eq. 5.40 is smoothed by the transient changes of E_S . This will introduce a time lag in deepening rate changes and also in the occurrence of layer retreat if q_* decreases suddenly.

More important then the time lag is the behaviour of the entrained fluid agitation term. If q_* suddenly decreases (e.g. the wind speed suddenly drops) this term, $E_S/2 d\xi/dt$, decays exponentially. This response, coupled with a decay of mean velocity allows the model to proceed smoothly to a new equilibrium. An alternative scheme, equivalent to that proposed by ZT, sets $dE_S/dt =$ and computes E_S as

$$E_s = \text{constant } x q_*^2$$
 (5.70)

 $E_S/2 d\xi/dt$ now follows q_* changes instantaneously. Problems may arise in the solution if shear production is dominant so that, from the RHS of eq. 5.40, the sum

$$-\frac{\alpha gh\Delta T}{2}+\frac{\beta gh\Delta S}{2}+\frac{C_{S}\Delta U_{S}^{2}}{2}$$

is a small number. Here, the deepening rate - $d\xi/dt$ will be large, and - $E_g/2$ will be significant when compared with the above sum of terms. A sudden drop in $E_g/2$, as computed from eq. 5.70 for a sudden wind speed drop say, may have a serious effect on a numerical solution: it will suddenly force the solution onto the singularity of eq. 5.40. It might be argued that a numerical solution with a small enough timestep should cope with any natural wind gusts, which develop over a finite time. However, in practice, the data usually available are in the form of time averages (e.g. 10 minute, hourly), and it is most convenient to allow the model to negotiate the discontinuities of such time series by itself (i.e. without prior smoothing of the data). For such data then, q_* will exhibit sudden changes.

In summary, where WML behaviour is being modelled on a short timescale with finely resolved inputs, the formulation of model equations 5.39 to 5.48 is recommended.

5.3.7 A Model for Seasonal Simulations

For most reservoir and oceanic applications a model is required to predict seasonal behaviour of surface water rather than diurnal behaviour. Data are generally sparse and may not be resolved better than daily averages. For such a case it is justifiable to neglect the effect of transient turbulent energy storage and decay. Hence eq. 5.39 and eq. 5.40 reduce to the forms given by eq. 5.49 and eq. 5.50, rewritten here as one expression:

$$\frac{d\xi}{dt} \left[-\left(C_{F}+C_{E}\right)^{-2/3} q_{*}^{2} - \alpha gh\Delta T + \beta gh\Delta S + C_{S}\Delta U_{S}^{2} \right] = \frac{C_{F}}{\left(C_{F}+C_{E}\right)} q_{*}^{3}$$
(5.71)

An entrainment relation of this form was first presented by Sherman, Imberger and Corcos (1978) and further developed by Fischer *et al.* (1979). These authors analysed the potential and kinetic energy budgets of a column of water and so derived the expression

$$\frac{dh}{dt} \left[C_{T}q^{2} + \alpha gh\Delta T - \beta gh\Delta S - C_{S}\Delta U_{S}^{2} \right] = C_{K}q^{3}$$
(5.72)
where $q^{3} = \left(\frac{\alpha ghH}{\rho_{o}C_{p}} + \eta^{3}u_{*}^{3} \right)$

Neglecting differences in the derivation and definition of some terms, the coefficients $C_{K}^{}$, $C_{T}^{}$ and η may be evaluated using the values of $C_{F}^{}$, $C_{E}^{}$ and $C_{N}^{}$ from Section 5.3.4, and compared to values supplied by Fischer *et al.* (1979):

$$C_{K} = 0.18 \text{ (cf } 0.13 \text{ from Fischer et al.)}$$

$$C_{T} = 0.8 \text{ (cf } 0.5 \text{ from Fischer et al.)}$$

$$\eta = 1.33 \text{ (cf } 1.2 \text{ from Fischer et al.)}$$

CHAPTER 6

A NUMERICAL MODEL OF THE DIURNAL WELL MIXED LAYER

Most of the theory developed in Chapter 5 is quite general and may be applied to both marine and atmospheric well mixed layers. It is noteworthy that some of the universal coefficients of Section 5.3 were evaluated from atmospheric field data.

The concept of a diurnal well mixed layer in a reservoi was introduced in Section 4.4. In this chapter the various algorithms required to incorporate the theory of Chapter 5 into a computer model of the diurnal cycle are described. The objectives of the modelling exercise are:

- to predict the diurnal cycle of temperature and salinit
 within the bulk or seasonal WML, including both layer
 retreat and layer deepening, and,
- ii) to investigate the roles of individual deepening mechanisms and comment on the choice of coefficients in Section 5.3

6.1 MODEL ARCHITECTURE

Figure 6.1 is a block diagram of the model showing fundamental input and output requirements. The following considerations influenced the model's architecture:

 Simulation runs are for single days only (data were not gathered for successive days). Hence it is reasonable to be



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generous with computer resources since the running costs are minimal.

2. Fluctuations of wind and surface heating were observed to produce intermittent mixing events which left skeleton step structure within the seasonal well mixed layer. For example, the effects of the previous night's mixing could be seen in the morning as a fairly sharp step near the base of the seasonal well mixed layer. This skeleton structure, containing significant density gradient, affects subsequent deepening and the model must therefore 'remember' it.

The following are the broad features of the model. Reference is made to the model flowchart (Appendix B2) and the program copy (Appendix C2).

6.1.1 <u>Vertical Grid</u>

To give the model memory, a vertical grid of closely and equally spaced points is used. Associated with the grid are temperature and salinity arrays, which are loaded from the initial profiles and subsequently updated as the simulation proceeds.

Superimposed over the upper part of the grid is the diurnal WML. Note that the WML depth h is not constrained to coincide with a grid point; solution of the WML equations occurs independently, except for a procedure for determining the thermocline temperature step as described in Sections 6.2.3 and 6.2.6 Grid points falling within the WML are updated to reflect WML temperature and salinity.

Required resolution is the major critierion for determining grid spacing. If WML retreat occurs, the remaining temper-

ature step is remembered as the difference between two adjacent gridpoint temperatures. If the grid spacing is large and the step was not central in the grid interval, a heat storage error is introduced. Large spacing also results in smoother gradients, giving a poor representation of steps. The surface temperature profile under strong solar heating would also be poorly represented. In view of the above and in the light of model testing, a grid spacing of between one and five centimetres is acceptable. For flexibility, grid spacing appears in the model as a variable to be specified in the input data.

6.1.2 Model Timestep

Two criteria for the model timestep must be satisfied:

- i) it must be much smaller than the timescale of meteorological flux changes, and,
- ii) it must be sufficiently small to ensure that not more than one gridpoint is entrained per step during WML deepening. This is to ensure that the algorithm for AT and AS determination remains valid.

The shortest timescale for fluxes is 15 minutes (see Section 3.4.3) so criterion (i) is easily met. However, the deepening rate varies greatly, being dependent on meteorological forcing and the recent history of deepening or retreat. To enhance model efficiency, the timestep is managed dynamically within the range 30 seconds to 4 minutes. Details are as follows:

 A check is maintained on the deepening after each timestep. If it falls outside acceptable upper or lower limits (fractions of a grid interval) the timestep is halved or doubled within the specified range.

ii) When approaching a new flux interval, or at the onset of deepening following WML retreat, the timestep is set to 30 seconds and subsequently allowed to readjust itself via (i). This minimises the integration timestep for a period where the time derivatives of eqs. 5.39 to 5.48 are likely to be large.

6.2 DESCRIPTION OF MODEL ALGORITHMS

Details of those model algorithms not fully described by the flowchart in Appendix B2 are provided below.

6.2.1 Loading Grid Arrays

Part of File 1 (see Figure 6.1) is a specified number of height/temperature/salinity records. These are read into S/R LOAD which then, by linear interpolation, assigns a temperature and salinity value to each gridpoint. These values specify the starting profile for the model.

6.2.2 Meteorological Flux Computation

S/R FLUXES initially accesses File 2 (sequential records of meteorological data) and reads records until the correct time interval is entered. In subsequent calls to S/R FLUXES, the interval is updated only if the model time has advanced past the old interval end-time.

In S/R FLUXES, the timestep-average meteorological data are determined by linear interpolation within the current interval. These data, plus the current

modelled WML temperature, are fed to S/R TURB which computes stability corrected meteorological fluxes by the method described in Section 3.5.2. Use of the model WML temperature in the computation of turbulent and long-wave radiative heat fluxes provides a feedback to the WML simulation.

Instantaneous fluxes required by the integration routine are similarly computed through ENTRY IFLUX.

6.2.3 Solar Heating Below the Well Mixed Layer

Eq. 5.48 must be solved every timestep to simulate heating by solar radiation absorption in the water below the WML. S/R SOLAR actually heats all gridpoints, but those in the resultant WML are overwritten later with the value of T_S . This process is necessary to correctly simulate the heating associated with WML retreat, should this occur.

S/R SOLAR and S/R STEP together compute the temperature and salinity gradients directly beneath the WML, by remembering the details of the most recently entrained gridpoint. This gridpoint, with pre-entrainment temperature and salinity values substituted, is heated and then used to compute the new gradients.

6.2.4 Well Mixed Layer Deepening or Retreat?

The physical insight into WML retreat afforded by eqs. 5.39 and 5.40 justifies their added complexity. It would be possible to continue solving an entrainment equation such as eq. 5.71 after q_* had become negative (e.g. for conditions of strong solar heating and light winds), giving continuous de-entrainment of water, which is not realistic. Field observations from this project indicate that when solar heating begins to dominate, continuous mixing degenerates to sporadic mixing events and the once active thermocline region retains its position, subject only to diffusive processes. $d\xi/dt$ never becomes positive, but a new mixed layer may subsequently form within the old layer if mixing energy again becomes available at the surface.

Eq. 5.40 shows that, for entrainment to occur, there must be a positive energy level E_S within the layer. There is no such thing as negative energy; hence $d\xi/dt \leq 0$ always. A new shallow layer must therefore form whenever E_S for the existing layer decays to zero. Within the model, a check is maintained on the value of E_S , and if it is certain to decay to zero in the next timestep, layer retreat computations are initiated.

6.2.5 Layer Retreat

When E_S has decayed to zero, a new layer depth must be found such that E_S and its time derivative dE_S/dt are just held to zero. In this new layer, TKE introduced by wind stirring will just balance the buoyant damping due to solar heating. Eq. 5.39 then reduces to

$$q_{\star}^{3} = 0$$
 (6.1)

where $q_{\star}^{\ 3}$ is a complicated function of h (or $\xi)$ through the term $\stackrel{\sim}{H}_{\star}$.

Solution of eq. (6.1) in the model is performed by the Newton-Raphson iteration method. The derivative $dq_{*}^{3}/d\xi$ necessary for this method is evaluated by ENTRY NEWSIG. The iteration is performed by S/R NEWTON. Convergence of ξ to its new value (to

within .05%) is rapid (usually less than five steps).

If the salinity flux contribution to w_{\star}^{3} is neglected, eq. 6.1 reduces to

$$h = \frac{C_N^3 u_*^3}{\alpha g \tilde{H}_* / \rho_0 C_p}$$

which, from inspection, is a form of Monin-Obukhov length (see eq. 2.5). The above procedure for determining h from eq. 6.1 is consistent with the definition of the Monin-Obukhov length given in Section 2.1.1.

Having determined ξ , the equations for WML heat and salinity (5.41 and 5.43) are solved while constraining dE_S/dt, d\xi/dt and dU_s/dt to zero.

The velocity jump ΔU_S at the thermocline is computed, during deepening, from eq. 5.42, which is based on the assumption that the velocity below the thermocline may be neglected. When layer retreat occurs, ΔU_S is set to zero in the model and only increases again when deepening is re-initiated. This procedure does not conserve momentum but does provide a correct description of ΔU_S . The problems of specifying momentum sinks (e.g. internal wave radiation) and changing wind directions are thus avoided. Although wind direction was not reliably measured during the fieldwork, it was noted that the afternoon winds responsible for deepening came from a single quadrant.

6.2.6 Integration of Well Mixed Layer Equations

S/R MESRl is a fourth order Runge Kutta routine which computes relative accuracy of integration via a fifth step, and uses this test to govern its own timestep halving or doubling



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procedure. This procedure is independent of the model timestep management described in the Section 6.1.2, except that the integration timestep is not allowed to exceed the model timestep. In practice the two agree except for rapidly changing conditions where the integration timestep decreases.

The WML differential equations are contained in S/R DIFF, together with other necessary expressions which are described below.

i) The temperature and salinity jumps at the bottom of the layer must be evaluated for each Runge Kutta (RK) step. ΔT and ΔS change as the layer deepens and as the water below the thermocline is heated. The scheme for computing the temperature and salinity gradients below the WML was summarised in Section 6.2.3. For increased precision, these gradients are also determined each RK step. Given the gradients and the current value of ξ , ΔT and ΔS are given by

$$\Delta T = T_{S} - T_{1} - (\xi - z_{1}) \frac{dT}{dz}$$
(6.2)

$$\Delta S = S_{S} - S_{1} - (\xi - z_{1}) \frac{dS}{dz}$$
(6.3)

 T_1 and S_1 are the values at the gridpoint immediately below the WML, at height z_1 . Figure 6.2 aids understanding of eq. 6.2.

ii) Instantaneous meteorological fluxes are determined each RK step, for use in the solution, by a call to ENTRY IFLUX (previously described). To facilitate interpolation in the flux interval, the RK integration range is matched to the flux interval. Each time S/R FLUXES indexes the flux interval it also resets the RK integration range (i.e. ST = 0.0).

- iii) The WML deepening equation 5.40 has a singularity discussed previously in Section 5.3.6. During deepenin with continuous determination of the fluxes, ΔT and ΔS , the RK scheme will properly manage integration if this singularity is approached. That is, $d\xi/dt$ will become large. Care is necessary, however, to ensure that deepening is initiated correctly following layer retreat (when $\Delta T = \Delta S = 0$). This is accomplished by keeping $\Delta U_S = 0$ until mixing is definitely established, that is, ξ has fallen. In practice this occurs within one or two model timesteps. It is detected in the mainline and transmitted to S/R DIFF by the variable MFLAG.
- iv) As mentioned in Section 6.2.5, once ξ has been determined by iteration, the remaining WML equations (except momentum) are solved. This can be seen in S/R DIFF: when NFLAG = 0, $dE_S/dt = d\xi/dt = d\Delta U_S/dt = 0$, and dT_S/dt , dS_S/dt and dH/dt are solved normally.

6.2.7 Pressure Gradient Calculation

In varying wind conditions it is difficult to calculate a representative value of T_i from eq. 5.67 in order to determine whether the interfacial pressure gradient has been set up. An alternative procedure which was adopted is described below.

At each timestep the advected volume is updated from its value at the previous timestep:

$$v_t = v_{t-1} + h \Delta U_S \Delta t$$

Also computed is the final set-up slope from eq. 5.68 and, from this, the final advected volume

$$V_f = \frac{L^2 u_{\star}^2}{8 \alpha g h \Delta T}$$
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The pressure gradient PGRAD is turned on if V $_{\rm t}$ > V $_{\rm f}$ and off if V $_{\rm t}$ < V $_{\rm f}.$

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CHAPTER 7

RESULTS OF MODEL SIMULATIONS

The numerical model described in Chapter 6 was first developed and then refined to its final form using only the data from the field day 05 02 76. Determination of an appropriat value for C_S , as described in Section 5.3.4, was also completed using this one data set. These procedures were adopted because:

- i) data from day 05 02 76 were considered to be the most reliable overall, and,
- ii) data from the remaining three days then provided a realistic test for the model.

In order to provide maximum insight into the mechanics of the model, a composite set of computer plots was produced These plots are described in Section 7.1. Section 7.2 contains an analysis of the model predictions for a full daily cycle. Section 7.3 contains an appraisal of the model's performance and a discussion of specific model deficiencies.

7.1 DESCRIPTION OF MODEL PLOTS

Two forms of model output have been plotted for analysis. These are described below.

7.1.1 Temperature Profile Plots

The measured profiles of temperature at specified times throughout the four field days were described in Section 4.4.1 and presented as computer plots in Appendix A5. Figure6.1 shows that the model output File 6 contains modelled profilesfor those times which correspond to field profiles.

The computer plots in Appendix Dl were produced, following a model run, by a program which accessed both the field profile data and File 6. Field data points are plotted as crosses while the model profile appears as a full line. The initial model profile for each day is loaded from File 1 so as to be identical to the field profile, although specification of an initial thermocline height tends to be somewhat arbitrary in mid-morning.

The temperature jump_at the thermocline is plotted with its position and magnitude exact. Only one grid point in every four is plotted however, giving a depth resolution of 20 cm, equal to the finest resolution of field profiles. Note that the start and scale values on the temperature axis vary for different days.

7.1.2 Daily Cycle Plots

These plots, appearing in Appendix D2, were produced from File 5 and File 8 of Figure 6.1.

The lowermost plot on each page shows the meteorological fluxes which were computed within the model. These fluxes combine to form the net surface power term, q_*^3 , plotted on a log scale in the second plot. Only values of q_*^3 above 1.0 x 10^{-10} are plotted; positive values below this are negligible and layer retreat precludes negative values, except for short periods immediately prior to retreat. Plotted with q_*^3 , also

on a log scale starting from 1.0 x 10^{-7} , is the WML TKE level, $E_{\rm S}$.

The third plot from the bottom shows the evolution of temperature, salinity and velocity differences across the thermocline. Large values of ΔT and $-\Delta S$ inhibit mixing, while ΔU_{c} promotes mixing at the thermocline.

The uppermost plot shows the evolution of temperature and depth of the WML. The start and scale values of axes for this plot vary from day to day.

7.2 ANALYSIS OF THE SIMULATION OF A DIURNAL CYCLE

Inspection of one of the plots of Appendix D2 will aid understanding of the mechanics of the model. The plot for day 05 02 76 is broken into convenient time intervals and discussed below.

i) 0630 to 0820

Latent cooling and surface stirring are dominant, giving a large value of q_*^3 and hence large E_S also. This period is in fact the end of the night cycle, where mixing has proceeded to a depth of 8 metres, below which there is a moderately stable temperature gradient down to the seasonal thermocline at 12 metres. (At this time of the year the seasonal thermocline is still strengthening.) With increasin solar heating and a drop in wind after 0800, q_*^3 drops rapidly to zero at 0808 and then becomes negative (not plotted). The transient response of the model is apparent at this time; E_S does not fully decay to zero until 0820. A survey of all plots shows E_S lagging q_*^3 , as expected from eq. 5.39.

ii)

0820 to 1400

At time 0820 there is a good example of layer retreat. Within one timestep (30 seconds), the WML depth h changes from 8.13 m to 3.83 m. The full plotted line representing this jump should not be considered as representing an upward movement of the thermocline. The old temperature step still remains at 8.13 m depth as seen from the 0830 model profile in Appendix D1.7(it appears somewhat diffused due to the selective plotting of gridpoints).

On three occasions before 1400, sufficient surface power q_*^3 becomes available to initiate layer deepening. As can be seen from the plot of h however, these mid-morning mixing events have little effect and serve only to distribute heat over a slightly greater depth. By 1230 the WML is only 13 cm deep and its temperature has risen dramatically. The 1230 profile shows a strong temperature gradient below the layer. Absorption of solar radiation in the surface two metres is the dominant effect. When slight mixing is initiated after 1230, a large value of ΔT inhibits its progress. At 1430, although q_*^3 goes negative for a brief period (four minutes), E_c does not completely decay.

iii) 1400 to 2310

Layer retreat does not occur again after 1400. Increasing wind speeds and latent cooling are associated with decreasing solar heating and so q_*^3 climbs to high values, providing a continuous supply of mixing energy. The importance of accurately describing short period wind

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speed peaks can be seen around 1545.

The momentum of the WML (and hence $\Delta U_{\rm S}$) increases until 1815, supplying mixing energy at the thermocline. All mixing mechanisms are operative during this period, with interfacial shear dominating. At 1815 the pressure gradient described in Section 6.2.7 is set up, and by 2310 this has driven almost one complete oscillation (as shown in Figure 5.2.)

7.3 COMPARISON OF MODEL AND FIELD PROFILES

Overall, the comparison between modelled and measured temperature profiles as plotted in Appendix Dl is very good. The capability of the model to simulate the heating and mixing phases, with the transitions occurring at roughly the correct times, substantiates the form of the model equations 5.39 to 5.48 and the use of q_{\star}^{3} as the controlling parameter.

Some aspects of the model's performance are examined in detail below.

7.3.1 <u>Model Coefficients</u>

A value of $C_S = 0.2$ was chosen after several model runs with different values. The model response proved to be quite sensitive to this parameter. Setting $C_S = 0$ for example resulted in a 40% decrease in deepening rate during the afternoon of 05 02 76.

Table 7.1 gives all the universal coefficients and other physical constants used. Derived values applicable to the Reservoir model DYRESM are included. Also included are current values used in DYRESM (Imberger and Hebbert (1980)).

		_
MODEL COEFFICIENT	VALUE	
C _F	0.25	
с _Е	1.15	
с _N	1.33	
с _s	0.20	
DYRESM EQUIVALENTS	DERIVED VALUE	CURRENT VALUE
с _к	0.18	0.125
с _т	0.80	0.51
η	1.33	1.23
с _s	0.20	0.50
PHYSICAL CONSTANTS		
α	$2.54 \times 10^{-4} \text{ °C}^{-1}$	
β	10 ⁻⁶ ppm ⁻¹	
C _P	4180 J/kg ^O C	
ρ _ο	1000 kg/m ³	
L (Latent heat)	2445 kJ/kg	

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TABLE 7.1 - Model coefficients and physical constants. DYRESM equivalents are derived in Section 5.3.7. Current values of DYRESM coefficients are as specified by Imberger and Hebbert (1980). Referring to the choice of C_N discussed in Section 5.3.4, it was found that the value obtained from eq. 5.61 caused an unrealistic delay in the onset of deepening during daytime hours. Recall that deepening commences soon after

$$q_{*}^{3} = w_{*}^{3} + C_{N}^{3}u_{*}^{3}$$

becomes positive. If w_* is negative (when solar heating is strong) the value of C_N determines the wind strength necessary to initiate mixing. Mixing will occur whenever $C_N u_*^{3} \ge -w_*^{3}$. C_N determined from eq. 5.65, however, produced very good model response to changing meteorological conditions. This value appears in Table 7.1.

7.3.2 <u>Thermocline Thickness</u>

The profile plots of Appendix D1 show the thermocline as having zero thickness; hence the temperature profiles include a sharp step across the thermocline, consistent with the assumptions stated in Section 5.1. In conditions of free convectior where only surface cooling is important, the thermocline does become very thin (see Willis and Deardorff (1974)). In the reservoir however there is almost always some shear across the thermocline during deepening and so Kelvin-Helmholtz billows, as described in Section 5.3.4, will ensure a finite thermocline thickness.

Intuitively, it is expected that the mixing process at the thermocline is cyclic in nature. Billowing would be followed by entrainment of the diffuse region, sharpening the gradients until billowing recurs. It must be assumed for modelling purposes that the efficiency of entrainment of the

diffuse region is accounted for in the coefficient C_S , so that the model computes the correct deepening rate. Accepting this, it is possible to directly compare the model and field profiles.

An ideal procedure to aid comparison, given accurate and finely resolved field profile data, would be to 'square up' the field profiles, conserving heat and potential energy. An alternative means of aiding comparison has been adopted here. The thickness of the billowing region was calculated from eq. 5.66 for those profiles where deepening was established, prior to interface set-up. The position of this region in plotted field profiles was determined by visual inspection and is shown, on the particular plots, as the region bounded by dotted lines. The agreement between computed and observed thickness of this region is very good. Note how the billowing region becomes very thin on 05 04 76 at 0200 after mixing has encountered the seasonal thermocline. The salinity jump is also significant at this time, as shown by the daily cycle plot in Appendix D2.4.

7.3.3 <u>Temperature Profile Representation</u>

Accepting the thermocline step representation of the temperature profile, there remain three anomalies, common to the model profiles of all days, which require explanation:

- The model layer retreat occurs too slowly and WML temperature is underpredicted in the mornings,
- ii) Overheating of the WML occurs in early to midafternoon and subsequent WML deepening is impeded somewhat by the large resultant value of ΔT, and,
 iii) The model underpredicts heating of the water at

medium depth below the WML in the hours around midday.

The dominant cause of both (i) and (ii) above is clearly the model's method of stability correction to meteorological fluxes. The problem was addressed in Section 3.5.2. Neglecting the precise details of the calculation procedure, the method effectively corrects the fluxes with the parameter $Ri_{\rm R}$, where from eq. 2.43

$$Ri_{B} = \frac{gz}{T_{V}} \quad \frac{(\Delta \theta + 0.61T_{V} \Delta q)}{U^{2}}$$

The value of $\Delta \theta$ is evaluated by

$$\Delta \theta = T_{10} - T_{S},$$

that is, the temperature at z_{H} is taken to be the WML temperature T_{S} . The correct value to use however is the temperature of the conductive sublayer at the surface, or the 'skin' temperature, which will deviate from T_{S} towards the air temperature. Hence, $|\Delta\theta|$ is always overestimated in the model. This leads to unrealistic enhancement of latent cooling in the morning ($\Delta\theta$ negative) and suppression of latent cooling in the early to mid-afternoon ($\Delta\theta$ positive), explaining the anomalies (i) and (ii). A similar effect on the momentum flux $\rho_{o}u_{\star}^{2}$ enhances deepening (delays retreat) in the morning and inhibits deepening in the afternoon. Sensible heat flux is similarly affected but is small in magnitude compared with latent heat flux.

Model runs in which the stability correction was suppressed gave results which erred in the opposite sense, as expected. Having understood the problem it was decided to retain the stability correction method, as stability effects over a medium sized reservoir are obviously important. Future work may involve modelling of the 'skin' temperature to provide the correct value for stability calculation.

In the case of (iii) above, there are two factors which may contribute to insufficient heating of gridpoints at a medium depth below the thermocline.

The form of the solar shortwave radiation attentuation profile given by eq. 3.1 may be somewhat in error. Tests of the model using different attenuation profiles indicated a marked sensitivity to the form chosen. A form which prescribes less attenuation near the surface and greater attenuation at depth would tend to correct the anomaly (iii) and also (ii). The form of eq. 3.1 will be retained, however, until more reliable field data for the Wellington Reservoir become available.

The feature of the model which is mainly responsible for (iii) (and to some extent, (ii)) however is the flux boundary condition at the base of the thermocline. In Section 5.3.1 the following are specified: $\overline{u'w'}(\xi-\delta) = \overline{\theta'w'}(\xi-\delta) = \overline{s'w'}(\xi-\delta) = 0$. In reality however, there will be leakage of these fluxes through the thermocline, especially when ΔT is small and diffuse.

Below the thermocline, residual turbulence, plus turbulence from other sources (thermocline leakage, internal wave breaking) will act to distribute the leaked heat downwards, so heating the water. The turbulence will also enhance diffusion of temperature and salinity where sharp gradients remain after WML retreat. No diffusion mechanism has been included in the model and so temperature structure below the WML retains its identity over a full daily cycle.

7.3.4 Conclusions

This Section has described various aspects of the model's performance which lead to observable differences between modelled and measured profiles. It is evident however that the model can simulate the essential mechanisms involved in the diurnal cycle on a quasi-continuous timescale (bearing in mind the smoothing of meteorological data). The results discussed in this Chapter lend strong support to the formulation of well mixed layer energetics developed in Chapter 5.

7.4 HEAT AND POTENTIAL ENERGY BUDGETS

In conclusion, an interesting observation on the sensitivity of heat and potential energy budget calculations is described below.

As stated in Section 4.1, temperature profiles were measured with, at best, an accuracy of 0.1°C, corresponding to the finest graduation on the thermometer used for calibration. If an hour by hour heat budget of the top seven metres of water is attempted, the uncertainty in the heat storage calculation associated with the above accuracy will be,

 $\Delta H = 7 \times \rho C_{D} \Delta T = 2930 \text{ kJm}^{-2}$

However, this uncertainty is of the same order of magnitude as the surface heat transfers for the period. For example, on the day 05 02 76 between 1430 and 1530 hours, the relatively large surface heat transfers were as follows:

 $H_{sensible} = -100 \text{ kJ m}^{-2}$, $H_{latent} = 1096 \text{ kJ m}^{-2}$, $H_{shortwave} = -2897 \text{ kJ m}^{-2}$,
$H_{longwave} = 126 \text{ kJ m}^{-2}.$

Obviously on such a short timescale, no meaningful heat budget calculations are possible, as the measured temperature profiles are not sensitive enough to heat transfer. In particular it is not possible to estimate evaporation by this method.

The profiles plotted in Appendix A5 or Appendix D1 present another intriguing possibility however. Unlike the absolute temperature, the well mixed layer depth is very sensitive to the balance of surface heat transfers and its changes may be measured quite accurately. In other words, whereas heat budget calculations are impractical, it is possible to accurately estimate the potential energy increase of a water column associated with WAL deepening. As confidence is gained in the values of universal coefficients (see Table 7.1), the model may be used in reverse to predict the surface heat transfers leading to an observed WAL deepening pattern. Of particular interest is the steady state, free convection situation found on cold, calm nights. The deepening equation for this case (see eq. 5.51) may be rearranged to the form

$$H_{S} + H_{L} + Q_{L} = \frac{{}^{\rho} \circ {}^{\rho} p}{K_{A}} \left(\Delta T {}^{dh}_{dt} \right)$$
(7.1)

The longwave radiation Q_L may be calculated accurately and the product ΔT dh/dt may be computed from sequential measured profiles. Eq. 7.1 therefore provides a useful tool for appraising the various formulations of atmospheric turbulent heat transfer from a reservoir surface in free convection conditions.

CHAPTER 8

CONCLUSIONS

The numerical model of the diurnal cycle within the seasonal well mixed layer appears to be capable of simulating all of the important features of that cycle. A few features of lesser importance are not directly simulated, but their effects have been examined qualitatively. Important aspects of the Project in general and of the model's capability are outlined below.

The model simulates realistically the shallowing of a diurnal well mixed layer when solar heating is dominant and also the deepening of this layer when surface cooling and mixing become dominant. The success of the model lies in its formulation. Careful integration of the turbulent kinetic energy equation over the full well mixed layer depth ensures that all known contribution Equations for heat, mass, momentum and salt concenare included. tration are similarly treated. The depth and temperature of the well mixed layer during strong solar heating is determined by the parameter $\textbf{q}_{\star},$ which incorporates the effects of surface wind stirring, surface heating and cooling by all heat fluxes and, importantly, penetration of solar radiation below the surface. The parameterization schemes employed for surface energy transfers and internal shear production of energy are supported by the model's results. Also supported is the closure hypothesis which describes convergence of turbulent kinetic energy at the thermoclin leading to the final equation set of eqs. 5.39 to 5.48. Retaining

turbulent kinetic energy as a model variable results in a smooth model response to rapidly changing meteorological inputs. It also enhances interpretation of model behaviour. For example, layer retreat occurs only when the energy in the old layer has been completely consumed in overcoming the buoyancy induced by solar heating.

The model also realistically predicts the vertical temperature structure at particular times throughout a daily cycle. Predicted values of velocity and turbulent kinetic energy are also realistic, although no field measurements of these are available. The values of C_F , C_E and C_N from Table 7.1 may therefore be used with some confidence, especially considering the internal consistency of their determination. The shear production efficiency, C_S , has also been determined with some confidence as described in Section 7.3.1.

Averaged meteorological data used by the model are of high quality. As discussed in Section 7.3.3 however, using modelled or measured mean water temperature to compute a stability correction to atmospheric turbulent transfers will cause the correction to be overestimated. The correct temperature to use is that of the surface 'skin' or conductive sublayer. The problem is evidenced, in the model results, by morning over-cooling, afternoon over-heating and a time delay in the onset of either layer retreat or layer deepening. The problem should be addressed in future work.

Features of secondary importance are discussed in Chapter 7. The presence of Kelvin Helmholtz billows at the thermocline is clearly seen from field data (see Appendix D1). The model does not explicitly represent these however. Modification

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of thermocline shear by reservoir end wall effects is represented i the model but has not been verified from field data. Leakage of heat, salt and momentum through the thermocline and diffusion of these below the thermocline are also evident from field data, but are not included in the model due to a lack of information on these processes.

The model equations and coefficients, now tested, may be directly incorporated into a model such as DYRESM which includes simulation of the seasonal structure. It will be profitable to continue to study the diurnal cycle, however, in order to improve some aspects of the model. Future work could involve:

- i) obtaining finely resolved (e.g. 10 minute average)
 meteorological data over several daily cycles to allow
 more extensive model testing,
- ii) measuring the solar radiation attenuation profile more accurately,
- iii) obtaining a measure or estimate of 'skin' temperature for atmospheric stability calculation,
- iv) measuring a velocity profile (if instrumentation with sufficient resolution becomes available) and so investigating the momentum budget,
- v) investigating the atmospheric internal boundary layer in order to specify maximum heights for meteorological. sensors,
- vi) parameterizing thermocline leakage and hypolimmetic diffusion, and,
- vii) improving the estimate of C_c.

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APPENDIX A: FIELD DATA

N. X.

DATE 150176 SERIES 1

RUN 3 DAY 1	TIME PERI	10 830 TO	930		RUN	5	DAY	1	TIHE	PERIOD	1030 TO	1130	
H.H. 0/P (NV)	42.0 55.	3 59.8	59.8		M.H	0/P	(HV)		51.4	58.2	51.1	67.6	
SPOT READINGS	44.1 56.	3 59.0	62.2		SPO	T REAL	DINGS		56.2	60.4	49.0	69.1	
	AT(C)	WT(C)	RH (%)	NR (HW/SQCH)					AT	(C)	WT(C)	RH (%)	NR (NW/SQCH)
H.M. AVERAGES	20.6	23.7	59.8	62.4	H.H	. AVE	RAGES		2	4.5	24.8	51.1	85.9
CURRENT SPOT READ. PREVIOUS SPOT READ.	21.4 . 18.6	24.1 23.5	59.0 62.0	69•7 49•5	CUR PREV	RENT S IOUS	SPOT R Spot r	EAD. EAD.	2 2	6.2 3.7	25.6 24.6	49.0 56.0	90.5 82.7

SPEED(M/S)	E.R.ANEH(H/S)	PYR (MW/SQCM)	KIPP(MW/SQCM)	SPEED(M/S)	E.R.ANEH(M/S)	PYR(HW/SQCM)	KIPP(MW/SQCK)
• 0	1.4	88.8		,	.0	1.6	88.8	

RUN 4 DAY 1	TIME PERIOD	930 TO 1	030	•		RUN 6 DAY 1	TIME	PERIOD	1130 TO	1333	
N.K. 0/P (HV) -	46.2 55.9	56.5	62.5			N.H. 0/P (HV)	59.7	61.7	39.2	0.0	
SPOT READINGS	49.9 57.7	56.0	66.5			SPCT READINGS	64.7	65.0	39.0	63.6	
	AT(C)	WT(C)	RH (%)	NR (MW/SOCH)	•		AT	(с)	WT(C)	R4(I)	NR (MW/SOCH)
M.M. AVERAGES	22.3	24.0	56.5	70.5		M.M. AVERAGES	2	7.6	26.1	39.2	0.0
CURRENT SPOT READ. PREVIOUS SPOT READ.	23.7 21.4	24.6 24.1	56.0 59.0	82 .7 69 . 7	a.	CURRENT SPOT READ. Previous spot read.	20	9.5 6.2	27.3 25.6	39.0 49.0	89.3 90.5

 SPEED(M/S)
 E.R.ANEH(M/S)
 PYR(HW/SQCH)
 SPEED(H/S)
 E.R.ANEH(H/S)
 PYR(HW/SQCH)
 KIPP(HW/SQCH)

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 1.6
 68.8
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RUN 7 DAY 1	TIME PERIOD 1333	TO 1430	$(A_{ij}) = (A_{ij}) = (A_{ij})$	RUN 9 DAY 1 TIME PERIOD 1530 TO 1645
M.N. 0/P (HV)	64.3 61.8 35	.6 64.7		N.H. O/P (HV) 66.5 60.3 37.3 59.0
SPOT READINGS	66.9 62.5 38	.0 66.7		SPOT READINGS 66.0 59.4 37.0 55.0
	AT(C) WT(C) RH(Z)	NR (MW/SQCM)	AT(C) WT(C) RH(Z) NR(MW/SQ
M.M. AVERAGES	29.4 26.	1 35.6	77.4	M.M. AVERAGES 30.2 25.6 37.3 50.2
CURRENT SPOT READ. PREVIOUS SPOT READ.	30.4 26. 29.5 27.	38.0 3339.0	83.6 89.3	CURRENT SPOT READ. 30.D 25.2 37.0 48.3 PREVIOUS SPOT READ. 30.7 26.2 35.0 71.2
SPEED(M/S)	E.R.ANEM(M/S) P	(R(HWŻSQCH)	KIPP(HW/SQCH)	SPEED(M/S) E.R.ANEM(M/S) PYR(MW/SOCM) KIPP(MW/S
.0	2.5	93.5		•0 5•7 23•7
RUN 8 DAY 1	TIME PERIOD 1430	TO 1530	-	RUN 10 DAY 1 TIME PERIOD 1645 TO 1730
M.N. 0/P (HV)	67.4 62.2 33	.3 64.6		H.H. D/P (HV) 65.1 58.5 39.7 52.5
SPOT READINGS	67.7 (1.9 35)	0 62.6		S°UT READINGS 63.5 58.4 44.0 49.7
	AT(C) WT(C)	RH (2)	NR (HW/SOCH)	AT(C) WT(C) RH(Z) NR(MW/SQ
N.N. AVERAGES	30.6 26.3	33.3	77.3	N.M. AVERAGES 29.7 24.9 39.7 40.8
CURRENT SPOT READ. PREVIOUS SPOT READ.	30.7 26.2 30.4 26.4	35.0 38.0	71.2 83.6	CURRENT SPOT READ. 29.1 24.9 44.0 32.3 PREVIOUS SPOT READ. 30.0 25.2 37.6 48.3

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SPEED(H/S) É.R.ANEH(H/S) PYR(HW/SOCH) KIPP(HW/SOCH)

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2 48.2 40.7
8 54.0 36.8
WT(C) RH(Z) NR(MW/SQCM)
24.4 48.2 5.2
24.3 54.0 -6.6 24.9 44.0 32.3
•

SPEED(H/S)	E.R.ANEM(H/S)	PYR(MW/SQCM)	KIPP(MW/SQCM)
• 0	5.9	5.9	

RUN 12 DAY 1 TINE PERIOD 20 0 TO 2225

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H.H. DZP (HV)	47.4 56.6	59.8	36.2	
SPOT READINGS	41.5 36.2	70.0	36.3	
	AT(C)	WT(C)	RH (%)	NR (HW/SQCM)
M.M. AVERAGES	22.7	24.2	59.8	-8,5
CURRENT SPDT READ. PREVIOUS SPOT READ.	20.4 25.5	24.1 24.3	70.0 54.0	-8.1 -6.6

SPEED(H/S) E.R.ANEM(H/S) PYR(HW/SOCH) KIPP(HW/SOCH)

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DATE 30276 SERIES 1

RUN 3 DAY 1	TIME PERIO	931 TO 1030		RUN	5 DAY 1	TINE PERIOD	1130 TO 1230	
H.H. 0/P (HV)	53.4 58.8	42.5 63.1		н.н	. 0/P (HV)	0.3 64.0	41.2 69.0	
SPOT READINGS	56.6 61.2	40.0 66.3		S P O	T READINGS	66.3 65.2	29.0 70.3	
	AT(C)	₩T{C} RH{2)	NR (MW/SOCH)			AT(C)	WTEC) RHEZ3	NR (NV/SQCM)
H.H. AVERAGES	25.1	24.9 42.5	70.4	н.н	. AVERAGES	0.0	26.9 41.2	83.7
CURRENT SPOT READ. PREVIOUS SPOT READ.	26.4 24.6	25.9 40.0 24.9 44.0	80.2 67.6	CUR PREV	RENT SPOT READ. IOUS SPOT READ,	30.2 28.2	27.4 29.0 26.5 43.0	92.6 87.2
SPEED (M/S)	E.R.ANEH(M/	S} PYR(H¥/SQCH)	KIPP(MW/SQCM)		SPEED(M/S)	E.R.ANEM(M/S)	PYR (HW/SQCH)	KIPP(NW/SQCM)
1.1		60.2			2.1	• 4	, 0.0	

RUN 4 DAY 1	TIME PERIOD	0 1030 TO 1	130		RUN 6	DAY 1	TIME	PERIOD	1230 TO	1330	
H.N. O/P (NV)	58.5 61.9	41.3	56.0		₫.₫. 0/P	(XV)	66.0	66.2	33.6	70.0	
SPOT READINGS	61.3 63.0	43.0	68.5	1	SPOT REA	OINGS	71.3	68.2	23.0	69.1	
	AT (C)	WT(C)	RH (%)	NR (MW/SQCM)			AT.	(C)	NI(C)	RH (%)	NR EMW/SOCH)
M.M. AVERAGES	27.1	26.1	41.3	49.3	H.H. AVE	RAGES	3(0.1	27.7	33.6	91.6
CURRENT SPOT READ. PREVIOUS SPOT READ.	28.2 26.4	26.5 25.9	43.0 40.0	87•2 80•2	CURRENT PREVIDUS	SPOT READ. SPOT READ.	3	2.1 0.2	28.5 27.4	23.0 29.0	89.0 92.6

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SPEED(N/S) "F.R.INFM(M/C) DYDINUICOCHI MTDDINUICOCHI

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RUN 7 DAY 1	TIME PERIOD	1330 TD 1430		·	RUN 9 DAY 1	TIME PERIOD	1531 TO 1630	
N.N. D/P (NV)	73.9 69.4	26.4 68.3			M.M. 0/P (HV)	68.5 ز.72	32.7 29.6	
SPOT READINGS	72.3 69.0	23.0 67.1	l		SPOT READINGS	74.3 67.9	22.0 57.6	
	AT(C)	WT(C) RH() NR(MW/SQCM)			AT(C)	WT(C) RH(Z)	NR (MW/SQCM)
N.M. AVERAGES	33.2	29.0 26	4 86.3		M.M. AVERAGES	32.7	28.6 32.7	-29.3
CURRENT SPOT READ. PREVIOUS SPOT READ.	32.5 32.1	28.8 23 28.5 23	0 85.4 0 89.0		CURRENT SPOT READ. Previous spot read.	33.3 33.9	28.4 22.0 29.3 23.0	54.9 77.8
Speed (M/S)	E.R.ANEH(M/	5) PYR(HŴ/SQC	1) KIPP(MW/SQCM)		SPEED (M/S)	E.R.ANEM(M/S) PYR(MW/SOCH)	KIPP(HW/SOCH)
1.2		.6 222	0.	·	1.2	•	4 0.0	
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RUN 8 DAY 1	TIKE PERIO	D 1430 TO 1531		· · · ·	RUN 10 DAY 1	TIME PERIOD	1530 TO 1730	
M.H. 0/P (HV)	75.1 68.2	22.0 54.			M.M. 0/P (HV)	75.8 67.6	26.9 53.6	
SPOT READINGS	75.7 70.2	23.0 65.			SPUT READINGS	74.9 64.9	26.0 49.4	
	AT(C)	WT(C) RH(NR (MW/SQCM)			AT(C)	WT(C) RH(Z)	NR (MW/SQCM)
N.M. AVERAGES	33.6	28.5 22	.0 45.5		M.M. AVERAGES	33.9	28.3 26.9	42.8
CURRENT SPOT READ. PREVIOUS SPOT READ.	33.9 32.5	29.3 23 28.8 23	.0 77.8 .0 85.4		CURRENT SPOT READ. PREVIOUS SPOT READ.	33.6 33.3	27.3 26.0 28.4 22.0	30.2 54.9

SPEED(M/S) E.R.ANEM(M/S) PYR(MW/SQCH) KIPP(MW/SQCM)

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SPEED(H/S) É.R.ANEH(H/S) PYR(HW/SQCH) KIPP(HW/SQCH) 1.4 • 4 116.5

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RUN 11 DAY 1	TIME PERIO	D 1730 TO	13 5		RUN 13 DAY 1	TIME PERIC	10 1940 TO	2010	
H.H. 0/P (HV)	74.8 65.8	26.2	47.2		H.H. O/P (HV)	65. 63.3	33.6	35.5	
SPOT READINGS	72.3 66.0	30.0	43.8		SPOT READINGS	64.2 63.4	36.0	37.2	
	AT(C)	WT (C)	RH (Z)	NR (MW/SQCH)		AT (C)	WT(C)	RH (Z)	NR (NW/SOCH)
M.M. AVERAGES	33.5	27.6	26.2	23.4	M.M. AVERAGES	29.9	26.7	33.6	-12.2
CURRENT SPOT READ. PREVIOUS SPOT READ.	32.5 33.6	27.7 27.3	30.0 26.0	13.0 , 30.2	CURRENT SPOT READ. Previous Spot Read.	29.3 30.1	26.7 26.7	36.0 36.0	-6.9 -7.2
SPEED(N/S)	E.R.ANEM(H/	S) PYR(H	W/SQCH)	KIPP(HW/SQCM)	 SPEED(M/S)	E.R.ANEM(M	S) PYR	(MW/SQCH)	KIPP (NW/SQCK)
3.2		• 4	0.0	•	4.3		• 4	0.0	
	•								
RUN 12 DAY 1	TIME PERIO	D 18 5 TO	1940			•			
M.N. (1/P (MV)	70.8 65.2	31.6	39.3						
SPOT READINGS	66.0 63.5	36.0	37.1						
	AT(C)	WT(C)	RH (Z)	NR (MW/SQCH)	к				
M.N. AVERAGES	31,9	27.4	31.6	5					
CURRENT SPOT READ. PREVIOUS SPOT READ.	30.1 32.5	26.7 27.7	36.0 30.0	-7.2 13.0					

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SPEED(M/S) "E.R.ANEH(H/S) PYR(HW/SQCH) KIPP(HW/SQCH)

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DATE 50276 SERIES 2

RUN 3 DAY 1	TIME PERIOD	75TO.	8 0			RUN 5	DAY 1	TIN	PERIOD	9 O TO	10 0	
N.H. 0/P (HV)	26.6 57.3	65.5	45.8			M.M. D	/P (MV)	0.0	0.0	0.0	0.0	
SPOT READINGS	29.5 57.5	60.0	50.7		· · ·	SPOT R	EADINGS	41.5	58.6	43.0	64.4	
	AT(C)	WT(C)	RH (%)	NR (MW/SQCM)	•			A	r(c)	WT(C)	RH (Z)	NR (HW/SQCH)
M.M. AVERAGES	18.1	24.3	65.5	18.5		M.M. A	VERAGES		0.0	0.0	0.0	0.0
CURRENT SPOT READ. PREVIOUS SPOT READ.	19.3 17.3	24.4 24.4	60.0 65.0	33.8 13.0		-CURREN PREVIOU	T SPOT READ. S SPOT READ.		24.3 21.9	24.8 24.6	43.0 50.0	75.4 57.0
SPEED(M/S)	E.R.ANEH(H/S) PYR(H	(/SQCM)	KIPP(MW/SQCM)	•		SPEED(M/S)	E.R.	ANEM(M/S)	PYR (HW/SQCH)	KIPP(HW/SQCM)
3.0	2.	9	32.3		T		3.5	i	3.7	ı	88.8	
RUN 4 DAY 1	TIHE PERIOD	8 0 TO	90		•	RUN 6	DAY 1	TIM	E PERIOD	10 O TO	11 0	
M.M. 0/P (MV)	32.0 57.7	55.3	0.0		. •	H.H. 0	/P (HV)	44.2	59.3	41.6	59.4	
SPOT READINGS	35.7 57.9	50.0	58.3		• *.	SPOT R	EADINGS	46.2	61.5	39.0	67.4	
	AT(C)	WT(C)	RH (🎗)	NR (HW/SQCH)	·			A	т(с)	WT(C)	RH (%)	NR (MW/SQCM)
M.H. AVERAGES	20.3	24.5	55.3	0.0		M.M. A	VERAGES		25.4	25.1	41.6	59.5
CURRENT SPOT READ. PREVIOUS SPOT READ.	21.9 19.3	24.6 24.4	50.0 60.0	57.0 33.8	•	CURREN PREVIOU	T SPOT READ. S SPOT READ.	•	26.2	25.9 24.9	39.0 43.0	84.8 75.4
SPEED(M/S)	E.R.ANEH(N/S) PYR(HV	(/SQCH)	KIPP(MW/SQCM)	•		5.0FED/M/51	F.9	ANF#/#/51	D Y D I	Накорен	****
2.2	2.	4	44.4		•		1.6)	1.0)	93.7	NET FILEFORDUCTI

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RUN 7 DAY 1	TIME PERIOD	11 0 TO 1	2 0	·			RUN 9 DAY 1	TIME PERIOD	13 0 TO 14 0	
H.H. 0/P (MY)	47.8 62.6	40.2	58.1				H.H. O/P (HY)	58.~ 67.6	25.7 69.6	
SPOT READINGS	50.6 64.1	35.0	69.3	ι.			SPOT READINGS	59.8 65.3	20.2 67.0	
	AT(C)	WT(C)	RH (X)	NR (HW/SQCH)				AT(C)	WT(C) RH(X)	NR (MW/SQCH)
M.H. AVERAGES	26.9	26.3	40.2	56.9			M+N+ AVERAGES	31.2	28.2 25.7	92.6
CURRENT SPOT READ. PREVIOUS SPOT READ.	28.0 26.2	26.9 25.9	35.0 39.0	90.5 64.8			CURRENT SPOT READ. PREVIOUS SPOT READ.	31.6 30.0	27.7 20.2 27.1 27.8	84*8 91*4
SPEED(M/S)	E.R.ANEM(M/S	I) PYRCHŴ	(SOCH)	KIPP(HW/SQCH)	,		SPEED(M/S)	E.R.ANEM(M/S)	PYR (NW/SQCH)	KIPP(HW/SOCH
1.4	1.	.6	93.7	·		•	1.5	1.9	2 103.6	
Рим в пам 1	TINE OFFICE	13 0 70 1	3 0				RUN 10 DAY 1		16 0 70 1610	
	TTHE FERIOD		30	•	•					
H.H. D/P (HV)	50.5 62.9	34.6	68.4				H.H. 0/P (HV)	59.5 66.6	22.8 51.2	
SPOT READINGS	55.6 64.7	27.8	69.2	•		. /	SPOT READINGS	58.2 64.8	29.0 62.7	
	ATICI	WT(C)	RH(2)	NR (NW/SQCH)				AT(C)	WT(C) RH(Z)	NR (HW/SOCH)
M.M. AVERAGES	28.0	26.4	34.6	88.6			M.M. AVERAGES	31.5	27.8 22.8	36.8
CURRENT SPOT READ.	30.0	27.1	27.8	91.4		*	CURRENT SPOT READ. PREVIOUS SPOT READ.	31.0	27.1 29.0	70.9

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	RUN 11 DAY 1	TIME PERIOD 1510 T	D 16 O	f		RUN 13 DAY 1	TIME PERIOD	17 O TO 18 O	
-	N.M. D/P (NV) Spūt rēadings	58.2 63.9 24.4 58.0 62.4 20.0	59.5 58.1			M.M. D/P (MV) Spot readings	55.8 61.9 53.5 61.8	26.7 47.4 29.0 42.9	
		AT(C) WT(C)	RH (Z)	NR (MW/SQCM)			AT(C)	WT(C) RH(2)	NR (MW/SQCM)
	M.M. AVERAGES	31.0 26.8	24.4	61.2		H.H. AVERAGES	30.1	26.0 26.7	24.5
	CURRENT SPOT READ. PREVIOUS SPOT READ.	30.9 26.2 31.0 27.1	20.0 29.0	57.0 70.9		CURRENT SPOT READ. PREVIOUS SPOT READ.	29.1 30.7	26.0 29.0 26.1 20.7	10.9 35.3
>	SPEED(M/S)	E.R.ANEM(M/S) PYR	(HW)SOCH)	KIPP(HW/SQCM)	•	SPEED(M/S)	E.R.ANEM(M/S)	PYR(HW/SOCM)	KIPP(HW/SGCH)
	5.9	6.2	71.0		, 7	4.2	4.2	14.8	
	RUN 12 DAY 1	TIME PERIOD 16 O T	0 17 0			. RUN 14 DAY 1	TIME PERIOD	18 O TO 20 O	
	H.H. 0/P (HV)	56.5 61.1 23.9	54.2			H.H. D/P (HV)	49.3 61.9	40.7 39.4	
	SPOT READINGS	57.5 02.1 20.7	50.9		·	SPO; READINGS	41.6 61.2	51.5 36.2	
		AT(C) WT(C)	RH (%)	NR (MW/SOCM)			AT(C)	NT(C) RH(Z)	NR (HW/SOCH)
	H.M. AVERAGES	4 30.3 25.8	23.9	45.3		H.M. AVERAGES	27.5	26.0 40.7	• 2
	CURRENT SPOT READ. PREVIOUS SPOT READ.	30.7 26.1 30.9 26.2	20.7 20.0	35.3 57.0	• •	CURRENT SPOT READ. PREVIOUS SPOT READ.	24.3 29.1	25.8 51.5 26.0 29.0	-9.4 10.9
	SPEED(M/S)	E.R.ANEM(M/S) PYR	(HW/SQCH)	KIPP(HW/SQCH)	· · · ·	SPEED(H/S)	E.R.ANEM(M/S)	PYR(MW/SQCM)	KIPP(HW/SOCM)
	5.2	5.5	59.2			2.2	2.4	0.0	
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RUN 15 DAY 1 TIME PERIOD 20 0 TO 23 0

N.N. D/P (NV)	39.2 60.8	53.3	36.5	
SPOT READINGS	35.3 60.3	52.0	36.0	
	AT(C)	WT (C)	RH (%) .	NR (HW/SQCH)
M.N. AVERAGES	23,3	25.6	53.3	-8.6
CURRENT SPOT READ. PREVIOUS SPOT READ.	21.7	25.4 25.8	52.0 51.5	-10.3

SPEE	0(8/5)	E.R.ANEM(M/S)	PYR(HW/SQCH)	KIPP(HW/SQCH)
	2.9	2.8	0.0	

DATE 50476 SERIES 5

RUN 2 DAY 1	TIME PERIOD	830 TD 945			RUN 4 DAY 1	TIME PERIOD	11 7 TO 1235	
M.M. D/P (MV) Spot readings	9.9 47.7 17.9 48.4	69.5 50.9 70.0 54.5			M.M. O/P (MV) SPOT READINGS	34.5 47.4 40.9 51.5	55.6 53.4 50.0 58.8	
	AT(C)	₩T(C) RH(%)	NR (HW/SQCH)			AT(C)	WT(C) RH(%)	NR (HW/SQCH)
M.M. AVERAGES	14.5	21.3 69.9	5 33.8		M.M. AVERAGES	19.5	21.2 55.6	56.3
CURRENT SPOT READ. PREVIOUS SPOT READ.	16.1 14.0	21.3 70.0 21.2 71.0	0 44.3 0 21.7		CURRENT SPOT READ. Previous spot read.	20.7 18.5	21.8 50.0 21.5 57.0	57.6 53.8
SPEED(M/S)	E.R.ANEM(H/S) PYR(HW/SQCH) KIPP(HW/SQCM)	· ·	SPEED(M/S)	E.R.ANEH(M/S)	PYR (MW/SQCH)	KIPP(HW/SQCH)
3.4	3.	6 47.4	4 61.6		3.9	4.0	70.6	63.1
RUN 3 DAY 1	TIME PERIOD	945 TO 11 7	•		RUN 5 DAY 1	TIME PERIOD	1235 TO 1430	
H.H. D/P (HV)	23.8 48.8	62.2 57.3			H.M. 0/P (HV)	45.6 48.6	48.8 54.9	
SPOT READINGS	31.0 49.4	57.0 59.2	•		SPOT READINGS	34.7 53.1	43.0 52.7	
	AT(C)	WT(C) RH(Z)	NR(MW/SQCM)			AT(C)	WT(C) RH(Z)	NR (MW/SQCM)

M.H. AVERAGES

CURRENT SPOT READ. PREVIOUS SPOT READ. 21.7

19.5 20.7

2.4

1

21.4

22.0 21.8

SPEED(M/S) E.R.ANEH(H/S) PYR(MW/SOCH) KIPP(MW/SOCH)

2.5

48.8

43.0 50.6

54.1

46.0

39.5 57.6

55.5

M.M. AVERAGES	17.3	21.4	62.2	53.1
CURRENT SPOT READ.	18.8	21.5	57.0	58.8
PREVIOUS SPOT READ.	16.1	21.3	70.0	44.3
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 SPEED(M/S)
 E.R.ANEM(M/S)
 PYR(MW/SQCM)
 KIPP(MW/SQCM)

 4.2
 4.3
 65.0
 75.5

	RUN 6 DAY 1	TIME PERIOD 1430 T	0 1530			•	RUN 8 DAY 1	TIME PERIOD	1631 TO 1835	
	N.N. D/P (NV) Spot readings	50.9 0.0 43.7 54.0 52.7 45.0	, 0.0 49.6				M.M. D/P (MV) Spot readings	45.9 51.3 28.5 50.2	55.1 37 73.0 36	•9
		AT(C) WT(C)	RH(%)	NR (HW/SOCH)		·		AT(C)	NT(C) RH	(X) NR(N¥/SQCK)
	N.M. AVERAGES	22.8 0.0	43.7	0.0			M.M. AVERAGES	21.8	21.7 5	5.1 -5.1
	CURRENT SPOT READ. Previous spot read.	23.4 21.9 19.5 22.0	45.0 43.0	30.2 39.5	. •		CURRENT SPOT READ. PREVIOUS SPOT READ.	18.2	21.6 7 21.9 4	3.0 -9.7 6.0 9.7
Al	SPEED (M/S)	E.R.ANEN(M/S) PYR	(HW/SQCM)	KIPP(MW/SQCN)		•	SPEED (H/S)	E.R.ANEM(M/S) PYR(MW/SQ	CH) KIPP(HW/SQCH)
. 12	2.5	2.7	29.6	42.7			2.0	2.	0	7.2 0.0
						• • •				
		,				÷				
1	RUN 7 DAY 1	TIME PERIOD 1530 T	0 1631	•			RUN 9 DAY 1	TIME PERIOD	1835 TO 20 O	
	N.H. D/P (HV)	54.6 51.8 43.2	45.1			•	M.M. C/P (MV)	24.1 49.1	71.8 36	•1
	SPOT READINGS	55.5 52.3 46.0	42.8	:		in and a second s	SPOT READINGS	17.4 49.4	78.0 36	•0
	·	AT(C) WT(C)	RH (\$ }	NR (MW/SQCM)		•		AT(C)	WT(C) RH	(Z) NR (NW/SQCM)
	H.H. AVERAGES	23.5 21.B	43.2	16.7			H.H. AVERAGES	17.4	21.4 7	1.8 -10.6
	CURRENT SPOT READ Previdus spot read.	· 23.7 21.9 · 23.4 21.9	46.0 45.0	9.7 30.2		•	CURRENT SPOT READ. PREVIOUS SPOT READ.	16.0 18.2	21.5 7 21.6 7	8.0 -10.9 3.0 -9.7

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RUN 10 DAY 1	TIME PERIO	0 20 0 TO 2130		I = 1		RUN 12 DAY 1	TIME PERIOD	23 5 TO 125	
M.M. D/P (MV) SPOT READINGS	15.2 48.4 13.2 49.1	77.8 35 79.0 35	.2 .8	•.		M.M. D/P (MV) Spot readings	0.9 0.0 18.2 47.7	0.0 0.0 62.0 35.4	
	AT(C)	WT(C) RH	(2)	NR (HW/SQCH)			AT (C)	WT(C) RH(Z)	NR (MW/SOCH)
N.M. AVERAGES	15.6	21.3 7	7.8	-13.4		M.M. AVERAGES	0.0	0.0 0.0	0.0
CURRENT SPOT READ. PREVIOUS SPOT READ.	15.2	21.4 7 21.5 7	9.0 8.0	-11.5		CURRENT SPOT READ. PREVIOUS SPOT READ.	16.2 15.3	21.3 62.0 21.6 81.0	-12.1 -9.7
SPEED(M/S)	E.R.ANEM(M/	S) PYR(MW/SC	сн) к	IPP(HW/SQCM)	•	SPEED (M/S)	E.R.ANEH(M/S)	PYR (HW/SQCM)	KIPP(HW/SQCH)
1.6	. 1	• 6	0.0	0.0		3.6	3.:	5 0.0	0.0
							·		
RUN 11 DAY 1	TIME PERIO	D 2130 TC 23 5	i			RUN 13 DAY 2	TIME PERIDO	125 TO 3 O	
M.N. 0/P (HV)	12.8 47.7	78.3 34	.8			M.M. 0/P (HV)	0.0 0.0	0.0 0.0	
SPOT READINGS	13.9 50.0	81.0 36	.2			SPOT READINGS	10.9 47.5	76.0 35.7	
	AT(C)	WT(C) RH	(%)	NR (HW/SOCH)			AT(C)	WT(C) RH(Z)	NR (NW/SQCH)
M.M. AVERAGES	15.1	21.3	8.3	-14.2		H.M. AVERAGES	0.0	0.0 0.0	0.0
CURRENT SPOT READ. PREVIOUS SPOT READ.	15.3 15.2	21.6 21.4	1.0	-9.7 -11.5	· .	CURRENT SPOT READ. Previous spot read.	14.7 16.2	21.2 21.3 62.0	-11.2 -12.1
SPEED(H/S)	E.R.ANEM(M/	S) PYR(HW/S)		(IPP(HW/SOCH)		SPEED(H/S)	E.R.ANEM(H/S)	PYR (HW/SQCH)	KIPP(HW/Sach)
3.0	2	•6	0.0	0.0		2.6	. 2.5	0.0	0.0

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Time	Speed (m/s)	A.Temp (°C)	W.Temp (°C)	R.H. (%)	N.Rad (mW/ag cm)		m /					
		-		-			Time	Speed (m/a)	A. Temp (°C)	W. Terp	R.H.	H.Rad
150176 .					a.				,	(-0)	(4)	(my/sq cm)
32	1 50	10.00	22 10	(,	030374					
8 0	1.50	18.00	23.40	03.00	. 30.00	•	030210					
0.0	1.00	20 40	23.20	61.00	47.00							
9 0	1.20	20.00	23.10	01.00	00.00		0 7	+80	24.00	24.40	44.00	53.00
430	1.50	21.70	23.02	/ 30.30	09.50		420	.80	24.70	24.90	42.50	67.00
10 0	1.20	22.50	24.05	57.00	10.00		. 10 0	1.10	25.10	25,35	42.50	75.00
17 0	1.50	23.00	64+37	24.20	02.90		1030	1.50	26.20	25.90	42.50	81.00
1120	1.50	24.70	24.15	51.30	87.00		11 0	1.80	27.10	26.10	42.00	20.00
1120	1 50	22.70	27.50	40.00	· 90.50		1130	2.10	28.20	26.50	41.50	67.00
12 0	1.50	20.10	20.05	41.00	92.00		12 0	2.10	29.30	26.85	40.60	91.00
1230	1.50	27.50	20.20	39.00	93.00		1230	2.10	30.30	27.30	38.80	93.00
13 0	1.50	28.30	26.25	38.00	92.00		. 13 0	1.65	31.30	27.65	34.00	91.00
1330	1.50	29.00	26.30	36.60	89.00		1330	1.30	32.40	28.50	29.50	90.00
14 0	3.30	29.80	25.32	35.50	86.50		14 0	1.10	33.30	29.20	26.00	\$5.00
1430	2.20	30.40	26.33	34.90	83.50		1430	1.20	34.00	28.80	23.00	85.00
15 0	2.30	30.70	26.30	34.50	77.00		15 0	1.50	33.60	28.00	20.00	10.00
1530	3.90	30.50	26.24	35.00	71.00		1530	1.30	33.00	28.80	30.00	78.00
1545	6.00	30.40	26.00	36.00	67.00		16 0	1.20	32.30	25.80	35.00	63.00
16 0	6.00	30.25	25.80	36.50	63.00		1630	1.60	33.30	28.35	30.00	55.00
1630	6.03	30.00	25.36	38.20	52.00		· 17 0	2.40	34.20	28.00	27.00	44.00
17 0	4.80	29.75	24.95	39,80	42.00		1730	3.00	33.90	27.80	26.00	31.00
1730	5.70	29.40	24.66	42.40	32.00		• 18 0	4.60	32.90	27.60	29.00	17.00
18 0	5.75	28.80	24.52	45.00	20.00		1815	5.00	32.60	27.50	30.05	9.00
1530	5.84	28.20	24.41	47.50	8.00		1830	5.00	32.30	27.40	31,50	3.00
19 0	5.90	27.50	24.35	50.00	-2.50		19 0	5.00	31.60	27.20	32.00	-2.00
1930	5.99	26.40	24.31	52.20	-6.00		1930	5.00	31.00	27.00	32.60	-4.50
20 0	6.10	25.50	24.28	54.40	-7.50		- 20 0	4.30	30.10	26.80	33.00	-6.03
2030	6.14	24.40	24.25	56.60	-8,00		2030	3.60	29.20	26.60	34.00	-6.00
21 0	6.20	23.30	24.24	59.00	-8.50		•					~ ~ ~ ~ ~
2130	6.26	22.20	24.30	61.50	-8.50	•						
22 0	6.35	21.20	24.18	63.50	-8.50	•		÷				
Z230	6.30	20.10	24.14	65.30	-8.50							
23 0	6 36	10 10	74 00	47 60								

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Tim	e Speed (m/s)	А. Тетр (⁰ С)	W.Temp (°C)	R.n. (2)	N.Rad (mW/sq cm)	Time	Speed (m/s)	А.Тетр (⁰ С)	W.Temp (^D C)	R.H. (Z)	N.Rad (mW/sq cm)
050276						050476					
41						37					
630	0 2.30	16.80	24.30	70.00	0.00	830	3.60	13.80	21.20	71.50	22.00
7 (2.80	17.30	24.30	68.00	11.00	9 0	3.30	14.40	21.25	70.00	32.50
730	3.00	18.40	24.30	64.50	23.00	930	3.30	15.20	21.28	68.50	41.00
8 (3.20	19.40	24.35	60.00	35.00	10 0	4.30	10.00	21:33	65.50	48.50
830	1.80	20.80	24.40	55.00	47.00	1030	4.30	17.00	21.40	50 50	53.20
9 (2.20	22.00	24.50	50.00	58.00	11 0	4.10	10.00	21.45	59.50	57.00
91	5 4.50	22.65	24.53	48.50	63.00	1130	4.00	19.20	21.53	57.00	59,00
93	3.50	23.30	24.58	46.50	67.00	12 0	3.90	19.70	21.00	55.00	59.50
10 0	0 3.40	24.40	24.75	43.50	76.00	1230	3.15	20.30	21.07	53.00	57.00
103	0 1.10	25.40	25.00	41.50	82.00	1220	2.40	20.90	21.72	51.00	53.00
11 (0 1.10	26.30	25.50	40.50	86.00	1330	2.30	21.55	41.11	49.20	46.00
1130	0 1.40	27.20	26.10	40.00	89.00	14 0	2.20	22.00	21.80	47.50	42.30
12 0	1.70	28.10	26.70	38.50	91.00	11430	2.10	22.30	21.83	45.00	39.20
1230	•90	29.20	26.90	35.50	92.00	15 0	2.50	22.80	21.85	43.60	35.00
13 0	.90	30.20	27.70	29.50	91.50	1930	2.30	23.20	21.05	42.60	30.00
133	0 .90 5	31.20	28,10	25.50	89.50	16 0	2.20	23.70	21.05	42.00	20.00
134	5 3.30	31.33	28.30	24.50	88.00	1030	2.10	23.30	21.00	50.00	-3.00
142		31.70	28.40	23.00	88.00	1730	2.00	22.50	21.73	55.00	-5.00
145	5 4 0 0	31.60	20.00	22.50	36.00	18.0	1.95	20.80	21.67	59.50	-8.00
15 (31.30	20.10	22.50	78.90	1830	1.90	19.30	21.62	63.50	-9.30
151	5 3.30	33.2	27.20	23.00	73.50	19 0	1.90	17.90	21.53	68.00	-10.00
153	0 5.50	31.05	26.85	23.50	65.00	1930	1.90	16.90	21.45	73.00	-10.20
154	5 8.00	31.00	26.50	24.00	60.50	20 0	1.90	16.10	21.40	78.00	-10.20
16 (0.65	30.90	26.30	24.00	57.00	2030	1.50	15.70	21.35	78.00	-10,60
163	0 5.20	30-80	25,90	24.00	48.00	21 0	1.60	15.40	21.30	78.00	-11.20
17	0 4.70	30.70	26.00	25.00	36.00	2130	1.60	15.30	21.28	78.00	-11.00
173	u 4.20	30.20	26.00	27.00	24.00	22 0	3.00	15.25	21.27	78.30	-11.00
18	0 3.70	29.40	28.00	31.00	12.00	2230	3.30	15.25	21.25	78.50	-11.00
163	0 3.35	28.60	26.00	37.00	2.00	23 0	3.60	15.25	21.24	78.70	-11.00
184	5 2.20	28.00	26.00	39.00	-1.50	2330	3.60	15.20	21.22	78.90	-11.00
19 (0 2.00	27.40	26.00	42.00	-3.00	24 0	3.60	15.10	21.21	79.00	-11.00
193	0 1.65	26.30	26.00	46.00	-7.00	030	3.60	15.05	21.20	79.00	-11.00
20 (0 1.30	25.40	25.85	50.00	-9.00	1 0	3.60	15.00	21.20	79.00	-11.00
203	0 1.80	24.60	25.75	51.50	-9.00	130	3.60	15.00	21.20	79.00	-11.00
21 (0 2.35	24.00	25.68	53.00	-9.00	2 0	2.30	14.95	21.18	79.00	-11.00
213	0 2.90	23.30	25.60	54.00	-9.00	230	2.30	14.93	21.18	79.00	-11.00
22 (0 3.30	22.70	25.50	54.50	-9.00						
223	0 3.70	22.20	25.45	54.50	-9.00						
23	0 3.70	21.70	25.35	55.00	-9.00						
233	J 3.50	21.20	25.25	55.00	-9.30						

OATE	150176	SERIES	1
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RUN 1 DAY 1 TIHE 810	RUN 6 DAY 1 TIME 1400	RUN 11 DAY 1 TIME 2030
SOLN A SOLN B SALINITY 379. 529. CONDUCTIVITY 5 25C 734.2 925.5 SALINITY = .784*COND 25 + -196.6	SOLN A SOLN B SALINITY 379. 529. CONDUCTIVITY 5 29C 841.6 1097.4 SALINITY .586*COND 25 + -114.4 -114.4	SOLN A SOLN 8 SALINITY 379. 529. CONDUCTIVITY 5 25C 815.3 1068.2 SALINITY = .593*COND 25 + -104.4 541000000000000000000000000000000000000
BUCKET TEMP .04C PROBE THERMISTOR 12.79C	BUCKET TEMP 27.44C PROBE THERMISTOR 27.36C	BUCKET TEMP 24.04C PROBE THERMISTOR 23.93C
RUN Z DAY 1 TIME 900	RUN 7 DAY 1 TIME 1500	RUN 12 DAY 1 TIME 2230
SOLN A SOLN B SALINITY 379. 529. CONDUCTIVITY 5 25C 756.8 1028.0 SALINITY .553*COND 25 + -39.5 -39.5	SOLN A SOLN B SALINITY 379. 529. CONDUCTIVITY 5 25C 827.6 1080.1 SALINITY = .594*COND 25 + -112.6 500.1	SOLN A SOLN B SALINITY 379. 529. CONDUCTIVITY \$ 25C 808.1 1055.6 SALINITY • .606*COND 25 + ~110.8 1055.6
BUCKET TEMP 23.54C PROBE THERMISTOR 17.80C	BUCKET TEMP 26.64C PROBE THERMISTOR 26.47C	BUCKET TEHP 23.74C PROBE THERMISTOR 23.58C
RUN 3 DAY 1 TIME 1000	RUN 8 DAY 1 TIME 1600	
SOLN A SOLN B SALINITY 379. 529. CONDUCTIVITY 5 25C 826.3 1077.3 SALINITY597+COND 25 + -114.7	SOLN A SOLN B SALINITY 379. 529. CONDUCTIVITY ≤ 25C 831.2 1086.3 SALINITY = .588*CON9 25 + -109.9	
BUCKET TEMP 24.44C PROBE THERMISTOR 24.28C	BUCKET TEMP 25.64C PROBE THERMISTOR 25.50C	
RUN 4 DAY 1 TIME 1100	RUN 9 DAY 1 TIME 1700	
SOLN A SOLN B SALINITY 379. 529. CONDUCTIVITY 5 25C 825.5 1073.8 SALINITY604+COND 25 + -119.7	SOLN A SOLN 8 SALINITY 379. 529. CONDUCTIVITY 5 25C 816.9 1078.4 SALINITY = .574*COND 25 + -89.5 -89.5	
BUCKET TEMP 25.44C PROBE THERMISTOR 25.19C	BUCKET TEMP 24.94C PROBE THERMISTOR 24.94C	
RUN 5 DAY 1 TIME 1210	RUN 10 DAY 1 TIME 1800	
SOLN A SOLN 8 SALINITY 379. 529. CONDUCTIVITY 5 25C 822.5 1075.7 SALINITY = .593+COND 25 + -108.4	SOLN A SOLN B SALINITY 379. 529. CONDUCTIVITY 5 25C 817.9 1070.7 SALINITY = .593*COND 25 + -106.4	

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DATE 30276 SERIES 1

RUN 1 DAY 1 TIME 910		RUN 6 DAY 1 TIME 1405		RUN 12 DAY 1 TIME 2000
SOLN A	SOLN B	SOLN A	SOLN B	SOLN A SOLN
SALINITY 402.	500.	SALINITY 402.	500.	SALINITY 402. 500
CONDUCTIVITY 5 25C 774.2	952.3	CONDUCTIVITY 5 25C 775.4	951.8	CONDUCTIVITY \$ 25C 772.4 946.
SALINITY550+C.OND 25 + -23.8		SALINITY = .556*COND 25 + -28.8		SALINITY = .563*COND 25 + -33.2
BUCKET TEMP 24.65C PROBE THERMIS	TOR 24.61C	BUCKET TEMP 28.05C PROBE THERE	131UK 20.00C	BOCKET TENP 20133C PROBE THERRISTOR 2013
RUN Z DAY I TIME 955		RUN 7 DAY 1 TIME 1500		
SOLN A	SOLN B	SOLN A	SOLN B	
SALINITY 402.	500.	SALINITY 402.	500.	
CBR0UCTIVITY ≤ 25C 775.0	951.7	CONDUCTIVITY ≤ 25C 772.0	948.9	
SALINITY555+COND 25 + -27.8		SALINITY = .554*COND 25 + -25.7		
BUCKET TENP 25.350 PROBE THERMIS	TOR 25.290	BUCKET TEMP 27.35C PROBE THERE	11STOR 27.31C	
NOR D DET I TIME IIOS				
SOLN A	SOLN B	SOLN A	SOLN B	
SALINITY 402.	500.	SALINITY 402.	500.	
CONDUCTIVITY \$ 25C 774.7	959.3	CONDUCTIVITY 5 25C 774.5	951.9	
SALINITY = .531+COND 25 + -9.3		SALINITY = .553*COND 25 + -25.9		
BUCKET TEMP 26.05C PROBE THERMIS	TOR 25.99C	BUCKET TEMP 28.75C PROBE THER	MISTOR 28.87C	
RUN 4 DAY 1 TIME 1200		RUN 9 DAY 1 TIME 1700		
SOLN A	SOLN B	SOLN A	SOLN B	
SALINITY 402.	500.	SALINITY 402.	500.	
CONDUCTIVITY 5 25C 771.4	937.4	CONDUCTIVITY \$ 25C 765.5	946.0	
SALINITY = .590*COND 25 + -53.4		SALINITY = .543*COND 25 + -13.7		
BUCKET TEMP 26.95C PROBE THERMIS	TOR 26.90C	BUCKET TEMP 26.90C PROBE THER	MISTOR 26.99C	
RUN 5 DAY 1 TIHE 1300		RUN 10 DAY 1 TIHE 1800		
SOLN A	SOLN B	SOLN A	SOLN B	
SALINITY 402.	500.	SALINITY 402.	500.	
CONDUCTIVITY \$ 25C 0.0	1038.7	CONDUCTIVITY \$ 25C 770.9	942.9	
SALINITY = .094*COND 25 + 402.0		SALINITY = .569+COND 25 + -37.0		
BUCKET TEMP 27.650 PROBE THERMIS	TOR 24.300	RUCKET TENP 27.45C PROBE THEP	MISTOR 27.470	

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SALINITY Conductivity 5 25C Salinity • .555*Con	DLN A 402. 773.4 D 25 + -27.9	SOLN B 500. 949.7	SOLN A SCLN B SOLN A SOLN A	N B 30. 2.7
BUCKET TEMP 23.85C	PROBE THERMISTO	IR 23.83C	BUCKET TEMP 26.0DC PROBE THERMISTOR 26.22C BUCKET TEMP 25.95C PROBE THERMISTOR 25.	.95C
RUN 2 DAY 1	TIME 730		RUN 7 DAY 1 TIME 1230 RUN 12 DAY 1 TIME 1730	
SALINITY CONDUCTIVITY ≰ 25C SALINITY = •555*CON	DLN A 402. 776.6 D 25 + -28.7	SOLN B 500. 953.4	SOLN A SOLN B SOLN A SOLN B SALINITY 402. 500. SALINITY 402. 50 CONDUCTIVITY ≤ 25C 786.9 957.4 CONDUCTIVITY ≤ 25C 778.5 953 SALINITY •.575*COND 25 + -50.1 SALINITY = .561*COND 25 + -34.5 54.5	N B DO. 3.2
BUCKET TEMP 23.90C	PROBE THERMISTO	IR 23.83C	BUCKET TEMP 26.BDC PROBE THERMISTOR 26.78C BUCKET TEMP 25.95C PROBE THERMISTOR 25.	.88C
RUN 3 DAY 1	TIME 830		RUN 8 DAY 1 TIME 1326 RUN 14 DAY 1 TIME 2010	
SALINITY Conductivity ≤ 25C Salinity ● .560*Con	OLN A 402. 778.0 D 25 + -34.0	SOLN B 500. 952.8	SOLN A SOLN B SOLN A SOLN A	N B DO. 2.5
BUCKET TEMP 24.70C	PROBE THERMISTO	IR 24.60C	BUCKET TEMP 27.80C PROBE THERMISTOR 27.76C BUCKET TEMP 25.70C PROBE THERMISTOR 25.	•22C
RUN 6 DAY 1	TIME 930		RUN 9 DAY 1 TIME 1430 RUN 15 DAY 1 TIME 2310	
SALINITY Conductivity 5 25C Salinity = .553*Con	DLN A 402. 776.0 D 25 + -26.8	SOLN B 500. 953.4	SOLN A SOLN B SOLN A SOL SALINITY 402. 500. SALINITY 402. 50 CONDUCTIVITY \$ 25C 776.3 953.5 CONDUCTIVITY \$ 25C 776.7 956 SALINITY = .553*COND 25 + -27.2 SALINITY = .545*COND 25 + -21.6	Х В Со. 6.4
BUCKET TEMP 24.BDC	PROBE THERMISTO	IR 24.64C	BUCKET TEMP 28.60C PROBE THERMISTOR 28.56C BUCKET TEMP 25.1DC PROBE THERMISTOR 24.	•94C
RUN 5 DAY 1	TIME 1030	,e	RUN 10 DAY 1 TIME 1530	
SALINITY Conductivity 5 25C SALÍNITY = .56D+CON	DLN A 402. 778.7 1D 25 + -33.8	SOLN 8 500. 953.8	SOLN A SOLN 8 SALINITY 402. 500. CONDUCTIVITY ≤ 25C 776.7 951.7 SALINITY = .560'COND 25 + -32.9	

DATE 50276 SERIES 2 • . . •

TIME

DAY 1

RUN 1

630

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RUN 6

DAY 1

TIME 1130

RUN 11

DAY 1

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TIME 1630

DATE 50476 SERIES 5

TIME 1845 GAY 1 TIME 930 RUN B DAY 1 RUN 1 SOLN A SOLN B SOLN B SOLN A 402. 500. 500. SALINITY SALINITY 402. CONDUCTIVITY \$ 25C 764.8 940.3 CONDUCTIVITY \$ 250 759.3 936.0 SALINITY - .558+COND 25 + -25.0 SALINITY - .555+COND 25 + -19.3 PROBE THERMISTOR 21.35C BUCKET TEMP 21.30C BUCKET TEMP 21.15C PROBE THERMISTOR 21.01C RUN 9 DAY 1 **TIME 2030** RUN 2 DAY 1 TIME 1030 SOLN B SOLN B SOLN A SOLN A 500. 402. SALINITY SALINITY 402. 500. CONDUCTIVITY \$ 250 764.8 940.3 CONDUCTIVITY \$ 250 759.7 933.2 SALINITY = .558*COND 25 + -25.0 SALINITY = .565*COND 25 + -27.0 PROBE THERMISTOR 21.06C BUCKET TEMP 21.00C BUCKET TEMP 21.15C PROBE THERMISTOR 21.08C TIME 2200 RUN 10 DAY 1 RUN 4 DAY 1 **TIME 1400** SOLN A SOLN B SOLN B SOLN A SALINITY 402. 560. SALINITY 402. 500. CONDUCTIVITY \$ 250 939.5 CONDUCTIVITY \$ 250 764.8 940.3 765.9 SALINITY = .565+COND 25 + -30.4 SALINITY = .558*COND 25 + -25.0 PROBE THERMISTOR 21.16C BUCKET TEMP 21.60C PROBE THERMISTOR 21.79C BUCKET TEMP 21.00C DAY 1 TIME 2350 RUN 6 DAY 1 TIHE 1500 RUN 11 SOLN A SOLN B SOLN B SOLN A 500. 500. SALINITY 402. SALINITY 402. 940.3 CONDUCTIVITY 5 25C 937.3 CONDUCTIVITY 5 25C 764.8 765.1 SALINITY = .558*COND 25 + -25.0 SALINITY . .569*COND 25 + -33.4 PROBE THERMISTOR 21.05C BUCKET TEMP 21.70C PROBE THERMISTOR 21.82C BUCKET TEMP 20.85C **RUN 12** DAY 2 TIME 200 RUN 7 DAY 1 TIME 1600 SOLN B SOLN A SOLN B SOLN A 500. SALINITY 402. 500. SALINITY 402. 940.3 937.4 CONDUCTIVITY 5 25C 764.B CONDUCTIVITY ≤ 25C 764.1 SALINITY = .558 COND 25 + -25.0 SALINITY = .565+COND 25 + -30.0 BUCKET TEMP 21.65C PROBE THERMISTOR 21.81C BUCKET TEMP 20.50C PROBE THERMISTOR 20.67C

TIME 810	TIHE 1000			TIME 1210			•	
0.0	23.13	426:9	0.0	24.06	454.2	0.0	26.16	459.4
.2	23.15	425.9	• 2	24.02	454.6	• 2	25.14	458.0
. 4	23.15	424.3	• 4	23.65	454.7	• 4	24.35	459.6
•6	23.14	422.7	• 6	23.51	454.2	• 6	23.98	459.1
. 8	23.14	421.9	. 8	23.42	454.5	• 8	23.78	457.9
1.0	23.14	421.2	1.0	23.38	454.3	1.0	23.68	457.2
1.2	23.14	420.3	1.4	23.28	454.0	1.4	23.51	457.0
1.8	23.13	419.6	1.8	23.26	454.3	1.8	23.35	456.8
2.0	23.13	418.8	2.0	23.23	453.9	2.0	23.30	457.3
2.5	23.11	417.4	2.5	23.18	453.8	2.5	23.26	457.1
3.0	23.09	416.8	3.0	23.15	454.0	3.0	23.22	457.4
3.5	23.09	416.0	3.5	. 23.09	454.1	3.5	23.13	456.5
5.0	23.05	415.7	4.0	23.01	453.0	4.0	23.03	456.3
4.5	22.73	413.4	4.5	22.89	452.4	4.5	23.01	455.8
5.0	22.69	412.2	5.0	22.81	451.9	5.0	22.88	456.5
6.0	22.57	411.8	6.0	22.72	451.0	6.0	22.75	454.1
7.0	22.40	410.3	7.0	22.58	450.5	7.0	22.71	453.9
8-0	22.24	40H . B	8.0	22.40	450.4	8.0	22.40	452.1
9.0	22.00	408.2	9.0	22.23	448.3	9.0	22.43	450.2
10.0	21.59	410.1	10.0	22.10	447.2	10.0	22.10	450.7
11.0	19.37	445.8	11.0	21.26	452.6	11.0	21.59	453.9
12.0	16.76	524.5	12.0	19.49	678.6	12.0	19.66	476.9
1210	10110	52.05	1200	1,1,1,1	11010			
TIME 900		TINE	1100		TI	ME 1400		
0.0	23.38	452.0	0.0	26.60	452.7	0.0	26.01	448.2
	23.33	451.9		24.55	452.6	• 2	25.73	449.7
	23.30	451.7	. 4	24.32	454.9	. 4	24.79	452.3
. 6	23.28	451.3	. 6	23.98	453.3	.6	24.40	445.7
• B	23.26	450.3	. 6	23.72	454.0	.8	24.26	446.7
1.0	23.24	449.9	1.0	23.60	453.4	1.0	24.15	445.9
1.6	23.21	448.6	1.4	23.47	454.1	1.4	23.78	446.5
1.8	23.18	447.1	1.8	23.32	452.5	1.8	23.63	445.6
2.0	23.16	446.2	2.0	23.26	653.0	2.0	23.57	445.6
2.5	23.14	445.2	2.5	23.21	453.0	2.5	23.40	445.9
3.0	23.13	443.7	3.0	23 16	452.8	3.0	23.40	445.5
3.5	23.09	462.6	3.5	23.09	452.0	3.5	23.30	445.3
4.0	22.98	661.1	5.5	22.97	452 2	4.0	23.29	444.7
4.0	22.90	439.0	4.5	22 00	451 7	4.5	23.11	666.7
5.0	27 76	437.6	1.5	22.70	451.1	5.0	23.09	443.1
5.0	22.60	436 5	5.9	22.71	401.1	6.0	22.34	442.5
7 0	22 56	434.0	0.0	22.11	42U•4	7.0	22.77	442.0
1.0	22.30	12107	(•U	22.01	447.5	8.0	22.60	444 6
8.0	22.39	737.3	8.0	22.42	449.0	9.0	. 22.46	490.0
9.0	22.18	434.U	9.0	22.21	447.9	10.0	22.15	434.3
10.0	21.97	432.0	10.0	21.93	448.8	10.0	22.13	442.0

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15 01 76 SALINITY AND TEMPERATURE STRUCTURE

TEMPERATURE

DEPTH

SALINITY

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TIME 1500			TIME 1700			TIME 2030		
0.0	26.07	450.4	0.0	24.73	447.5	0.0	23.92	447.7
• 2	26.04	449.5	• 2	24.73	447.5	• 2	23.94	447.5
. 4	25.88	449.3	. 4	24.73	447.5	. 4	23.94	447.5
.6	25.34	450.8	• 6	24.72	447.5	• 6	23.94	448.1
. 8	24.55	448.3	• 8	24.71	447.7	• 8	23.94	447.5
1.0	24.27	446.7	1.0	24.70	447.7	1.0	23.94	447.5
1.4	23.98	446.5	1.4	24.67	448.0	1.4	23.94	447.5
1.8	23.73	447.1	1.8	24.56	447.9	1.8	23.92	447.7
2.0	23.68	447.0	2.0	24.31	447,3	2.0	23.94	440.1
2.5	·23.55	447.1	2.5	23.89	447.7	2.5	23.90	447.0
3.0	23.47	446.7	3.0	23.53	447.5	3.0	23.88	447.4
3.5	23.38	448.1	3.5	23.39	447.1	3.5	23.86	447.1
4.0	23.32	448.7	4.0	23.31	447.2	4.0	23.78	440.6
4.5	23.20	448.7	4.5	23.26	446.5	4.5	23.63	447.4
5.0	23.10	448.5	5.0	23.21	445.8	5.0	23.27	446.6
6.0	22.87	447.0	6.0	22.89	445.9	6.0	23.05	445.1
7.0	22.80	446.5	7.0	22.82	444.7	7.0	22.78	445.3
8.0	22.56	445.8	8.0	,22.60	444.4	8.0	22.53	444.5
9.0	22.44	444.5	9.0	22.44	442.9	9.0	22.25	4
10.0	22.17	444.0	10.0	22.17	443.1	10.0	21.96	444.6
11.0	21.68	446.4	11.0	21.57	447.0	11.0	20.85	455.7
12.0	19.43	477.2	12.0	19.66	473.0	12.0	18.80	495.1
TIME 1600			TIME 1800			TIME 2230		
0.0	25.27	445.7	0.0	24.30	447 7	0_0	23.74	450 9
• 2	25.27	445.7	.7	24.38	447.9	.2	23.77	450.5
. 4	25.26	445.2	. 4	24.38	447.6	. 4	23.50	451 0
. 6	25.19	445.9	. 6	24.34	447.6	. 6	23.80	451 0
. 8	25.09	445.1	. 8	24.34	447 6	. 8	23.80	451 0
1.0	25.09	445.7	1.0	24.35	447 5	1.0	23.79	451 1
1.4	24.32	444.1	1.4	24.24	444 6	1.4	23.79	450 6
1.8	23.92	444.3	1.8	24.20	447 7	1.6	23.80	451.0
2.0	23.84	443.9	2.0	24.23	467.6	2.0	23.79	451.1
2.5	23.69	444.1	2.5	23.97	447 5	2.5	23.78	4.61 1
3.0	23.60	443.6	3.0	23.73	447 4	3.0	23.79	451 1
3.5	23.44	444.2	3.5	23.40	446 3	3.5	23.76	450.7
4.0	23.34	443.3	4.0	23.25	446.5	4.0	23.65	450 6
4.5	23.22	443.3	4.5	23.17	446.1	4.5	23.55	450.3
5.0	23.13	442.9	5.0	23.04	446 1	5.0	23.14	450.5
6.0	22.94	442.3	6.0	22.84	445.7	6.0	22.72	440 1
7.0	22.01	441.7	7.0	22.81	445.3	7.0	22.51	460.7
8.0	22.60	440.8	8.0	22.61	444.8	8.0	22.36	448.3
9.0	22.44	439.8	9.0	22.43	444.0	9.0	22.04	463 3
10.0	22.22	439.5	10.0	22.10	446 2	10.0	21.86	448 7
11.0	21.76	441.0	11.0	21.59	447 3	11.0	21.35	440./
12.0	19.72	472.3	12.0	10.22	445 3	12.0	17 00	493.2
				17026		12.00	11470	269.1

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TIME 1500

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03 02 76 SALINITY AND TEMPERATURE STRUCTURE

TEMPERATURE

SALINITY

DEPTH

$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	TIME 910	TIME 1105				TIME 1300			
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $		36 60	155 0	0.0	26 02	468.3	0.0	27.50	486.9
$\frac{1}{10} = \frac{1}{24, 40} = \frac{1}{27, 5} = \frac{1}{10} = \frac{1}{25, 75} = \frac{1}{100, 77, 7} = \frac{1}{100, 77, 77, 7} = \frac{1}{100, 77, 77, 77, 7} = \frac{1}{100, 77, 77, 77, 7} = \frac$		24.49	458.0	.2	25.94	469-0	•2	26.92	487.0
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	* 2	24.49	457.9	. 4	25.75	468.7	• 4	26.03	488.C
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	••	26.48	459.8	.6	25.23	468.5	• 6	25.52	487.3
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		24.47	460.9	.8	25.08	468.3	• 8	25.41	486.7
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1.0	24.47	461.0	1.0	24.99	468.6	1.0	25.20	485.4
$\frac{2}{2}, 0$ 2	1.5	24.40	462.2	1.5	24.66	469.1	1.5	24.77	450.8
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.0	24.34	462.8	2.0	24.49	468.6	2.0	24.57	487.0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	24.32	463.5	2.5	24.43	468.7	2.5	24.54	405.9
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3.0	24.30	463.0	3.0	24.39	468.5	3.0	24.53	456.8
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3.5	24.29	464.4	3.5	24.33	468.5	3.5	24.51	400.0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4.0	24.22	464.5	4.0	24.32	468.1	4.0	24.46	486.8
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4.5	• 24.20	464.2	4.5	24.28	467.9	4.5	24.43	466.8
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	5.0	24.09	464.1	5.0	24.24	467.8	5.0	24.38	480.7
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	6.0	23.89	463.4	6.0	24.00	460.4	6.0	24.25	485.8
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	7.0	23.72	463.3	7.0	23.70	444.6	7.0	23.83	420.0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	8.0	23.67	462.8	8.0	23.56	426.4	8.0	23.76	450.4
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	9.0	23.41	463.1	9.0	23.46	465.1	9.0	23.20	486.5
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	10.0	23.31	463.5	10.0	23.38	457.6	10.0	23.29	100.1
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	11.0	22.55	472.5	11.0	22.98	462.6	11.0	22.01	467.2
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	12.0	21.62	488.2	12.0	21.89	479.3	12.0	21.28	971.2
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	13.0	19.70	562.0	13.0	18.76	573.6	13.0	19.20	JUZ . L
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	14.0	17.00	ó37.6	14.0	·		14.0		
TIME 955 TIME 1200 TIME 1405 0.0 25.20 468.8 0.0 26.75 477.7 0.0 28.01 466.6 .2 24.90 469.0 .2 26.59 477.6 .2 27.71 471.3 .4 24.82 469.2 .4 26.26 477.9 .4 26.46 468.4 .6 24.73 469.0 .6 25.67 477.3 .6 25.69 469.2 .8 24.66 469.7 .8 25.38 476.3 .8 25.63 469.2 1.5 24.52 470.0 1.5 24.85 476.6 1.5 25.02 469.9 2.0 24.55 469.6 2.0 24.55 475.8 2.0 24.66 469.7 2.5 24.38 469.7 2.5 24.66 469.7 459.2 455.3 475.8 2.0 24.66 469.7 2.5 24.34 469.5 3.5 24.42	15.0	16.11	658.5	15.0			15.0		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	TIKE 955		TIME	1200		Т	IME 1405		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.0	26.30	/ <u>4 0 0</u>	0.0	26.75	477.7	0.0	28.01	465.6
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.0	23.20	460.0	.2	26.59	477.6	•2	27.71	471.3
1.7 24.62 10.72 1.7 17.73 $.6$ 25.69 469.6 $.8$ 24.66 469.7 $.8$ 25.38 470.3 $.8$ 25.63 469.4 1.0 24.62 469.6 1.0 25.21 470.3 1.0 25.38 469.4 1.5 24.52 470.0 1.5 24.85 476.6 1.5 25.02 469.9 2.0 24.52 470.0 1.5 24.85 476.6 1.5 25.02 469.9 2.0 24.54 469.6 2.0 24.59 475.8 2.0 24.66 469.7 2.5 24.33 469.6 2.0 24.54 475.6 3.0 24.65 459.2 3.5 24.34 475.6 3.0 24.65 459.2 459.2 475.8 3.0 24.65 459.2 3.5 24.34 475.6 3.0 24.65 459.2 472.7 469.3 469.6 469.3 3.5 24.34 475.6 4.00 24.45 472.7 469.4 472.7 4.5 24.27 469.6 4.5 24.34 473.8 4.5 24.46 472.4 4.5 24.23 469.6 4.5 24.34 473.8 4.5 24.46 472.4 4.5 24.23 469.6 6.0 24.30 473.9 6.0 24.43 468.0 6.0 23.53 467.6 4.02 23.53 467.4 7.0 <td>• 2</td> <td>24.90</td> <td>469.0</td> <td>. 4</td> <td>26.28</td> <td>477.9</td> <td>• 4</td> <td>26.46</td> <td>468.4</td>	• 2	24.90	469.0	. 4	26.28	477.9	• 4	26.46	468.4
10 $21,12$ 100 10 $25,38$ $170,3$ 10 $25,63$ $469,4$ 1.0 $24,62$ $469,6$ 1.0 $25,21$ $476,3$ 1.0 $25,38$ $469,2$ 1.5 $24,62$ $469,6$ 1.0 $25,21$ $476,3$ 1.0 $25,38$ $469,2$ 1.5 $24,52$ $470,0$ 1.5 $24,65$ $476,6$ 1.5 $25,02$ $469,9$ 2.0 $24,45$ $469,6$ 2.0 $24,59$ $475,8$ 2.0 $24,66$ $469,7$ 2.5 $24,34$ $469,7$ 2.5 $24,54$ $475,7$ 2.5 $24,64$ $459,3$ 3.0 $24,37$ $469,7$ 2.5 $24,46$ $475,6$ 3.0 $24,65$ $459,2$ 3.5 $24,34$ $469,7$ 3.5 $24,42$ $475,8$ 3.5 $24,53$ $472,7$ 4.0 $24,27$ $469,7$ 3.5 $24,42$ $475,8$ 3.5 $24,49$ $472,7$ 4.0 $24,27$ $469,7$ 4.0 $24,49$ $472,7$ 4.0 $44,20$ $472,7$ 4.0 $24,27$ $469,7$ 5.0 $24,30$ $475,3$ 5.0 $24,49$ $472,2$ 5.0 $24,16$ $469,1$ 5.0 $24,30$ $475,3$ 5.0 $24,49$ $472,2$ 5.0 $24,16$ $469,1$ 5.0 $24,30$ $475,5$ 7.0 $23,20$ $469,6$ 6.0 $23,96$ $468,3$ 6.0 $23,79$ $473,5$ 7.0 $23,67$	• •	24.02	409.2	-6	25.67	477.3	• 6	25.89	469.6
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	• C	24613	409.0	.8	25,38	476.3	• 8	25.63	469.4
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1.0	24.62	407.1	1.0	25.21	476.3	1.0	25.38	469.2
2.0 24.65 469.6 2.0 24.59 475.8 2.0 24.66 469.7 2.5 24.38 469.7 2.5 24.54 475.7 2.5 24.64 459.3 3.0 24.37 469.2 3.6 24.46 476.6 3.0 24.65 459.2 3.5 24.34 469.5 3.5 24.42 475.8 3.5 24.65 472.7 4.0 24.27 469.7 4.0 24.38 475.6 4.0 24.49 472.7 4.5 24.27 469.6 4.5 24.34 474.8 4.5 24.43 468.0 5.0 24.16 469.1 5.0 24.30 475.3 5.0 24.43 468.0 6.0 23.96 469.4 7.0 23.79 473.5 7.0 23.90 467.7 8.0 23.53 467.0 8.0 23.77 473.5 7.0 23.67 467.8 9.0 23.40 466.6 9.0 23.51 471.7 9.0 23.53 467.6 9.0 23.40 466.6 9.0 23.51 471.7 9.0 23.53 467.6 9.0 23.40 466.6 9.0 23.39 471.9 10.0 23.34 467.7 11.0 22.79 472.4 11.0 22.98 476.3 11.0 23.13 470.4 12.0 22.17 480.5 12.0 21.60 499.4 499.4 <tr< td=""><td>1.5</td><td>24.52</td><td>470-0</td><td>1.5</td><td>24.85</td><td>476.6</td><td>1.5</td><td>25.02</td><td>469.9</td></tr<>	1.5	24.52	470-0	1.5	24.85	476.6	1.5	25.02	469.9
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.0	26.65	469.6	2.0	24.59	475.8	2.0	24.66	469.7
3.0 24.37 469.2 3.6 24.46 476.6 3.0 24.65 459.2 3.5 24.34 469.5 3.5 24.42 475.8 3.5 24.53 472.7 4.0 24.27 469.7 4.0 24.38 475.6 4.0 24.49 472.4 4.5 24.23 469.6 4.5 24.34 474.8 4.5 24.46 472.2 5.0 24.16 469.6 4.5 24.30 475.3 5.0 24.43 468.0 6.0 23.96 468.3 6.0 24.09 473.9 6.0 24.20 469.6 7.0 23.77 467.4 7.0 23.79 473.5 7.0 23.90 467.7 8.0 23.53 467.0 8.0 23.57 471.7 9.0 23.67 467.8 9.0 23.40 466.6 9.0 23.51 471.7 9.0 23.53 456.9 10.0 23.22 407.8 10.0 23.39 471.9 10.0 23.34 467.7 11.0 22.79 472.4 11.0 22.98 476.3 11.0 23.13 470.4 12.0 22.17 480.1 12.0 22.17 486.5 13.0 13.0 18.98 590.3 13.0	2.5	24.38	469.7	2.5	24.54	475.7	2.5	24.64	459.3
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3.0	29.37	469.2	3.0	24.46	476.6	3.0	24.65	459.2
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	3.5	24.34	469.5	3.5	24.42	475.8	3.5	24.53	472.7
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	4.0	24.27	469.7	4.0	24.38	475.6	4.0	24.49	.472.4
5.0 24.16 669.1 5.0 24.30 475.3 5.0 24.43 468.0 6.0 23.96 468.3 6.0 24.09 473.9 6.0 24.20 469.8 7.0 23.77 467.4 7.0 23.79 473.5 7.0 23.90 467.7 8.0 23.53 467.0 8.0 23.70 472.7 8.0 23.67 467.8 9.0 23.40 466.6 9.0 23.51 471.7 9.0 23.53 466.9 10.0 23.22 407.8 10.0 23.39 471.9 10.0 23.34 467.7 11.0 22.79 472.4 11.0 22.98 476.3 11.0 23.13 470.4 12.0 22.17 480.1 12.0 22.17 486.5 12.0 21.60 49.4 13.0 18.98 590.3 13.0 13.0 49.4	4.5	24.23	469.6	4.5	24.34	474.8	4.5	24.46	472.2
	5.0	24.16	469.1	5.0	24.30	475.3	5.0	24.43	468.0
7.0 23.77 467.4 7.0 23.79 473.5 7.0 23.90 467.7 8.0 23.53 467.0 8.0 23.70 472.7 8.0 23.67 467.8 9.0 23.40 466.6 9.0 23.51 471.7 9.0 23.53 467.7 10.0 23.22 467.8 10.0 23.39 471.9 10.0 23.34 467.7 11.0 22.79 472.4 11.0 22.98 476.3 11.0 23.13 470.4 12.0 22.17 480.1 12.0 22.17 486.5 12.0 21.60 499.4 13.0 18.98 590.3 13.0 13.0 13.0 13.0 13.0 13.0	6.0	23.96	468.3	6.0	24.09	473.9	6.0	24.20	469.8
8.0 23.53 467.0 8.0 23.70 472.7 8.0 23.67 467.8 9.0 23.40 466.6 9.0 23.51 471.7 9.0 23.53 456.9 10.0 23.22 467.8 10.0 23.39 471.9 10.0 23.34 467.7 11.0 22.79 472.4 11.0 22.98 476.3 11.0 23.13 470.4 12.0 22.17 480.1 12.0 22.17 486.5 12.0 21.60 499.4 13.0 18.98 590.3 13.0 13.0 13.0 13.0 13.0	7.0	23.77	467.4	7.0	23.79	473.5	7.0	23.90	467.7
9.0 23.40 466.6 9.0 23.51 471.7 9.0 23.53 466.9 10.0 23.22 467.8 10.0 23.39 471.9 10.0 23.34 467.7 11.0 22.79 472.4 11.0 22.98 476.3 11.0 23.13 470.4 12.0 22.17 480.1 12.0 22.17 486.5 12.0 21.60 499.4 13.0 18.98 590.3 13.0	8.0	23.53	467.0	8.0	23.70	472.7	8.0	23.67	467.8
10.0 23.22 407.8 10.0 23.39 471.9 10.0 23.34 467.7 11.0 22.79 472.4 11.0 22.98 476.3 11.0 23.13 470.4 12.0 22.17 450.1 12.0 22.17 486.5 12.0 21.60 499.4 13.0 18.96 590.3 13.0 13.0 13.0 13.0 13.0 13.0 13.0	9.0	23.40	406.6	9.0	23.51	471.7	9.0	23.53	456.9
11.0 22.79 472.4 11.0 22.98 476.3 11.0 23.13 470.4 12.0 22.17 480.1 12.0 22.17 486.5 12.0 21.60 499.4 13.0 18.94 574.8 13.0 18.98 590.3 13.0	10.0	23.22	407.8	10.0	23.39	471.9	10.0	23.34	467.7
12.0 22.17 490.1 12.0 22.17 486.5 12.0 21.60 499.4 13.0 18.94 574.8 13.0 18.98 590.3 13.0	11.0	22.79	472.4	11.0	22.98	476.3	11.0	23.13	470.4
13.0 18.94 574.8 13.0 18.98 590.3 13.0	12.0	22.17	490.1	12.0	22.17	486.5	12.0	21.60	499.4
	13.0	18.94	574_R	13.0	18.98	590.3	13.0		

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TIME 1500		, TI	TIHE 1700		TINE 2000					
0.0	27.68	472.2	0.0	27.55	473.0	0.0	26.31	471.4		
•2	27.37	473.2	•2	26.40	472.8	• 2	26.34	471.1		
• 4	26.92	473.2	• 4	26.05	472.4	• 4	26.37	470.8		
• 6	26.61	472.4	• 6	25.75	472.1	• 6	26.36	470.9		
.8	26.17	474.6	• 8	25.49	471.9	• 6	26.33	471.7		
1.0	25.48	473.1	1.0	25.41	472.1	1.0	26.29	471.6		
1.5	24.95	472.9	1.5	25.29	471.7	1.5	25.69	472.6		
2.0	24.72	473.5	2.0	25.15	471.9	2.0	- 25.25	470.3		
2.5	24.71	473.0	2.5	25.08	472.6	2.5	24.97	409.1		
3.0	24.67	473.4	3.0	24.81	472.6	3.0	24.83	470.8		
3.5	24.55	473.5	3.5	24.17	471.8	3.5	24.13	470.2		
4.0	24.51	4/3.4	4.0	24.67	471.2	4.0	24.05	469.9		
4.5	24.47	4/3.3	4.5	24.51	4/1.1	4.5	24.40	469.8		
5.0	24.43	473.1	5.0	24.50	470.7	5.0	24 17	469.3		
7.0	24.10	471.9	7.0	24.37	470.8	7.0	23.03	467.1		
8.0	23.68	470.5	8.0	27.11	470.1	7.0 8.0	23.73	468.1		
9.0	23.57	470.5	9.0	23.02	408.9	0.0	23.53	467.2		
10.0	23.43	470.2	10.0	23.11	407.3	10.0	23.42	467.2		
11.0	22.91	476.7	11.0	22.00	407.3	11.0	22.63	477.3		
12.0	21.72	494.9	12.0	21.60	472.0	12.0	21.62	493.1		
13.0	21112	17117	13.0	21.00	1 493.5	13.0	21102			
14.0			14.0			14.0				
15.0			15.0			15.0				
						1,10				
TINE 1600		TI	ME 1800							
0.0	29.20	465.9	0.0	27.36	472.0					
• 2	28.75	464.9	• 2	27.42	471.5					
• 4	26.92	467.8	• 4	27.42	472.0					
• 6	26.09	465.6	•6	27.38	472.4					
• 8	25.30	470.6	• 8	27.16	472.9					
1.0	25.16	468.1	1.0	26.37	470.7					
1.5	24.86	468.2	1.5	25.82	471.7					
2.0	24.78	467.4	2.0	25.33	471.1					
2.5	24.78	467.4	2.5	25.06	472.1					
3.0	24.72	466.3	3.0	24.85	471.4					
3.5	24.69	456.7	3.5	24.76	471.8					
4.0	24.53	466.6	4.0	24.63	471.4					
1.5	24.48	465.9	4.5	24.48	471.1					
5.0	24.47	466.1	5.0	24.47	470.7					
7.0	24.20	404.0	6.0	24.18	470.2					
7.0	23.97	404.3	7.0	23.89	468.6					
0.0	23.72	403.4	8.0	23.69	468.3					
10.0	23.37	403.0	10 0	23.58	468.2					
11.0	22.84	470.1	11.0	23.40	467.8					
12.0	21.68	489.5	12.0	22.00	4/4.1					
13.0	21.00		13.0	22.00	490.1					
14.0			14.0							
15.0			15.0							

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0.0	24.30	468.8	0.0	24.41	470.1	0.0	24 84	(70.5
•2	24.33	469.0	• 2	24.43	470.0	.2	24.83	470.7
.4	24.33	469.0	. 4	24.44	469.9	• 2	24.03	471.0
• 6	24.34	468.9	• 6	24.43	470.0		24.01	471.2
. 8	24.34	469.0	• 8	24.42	470.1	•0	24.01	471.3
1.0	24.34	469.0	1.0	24.43	470.0	1.0	24.70	471.1
1.5	24.35	468.9	1.5	24.41	470.2	1.5	24.74	471.3
2.0	24.35	468.9	2.0	24.40	470.3	2.0	24.70	471.2
2.5	24.35	468.9	2.5	24.40	470.3	2.0	24.00	470.8
3.0	.24.34	468.9	3.0	24.39	469. B	. 2.5	24.03	470.8
3.5	26.36	468.9	3.5	24.39	469.8	3.0	24.53	471.2
6.0	24.33	469-0	4.0	24.39	469.9	3.5	24.49	471.1
4.5	24.34	469.0	4.5	24.37	670.0	4.0	24.49	471.1
5.0	24 33	467.0	5.0	24.37	460.5	4.5	24.47	470.6
5.0	24 32	460.2	6.0	26.36	469.5	5.0	24.45	470.4
7.0	24 32	46762	7.0	24.33	460 3	6.0	24.41	470.7
1.0	24 07	400.0	8.0	24.13	409.3	7.0	24.38	470.5
0.0	29.07	466 0	9.0	23 50	404.0	8.0	24.05	467.3
7.0	23.33	400.9	10.0	23.34	400.9	9.0	23.88	467.7
10.0	23.51	400.7	11 0	22 77	407.62	15.0	23.53	463.4
12.0	10.00	771.0	12.0	21 02	472.0	11.0	22.76	474.2
12.0	19.00	500.5	12.0	21.93	407.9	12.0	21.68	492.5
TIME 730		T	IME 930	,	т	IME 1130		
0.0	24.31	466.7	0.0	24.57	468.7			
.2	24.33	466.5	.2	24.58	469.1	0.0	26.10	468.5
	24.32	466.6	. 4	24.57	460 8	• 2	25.53	469.2
6	24 33	400.0	. 6	24.56	460 3	• 4	25.60	465.7
•0 8	24.33	466.5	. 8	24.56	404.3	• 6	25.14	469.1
•0	24 33	400.5	1.0	24.56	409.3	•8	25.05	469.0
1.0	24 53	400.5	1.5	24 53	409.3	1.0	24.98	469.1
2.0	24 22	407.0	2.0	24 52	404.0	1.5	24.84	468.9
2.0	24.32	400.0	2 5	24.52	469.1	2.0	24.80	468.1
2.5	24.35	400.9	3.0	24.45	100.0	2.5	24.79	463.3
3.0	24.35	400.5	3.0	24.43	469.4	3.0	24.74	463.2
3.5	24.35	430.3	5.5	24.41	409.7	3.5	24.62	467.7
4.0	24.34	400.4	7.0	24.41	409.2	4.0	24.58	467.6
4.2	24.34	400.4	1.5	24.39	469.4	4.5	24.57	467.7
5.0	24.34	400.4	5.5	24.37	469.6	5.0	24.52	467.6
6.0	24.33	400.5	0.3	24.35	469.2	6.0	24.45	467.2
7.0	24.30	400.3	/•0	24.34	468.8	7.0	24.39	466.1
8.0	24.22	465.9	8.0	23.91	467.4	8.0	24.08	465.3
9.0	23.52	463.9	9.0	23.71	467.8	9.0	23.86	466 1
10.0	23.33	464.1	10.0	23.44	466.6	10.0	23.56	404 • <u>1</u>
11.0	22.83	470.4	11.0	22.75	473.7	11.0	23.10	101.3
12.0	20.83	497.7	12.0	21.54	493.2	12.0	21.79	486.4

TIME 1030

TINE 630

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TIME 830

DEPTH TEMPERATURE SALINITY

05 02 76 SALINITY AND TEMPERATURE STRUCTURE

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TIME 1230		TI	ME 1430		т	IME 1630		
0.0	26.72	470.9	0.0	28.44	472.5	0.0	25,88 -	468.1
•2	26.51	470.3	.2	26.67	469.8	• 2	25.88	468.7
. 4	25.49	471.1	. 4	26.09	469.0	• 4	25.86	468.8
.6	25.32	470.6	• 6	25.80	469.1	• 6	25.84	465.5
• 8	25.17	470.4	.8	25.46	469.7	• 8	25.86	463.9
1.0	25.07	470.3	1.0	25.30	469.1	1.0	25.78	469.1
1.5	24.91	469.7	1.5	25.05	469.3	1.5	25.74	468.9
2.0	24.88	469.4	2.0	24.95	469.3	2.0	25.56	468.5
2.5	24.79	469.2	2.5	24.88	468.8	2.5	25.47	468.2
3.0	· 24.73	469.3	3.0	24.87	468.9	3.0	25.19	467.7
3.5	24.69	469.1	3.5	24.82	468.9	3.5	24.83	463.0
4.0	24.05	468.9	4.0	24.75	469.0	4.0	24.74	467.7
4.5	24.61	468.7	4.5	24.70	468.9	4.5	24.70	468.7
5.0	24.57	468.6	5.0	24.67	468.2	5.0	24.67	468.4
6.0	24.51	468.0	6.0	24.53	467.9	6.0	24.63	467.8
7.0	24.32	457.1	7.0	24.41	467 4	7.0	24.50	467.3
8.0	24.01	467.5	8.0	24.26	467.2	8.0	24.41	467.2
9.0	23.92	465.5	9.0	23.97	465 7	9.0	23.74	466.0
10.0	23.67	454.6	10.0	23 56	465 2	10.0	23.58	465 2
11.0	23.02	409.2	11.0	22.56	475 0	11.0	22.76	471.6
12.0	22.29	478.4	12.0	21.62	491.7	12.0	21.53	492.2
TTHE 1326			HE 1820		T	IME 1730		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
		11	ne 1530		·			
0.0	28.10	472.4	0.0	26.87	470.2	0.0	25.88	468.6
• 2	26.76	470.9	•2	26.85	469.8	• 2	25.90	468.9
. 4	25.80	470.6	• 4	26.94	470.4	. 4	25.89	469.6
• 6	25.55	470.3	• 6	26.82	470.6	• 6	25.89	469.6
• 8	25.38	469.7	• 8	26.61	469.4	• 8	25.88	469.1
1.0	25.24	470.0	1.0	26.20	470.1	1.0	25.88	469.7
1.5	25.02	469.5	1.5	25.18	469.2	1.5	25.89	469.6
2.0	24.96	468.9	2.0	25.07	469.8	2.0	25.85	459.4
2.5	24.90	469.0	2.5	25.03	469.0	2.5	25.70	453.7
3.0	24.81	469.3	3.0	24.96	469.2	3.0	25.59	407.6
2.5	24.75	468.8	3.5	24.92	469.0	3.5	25.47	456.3
4.0	24.71	468.7	40	24.80	469.1	4.0	24.84	469.0
4.5	24.67	468.5	4.5	24.68	469.2	4.5	24.70	467.5
5.0	24.64	468.3	5.0	24.63	469.1	5.0	24.68	467.7
· 6.0	24.52	467.8	6.0	24.54	468.4	6.0	24.62	467.2
7.0	24.38	460.1	7.0	24.41	467.9	7.0	24.50	467.4
9.0	24.23	467.4	8.0	24.37	467.8	8.0	24.43	466.9
9.0	23.97	466.6	9.0	23.83	465.3	9.0	23.86	465.3
10.0	23.69	464.8	10.0	23.63	466.2	10.0	23.55	465.6
11.0	22.48	477.1	11.0	22.81	470.6	11.0	22.53	475.1
12.0	21.68	494.3	12.0	20.92	500.6	12.0	21.45	492.4

12.0	21.04	502.5	
1			
0.0	25.31	468.9	
• 2	25.33	469.2	
.4	25.38	468.8	
•6	25.36	469.0	
.8	25.36	468.4	
1.0	25.34	468.6	
1.5	25.35	468.5	
2.0	25.38	468.3	
2.5	25.36	468.4	
э.О	25.25	469.5	
3.5	25.16	468.2	
4.0	25.15	467.8	
4.5	25.11	468.1	
5.0	24.61	468.1	
6.0	24.45	467.6	
7.0	24.35	467.4	
8.0	23.85	465.7	
9.0	23.28	468.1	
10.0	23.09	467.7	
11.0	22.92	468.9	
12.0	20.94	502.0	

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TIME 231

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0.0	25.69	468.8
• 2	25.70	468.8
. 4	25.70	469.3
•6	25.70	469.3
.8	25.70	468.8
1.0	25.70	468.8
1.5	25.66	468.6
2.0	25.58	469.4
.2.5	25.43	468.7
3.0	25.33	468.6
3.5	25.27	468.1
4.0	25.26	467.6
4.5	25.03	469.3
5.0	24.70	468.2
6.0	24.57	467.8
7.0	26.66	466.9
8.0	24.38	466.9
9.0	24.09	455.9
10.0	23.49	466.3
11.0	22.54	473.8
12.0	21.04	502.3
		,02.13
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TIME 2010
05 04 76 SALINITY AND TEMPERATURE STRUCTURE

DEPTH TEMPERATURE SALINITY

TIME 1400

0.0	21.03	514.8	0.0	21.75	497.8	0.0	21.76	499.3
.1	21.04	502.9	•1	21.76	497.9	•1	21.76	499.5
.15	21.05	502.8	.15	21.76	498.0	.15	21.77	499.6
• 2	21.05	502.8	• 2	21.75	498.2	• 2	21.78	499.5
. 4	21.05	502.8	. 4	21.73	498.2	• 4	21.76	499.4
• 6	21.05	502.9	. 6	21.73	498.0	• 6	21.78	499.3
• 8	21.05	503.0	. 8	21.68	498.4	. 8	21.78	499.1
1.0	21.05	502.8	1.0	21.66	497.7	1.0	21.76	499.4
1.5	21.05	502.9	1.5	21.61	497.5	1.5	21.55	499.0
2.0	21.04	503.0	2.0	21.56	497.4	2.0	21.57	498.5
2.5	21.04	502.5	2.5	21.48	497.6	2.5	21.52	493.7
3.0	21.03	502.6	3.0	21.45	497.4	3.0	21.38	493.E
3.5	21.03	502.4	3.5	21.43	497.6	3.5	21.28	493.4
4.0	21.03	501.8	4.0	21.39	497.9	4.0	21.30	498.2
4.5	21.03	502.1	4.5	21.36	497.7	4.5	21.27	498.1
5.0	21.03	502.0	5.0	21.32	497.0	5.0	21.24	497.7
6.0	21.02	501.8	6.0	21.27	497.0	6.0	21.22	497.2
7.0	21.03	501.0	7.0	21.22	497.0	7.0	21.20	497.2
8-0	21.02	500.9	8.0	21.22	496.7	8.0	21.21	197.1
9.0	21 02	500.6	0.0	21.20	496.6	9.0	21.19	497 1
10.0	21 01	500.5	10.0	21 17	494.5	10.0	21.14	406 2
11.0	21.01	501 1	10.0	21.09	499 2	11.0	21.10	475.5
12.0	20.00	507.1	11.0	21.00	512 7	12.0	21.10	490.0
12.0	20.90	507.1	12.0	20.78	512.17	12.0	21.00	479.1
12.3			12.3			12.5		
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12.7	17 (5		12.7		(20.4	12.7	10.22	
13.0	17.05	000.3	13.0	19.20	029.0	13.0	19.23	620.7
TIME 1030		TI	ME 1500		1	IME 1845		
0.0	21.16	503.3	0.0	21.76	499.4	0.0	21.38	500.1
.1	21.18	503.7	•1	21.77	499.7	-1	21.39	499.8
.15	21.18	503.6	.15	21.77	499.5	.15	21.39	500.2
. 2	21.18	503.6	• 2	21.76	499.4	.2	21.40	499.6
. 4	21.18	503.5	• 4	21.77	499.4	. 4	21.41	499.6
• 6	21.17	503.5	• 6	21.77	499.1	• 6	21.44	499.0
• 8	21.17	503.5	.8	21.74	498.7	. 8	21.44	499.2
1.0	21.17	503.7	1.0	21.68	499.1	1.0	21.41	499.4
1.5	21.17	503 .7	1.5	21.64	499.0	1.5	21.44	499.3
2.0	21.16	503.6	2.0	21.57	498.4	2.0	21.44	499.3
2.5	21.10	503.6	2.5	21.44	498.8	2.5	21.43	499.2
3.0	21.12	503.6	3.0	21.41	498.8	3.0	21.47	49c.7
3.5	21.11	503.4	3.5	21.34	498.9	3.5	21.45	498.6
4.0	21.11	503.4	4.0	21.27	498.0	4.0	21.35	499.0
4.5	21.11	503.1	4.2	21.26	498.4	4.5	21.28	498.9
5.0	21,10	502.6	5.0	21.26	498.2	5.0	21.28	499.2
6.0	21.10	502.1	6.0	21.21	498.1	6.0	21.24	498.2
7.0	21.09	502.1	7.0	21.17	495.0	7.0	21.19	496.8
8.0	21.08	501.8	8.0	21.16	497.7	8.0	21.16	496.8
9.0	21.06	501.2	9.0	21,15	497.5	9.0	21,15	497.0
10.0	21.05	500.1	10.0	21.13	497.4	10.0	21.11	497 4
11.0	21.03	500.6	11.0	21.06	500.6	11.0	20.99	498 0
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One 11 is 21 is 107 is 11 is 21 is <th2< td=""><td>0.0</td><td>21.34</td><td>497.1</td><td>0.0</td><td>21.22</td><td>498.0</td></th2<>	0.0	21.34	497.1	0.0	21.22	498.0
1.1 21.27 497.5 2 21.28 497.1 12 21.29 497.5 2 21.39 497.0 4 21.30 497.2 6 21.39 497.0 16 21.29 497.3 1.0 21.39 497.0 16 21.30 497.2 1.5 21.39 497.0 16 21.30 497.2 2.0 21.39 496.9 2.6 21.30 497.2 2.15 21.38 496.6 2.0 21.30 497.2 3.0 21.31 496.6 2.0 21.30 497.1 3.0 21.40 496.1 5.0 21.30 497.1 3.5 21.40 496.1 5.0 21.31 496.5 4.5 21.40 496.1 5.0 21.31 496.5 6.0 21.23 496.1 5.0 21.23 496.5 7.0 21.25 6.0 21.23 496.1	0.0	21 26	497.0	•1	21.26	497.6
1.2 21.26 497.5 12 21.26 497.5 6 21.39 497.0 6 21.30 497.5 6 21.39 497.0 6 21.30 497.5 10 21.39 497.0 16 21.30 497.5 1.0 21.39 497.0 1.6 21.20 497.5 2.0 21.38 496.9 2.6 21.30 497.2 2.0 21.38 496.9 2.6 21.30 497.1 3.5 21.40 496.4 3.5 21.31 497.1 3.5 21.40 496.4 3.5 21.31 497.1 4.0 21.40 496.1 5.0 21.31 497.1 4.0 21.41 496.1 5.0 21.31 497.1 5.0 21.41 496.1 5.0 21.32 497.5 6.0 21.22 496.6 1.0 21.26 496.7 10.0 21.13	.15	21.37	497.6	.15	21.27	497.5
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1 21.50 107.0 16 21.20 407.2 1.0 21.39 497.0 1.0 21.29 497.3 1.0 21.39 496.9 1.5 21.30 497.2 2.0 21.38 496.6 2.0 21.30 497.1 3.0 21.39 496.6 2.5 21.30 497.1 3.0 21.39 496.4 3.0 21.30 497.1 3.0 21.40 496.4 3.0 21.30 497.1 4.0 21.40 496.1 5 21.30 497.1 4.0 21.40 496.1 5 21.30 497.2 5.0 21.40 496.1 5 21.30 496.4 6.0 21.25 493.0 7.0 21.26 496.2 7.0 21.25 493.0 9.0 21.24 496.1 10.0 21.13 495.6 10.0 21.14 497.2 11.0 21.13	• •	21.30	497.0	.4	21.30	497.2
<td>• •</td> <td>21.37</td> <td>497.0</td> <td>.6</td> <td>21.29</td> <td>497.3</td>	• •	21.37	497.0	.6	21.29	497.3
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C 13 3.0 C 1.30 Y 00.0 Y 10.0 Y 11.0 Y 11.30 Y 00.0 3.5 C 1.40 Y 00.0	2.0	21.30	490.9	2.5	21.30	497.1
3.0 21.33 700.1 3.5 21.41 407.1 4.0 21.40 486.5 4.0 21.32 497.0 4.0 21.40 486.5 4.5 21.33 497.0 4.0 21.41 486.1 5.0 21.31 496.7 5.0 21.40 486.1 5.0 21.23 497.2 5.0 21.41 486.1 5.0 21.24 496.7 6.0 21.22 494.5 8.0 21.24 496.1 6.0 21.22 494.5 8.0 21.24 496.1 10.0 21.18 495.6 10.0 21.14 497.2 11.0 21.10 497.2 12.10 497.5 12.10 497.5 12.3 20.6 498.5 12.0 21.10 497.5 12.3 12.7 198.5 12.1 900.6 12.15 900.7 12.3 20.1 18.0 18.0 18.0 90.7	2.5	21.30	490.0	3.0	21.30	497.1
A:3 C1.40 400.1 C1.32 C1.71 4:0 21.40 400.1 4.5 21.33 407.0 4:5 21.40 400.1 5.0 21.33 406.5 6:0 21.27 495.6 6.0 21.23 406.5 6:0 21.25 404.9 7.0 21.26 496.6 9:0 21.18 405.0 9.0 21.23 406.1 10:0 21.13 405.0 10.0 21.14 497.2 11:0 21.00 406.4 11.0 21.10 497.2 12:0 20.85 498.5 12.20 21.05 497.5 12:1 10.0 21.13 405.0 13.0 18.0 554.2 12:1 10.16 653.0 13.0 18.0 554.2 12:2 20.1 21.15 500.7 12.16 500.7 12:2 21.20 408.2 11 21.16 500.7 12:2	3.0	21.39	490.4	3.5	21.31	497.1
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4.0	21.40	496.2	4.5	21 30	497.0
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7.0 21.25 494.9 7.0 21.26 496.0 9.0 21.18 495.0 9.0 21.23 496.1 10.0 21.13 495.0 10.0 21.14 497.2 11.0 21.00 496.4 11.0 21.10 497.2 11.0 21.00 496.4 11.0 21.10 497.2 12.0 20.86 498.5 12.0 21.05 497.5 12.3 20.18 542.9 12.5 12.7 19.83 554.2 12.7 19.83 554.2 12.7 19.83 556.7 13.0 18.16 653.0 13.0 16.04 658.7 14 21.29 498.0 0.0 21.15 500.7 15 21.27 498.5 .15 21.21 500.4 .12 21.29 498.0 .15 21.22 500.7 .15 21.22 497.5 .6 21.23 500.4 .	6.0	21.27	495.6	8.0	21.20	490.7
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0,0 21.18 495.0 9.0 21.23 496.1 10.0 21.10 496.4 11.0 21.10 497.0 11.0 21.00 496.4 11.0 21.10 497.0 12.0 20.85 498.5 12.0 21.05 497.0 12.3 12.0 12.0 21.05 497.0 497.0 12.7 12.7 12.5 12.7 19.83 554.2 13.0 18.16 653.0 13.0 18.04 656.7 11 21.29 498.5 .15 21.21 500.7 .1 21.29 498.5 .15 21.21 500.7 .1 21.29 498.5 .15 21.21 500.7 .1 21.29 498.5 .15 21.21 500.7 .1 21.29 498.5 .15 21.21 500.7 .1 21.29 498.5 .15 21.21 500.7 .15 21.32	6.0	21.22	494.5	8.0	21.24	496.0
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	9.0	21.18	495.0	.9.0	21.23	496.1
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TIME 2200 TIME 200 0.0 21.28 498.0 0.0 21.15 500.7 1 21.29 498.2 1 21.18 500.3 .16 21.27 498.5 .15 21.21 500.6 .2 21.22 497.6 .4 21.22 500.7 .6 21.32 497.6 .4 21.22 500.7 .6 21.32 497.5 .6 21.23 500.4 .6 21.32 497.5 .6 21.23 500.4 .6 21.32 497.5 .6 21.23 500.3 1.0 21.32 497.6 .6 21.23 500.4 .6 21.33 497.5 .6 21.23 500.4 .6 21.33 497.5 2.0 21.23 500.5 2.0 21.33 497.3 2.5 21.23 490.6 3.5 21.33 497.0 3.0 21.23 499.6 4.5 21.33 497.0 3.0 21.23 499.6 5.5 21.33 497.6 .5 21.23 499.6 6.5 21.33 497.6 .6 21.23 499.6 <	13.0	18.16	653.0	13.0	18.04	658.7
11ne 200 11ne 200 0.0 21.28 498.0 0.0 21.15 500.7 .1 21.29 498.2 .1 21.18 500.6 .2 21.32 497.9 .2 21.20 500.7 .4 21.32 497.6 .4 21.22 500.5 .6 21.32 497.5 .6 21.23 500.4 .8 21.32 497.5 .6 21.23 500.3 .10 21.32 497.7 1.0 21.23 500.4 .8 21.24 500.3 1.5 21.22 500.5 2.0 21.32 497.6 1.5 21.22 500.5 2.0 21.33 497.5 2.0 21.23 500.4 3.0 21.33 497.7 3.0 21.23 499.6 3.5 21.33 497.0 3.0 21.23 499.6 4.5 21.33 497.0 4.0 21.23 499.6 4.5 21.32 496.9 5.0 21.23	TTNC 3300			TINE 200		
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1 21.29 490.2 1 21.10 21.10 500.3 $.15$ 21.27 490.5 $.15$ 21.21 500.6 $.2$ 21.32 497.9 $.2$ 21.20 500.7 $.4$ 21.32 497.6 $.4$ 21.22 500.5 $.6$ 21.34 497.5 $.6$ 21.23 500.4 $.8$ 21.32 497.5 $.6$ 21.23 500.4 $.8$ 21.32 497.5 $.6$ 21.23 500.3 1.0 21.32 497.7 1.0 21.23 500.3 1.5 21.32 497.6 1.5 21.22 500.5 2.0 21.33 497.5 2.0 21.23 500.4 2.5 21.33 497.5 2.0 21.23 500.4 3.5 21.34 497.0 3.0 21.23 499.6 3.5 21.34 497.0 3.5 21.22 499.6 4.5 21.33 497.0 4.0 21.23 499.6 4.5 21.32 496.7 5.0 21.24 499.7 5.0 21.32 496.7 5.0 21.24 499.7 6.0 21.22 496.7 5.0 21.24 499.6 4.5 21.32 496.7 5.0 21.24 499.7 5.0 21.24 496.7 5.0 21.24 499.6 4.5 21.32 496.7 5.0 21.24 499.6 6.0 </td <td>0.0</td> <td>21.28</td> <td>498.0</td> <td>0.0</td> <td>21.15</td> <td>500.7</td>	0.0	21.28	498.0	0.0	21.15	500.7
11521.27490.511521.21500.6.221.32497.9.221.20500.7.421.32497.6.421.22500.5.621.34497.5.621.23500.4.821.32497.5.821.24500.31.021.32497.5.821.24500.31.521.32497.5.821.22500.52.021.33497.52.021.23500.42.521.33497.52.021.23500.43.021.33497.52.021.23500.43.021.33497.52.021.23500.43.021.33497.52.021.23499.63.521.34497.03.021.23499.63.521.34497.03.021.23499.64.521.32496.94.521.23499.75.021.33497.04.021.23499.75.021.22496.75.021.23499.75.021.32496.75.021.24499.76.021.23496.56.021.23499.17.021.24496.56.021.23499.17.021.22496.75.021.24497.89.021.23496.59.021.24497.89.021.24496.59.021.26498.3	0.0	21 20	47010	.1	21.18	500.3
.2 21.32 497.9 .2 21.20 500.7 .4 21.32 497.6 .4 21.22 500.5 .6 21.34 497.5 .6 21.23 500.4 .8 21.32 497.5 .6 21.23 500.4 .8 21.32 497.7 1.0 21.23 500.3 1.0 21.32 497.6 1.5 21.22 500.5 2.0 21.33 497.6 1.5 21.22 500.5 2.0 21.33 497.5 2.0 21.23 500.4 3.0 21.35 497.0 3.0 21.23 499.6 3.0 21.35 497.0 3.0 21.23 499.6 4.5 21.32 496.7 5.0 21.23 499.7 6.0 21.33 497.0 4.0 21.23 499.7 5.0 21.32 496.7 5.0 21.23 499.7 6.0 21.33 496.7 5.0 21.23 499.1 7.0 21.22 496.5	15	21 27	49012	.15	21.21	500.6
12 $11,32$ $197,6$ 12 122 $500,5$ $1,6$ $21,32$ $497,6$ 4 $21,22$ $500,4$ $1,8$ $21,32$ $497,5$ $.6$ $21,23$ $500,3$ $1,0$ $21,32$ $497,7$ 1.0 $21,23$ $500,5$ $2,0$ $21,33$ $497,5$ 2.0 $21,23$ $500,4$ $2,5$ $21,33$ $497,5$ 2.0 $21,23$ $500,4$ $2,5$ $21,33$ $497,5$ 2.0 $21,23$ $500,4$ $3,0$ $21,35$ $497,0$ 3.0 $21,23$ $499,6$ $3,5$ $21,34$ $497,11$ 3.5 $21,22$ $499,6$ $4,5$ $21,32$ $496,9$ 4.5 $21,23$ $499,6$ $4,5$ $21,32$ $496,9$ 4.5 $21,23$ $499,6$ $4,5$ $21,32$ $496,7$ 5.0 $21,23$ $499,6$ $4,5$ $21,32$ $496,7$ 5.0 $21,23$ $499,6$ 5.0 $21,29$ $496,5$ 6.0 $21,23$ $499,1$ 7.0 $21,26$ $498,4$ 7.6 $21,27$ $498,6$ 8.0 $21,24$ $496,5$ 6.0 $21,26$ $498,3$ 9.0 $21,23$ $495,5$ 9.0 $21,24$ $497,6$ 10.0 $21,11$ $496,3$ 10.0 $21,15$ $498,4$ 10.0 $21,21$ $530,1$ 12.0 $21,09$ $499,5$ 12.3 $20,21$ $530,1$ 12.3 $20,64$ $507.$ 12.5 <td>2</td> <td>21 32</td> <td>470.5</td> <td>.2</td> <td>21.20</td> <td>500.7</td>	2	21 32	470.5	.2	21.20	500.7
\cdot 21.32 497.5 \cdot 1.7 1.23 500.4 $\cdot 8$ 21.32 497.5 $\cdot 8$ 21.23 500.3 1.0 21.32 497.7 1.0 21.23 500.3 1.5 21.32 497.6 1.5 21.22 500.5 2.0 21.33 497.5 2.0 21.23 500.4 2.5 21.33 497.5 2.0 21.23 500.4 2.5 21.33 497.5 2.0 21.23 500.4 3.0 21.33 497.3 2.5 21.23 499.6 3.5 21.34 497.1 3.5 21.22 499.6 4.5 21.33 497.0 3.0 21.23 499.6 4.5 21.32 496.9 4.5 21.23 499.7 5.0 21.32 496.7 5.0 21.23 499.7 5.0 21.24 496.7 5.0 21.23 499.7 6.0 21.29 496.5 6.0 21.23 499.7 7.0 21.26 498.4 7.6 21.27 498.6 9.0 21.24 496.5 9.0 21.24 497.6 9.0 21.23 495.5 9.0 21.24 497.6 9.0 21.23 495.5 9.0 21.26 498.3 9.0 21.23 495.5 9.0 21.24 497.6 10.0 21.11 496.3 10.0 21.15 496.3 <t< td=""><td>• 2</td><td>21 32</td><td>407 6</td><td>. 4</td><td>21.22</td><td>500.5</td></t<>	• 2	21 32	407 6	. 4	21.22	500.5
0 21.32 497.5 10 21.24 500.3 1.0 21.32 497.7 1.0 21.23 500.3 1.5 21.32 497.6 1.5 21.22 500.5 2.0 21.33 497.5 2.0 21.23 500.4 2.5 21.33 497.5 2.0 21.23 500.4 2.5 21.33 497.3 2.5 21.23 499.6 3.0 21.35 497.0 3.0 21.23 499.6 3.5 21.34 497.1 3.5 21.22 499.9 4.5 21.32 496.9 4.5 21.23 499.7 5.0 21.32 496.7 5.0 21.23 499.7 5.0 21.32 496.7 5.0 21.23 499.7 6.0 21.29 496.5 6.0 21.23 499.7 7.0 21.26 496.7 5.0 21.23 499.7 6.0 21.29 496.5 6.0 21.23 499.7 7.0 21.26 496.5 6.0 21.27 496.8 9.0 21.24 496.2 8.0 21.26 498.3 9.0 21.23 495.5 9.0 21.24 496.3 10.0 21.11 496.3 10.0 21.15 496.3 11.0 21.11 496.3 10.0 21.15 496.3 11.0 20.93 499.0 12.0 21.09 499.5 12.3	••	21 34	407 5	. 6	21.23	500.6
10 21.32 497.7 1.0 21.23 500.3 1.5 21.32 497.6 1.5 21.22 500.5 2.0 21.33 497.5 2.0 21.23 500.4 2.5 21.33 497.5 2.0 21.23 500.4 3.0 21.33 497.5 2.0 21.23 500.4 3.0 21.33 497.5 2.5 21.23 499.6 3.0 21.35 497.0 3.0 21.23 499.6 4.0 21.33 497.0 4.0 21.23 499.6 4.5 21.32 496.9 4.5 21.23 499.7 4.5 21.32 496.7 5.0 21.23 499.7 5.0 21.32 496.7 5.0 21.23 499.7 5.0 21.29 496.5 6.0 21.23 499.7 6.0 21.29 496.5 6.0 21.23 499.1 7.0 21.26 496.4 7.6 21.27 496.8 9.0 21.24 496.2 8.0 21.26 498.3 9.0 21.23 495.5 9.0 21.24 497.6 10.0 21.11 496.3 10.0 21.15 496.3 11.0 21.03 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 $507.$ 12.5 19.93 541.6 547.6 547.6 12.5 19	•0	21 32	407 5	. 8	21.24	500.3
1.021.32497.61.021.22500.51.521.33497.52.021.23500.42.521.33497.32.521.23499.63.021.35497.03.021.23499.94.021.33497.04.021.23499.64.521.32496.94.521.22499.95.021.32496.94.521.23497.65.021.32496.75.021.23499.16.021.29496.56.021.23499.17.021.26498.47.621.27498.89.021.23495.59.021.26498.311.021.05496.310.021.15496.311.021.05496.611.021.15496.312.2020.93499.012.021.09499.512.320.21530.112.320.64507.12.519.93541.612.320.64507.		21 32	47745	1.0	21.23	500.3
1.521.32497.52.021.42 500.4 2.021.33497.32.521.23 500.4 2.521.33497.03.021.23 499.6 3.021.35497.03.021.22 499.6 3.521.34497.13.521.22 499.9 4.021.33496.94.521.23 497.7 5.021.32496.75.021.23 499.7 6.021.29496.75.021.23 499.7 7.021.26498.47.621.23 499.7 8.021.24496.56.021.23 499.7 9.021.259.021.24496.310.010.021.11496.310.021.15496.311.021.05496.611.021.14496.312.020.93499.012.021.09499.512.320.21530.112.320.64507.12.519.93541.612.320.64507.	1.0	21.32	49747	1.5	21 22	500.5
2.0 21.33 497.3 2.5 21.23 500.4 3.0 21.35 497.0 3.0 21.23 499.8 3.5 21.34 497.1 3.5 21.23 499.8 4.0 21.33 497.0 4.0 21.23 499.9 4.0 21.32 496.9 4.5 21.23 499.7 5.0 21.32 496.9 4.5 21.23 499.7 5.0 21.32 496.7 5.0 21.23 499.7 6.0 21.29 496.5 6.0 21.27 498.4 7.0 21.26 498.4 7.6 21.27 498.3 9.0 21.23 495.5 9.0 21.26 498.3 9.0 21.23 495.5 9.0 21.24 496.3 10.0 21.11 496.3 10.0 21.15 496.3 11.0 21.05 496.6 11.0 21.14 496.3 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 $507.$ 12.5 19.93 541.6 442.4 442.4	1.5	21,32	497.0	2 0	21.23	500.5
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3.0 21.35 497.0 3.0 21.23 497.0 3.5 21.34 497.0 3.55 21.22 499.0 4.0 21.33 497.0 4.0 21.23 499.6 4.5 21.32 496.9 4.5 21.23 499.7 5.0 21.32 496.7 5.0 21.23 499.7 6.0 21.29 496.5 6.0 21.23 499.7 7.0 21.26 498.4 7.6 21.23 499.7 8.0 21.24 496.5 6.0 21.27 498.6 8.0 21.24 496.2 8.0 21.26 498.3 9.0 21.23 495.5 9.0 21.24 497.6 10.0 21.11 496.3 10.0 21.15 496.3 11.0 21.05 496.6 11.0 21.14 496.4 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 $507.$ 12.5 19.93 541.6 482.8 482.8	2.5	21.33	497.3	2.5	21 23	400.4
3.5 21.34 497.1 3.5 21.22 496.9 4.0 21.33 496.9 4.5 21.23 499.7 4.5 21.32 496.9 4.5 21.23 499.7 5.0 21.32 496.7 5.0 21.23 499.7 6.0 21.29 496.5 6.0 21.23 499.1 7.0 21.26 498.4 7.6 21.27 496.4 8.0 21.24 496.2 8.0 21.26 498.3 9.0 21.23 495.5 9.0 21.26 496.3 10.0 21.11 496.3 10.0 21.15 496.3 11.0 21.05 496.6 11.0 21.14 496.3 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 $507.$ 12.5 19.93 541.6 12.3 20.64 $507.$	3.0	21.35	497.0	3.0	21.23	497.0
4.0 21.33 497.0 4.0 21.23 499.7 4.5 21.32 496.7 5.0 21.23 499.7 5.0 21.29 496.7 5.0 21.23 499.7 6.0 21.29 496.5 6.0 21.23 499.1 7.0 21.26 498.4 7.6 21.27 498.8 8.0 21.23 495.5 9.0 21.26 498.3 9.0 21.23 495.5 9.0 21.24 497.6 10.0 21.11 496.3 10.0 21.15 498.3 11.0 21.05 496.6 11.0 21.15 496.3 11.0 21.05 499.0 12.0 21.09 499.5 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 507. 12.5 19.93 541.6 12.3 20.64 507.	3.5	21.34	497.1	3.5	21.22	499.9
4.5 21.32 496.9 4.3 21.23 499.7 5.0 21.32 496.7 5.0 21.24 499.7 6.0 21.29 496.5 6.0 21.23 499.1 7.0 21.26 498.4 7.6 21.27 498.8 8.0 21.24 496.2 8.0 21.26 498.3 9.0 21.23 495.5 9.0 21.24 497.6 10.0 21.11 496.3 10.0 21.15 497.8 11.0 21.05 496.6 11.0 21.14 492.4 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 $507.$ 12.5 19.93 541.6 482.5 482.5	4.0	21.33	497.0	4.0	21.23	499.0
5.0 21.32 496.7 7.0 21.24 499.7 6.0 21.29 496.5 6.0 21.23 499.1 7.0 21.26 498.4 7.6 21.27 498.6 8.0 21.24 496.2 8.0 21.26 498.3 9.0 21.23 495.5 9.0 21.24 496.3 10.0 21.11 496.3 10.0 21.15 496.3 11.0 21.05 496.6 11.0 21.14 496.4 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 $507.$ 12.5 19.93 541.6 482.5 9.064 $507.$	4.5	21.32	496.9	4.5	21.23	499.7
6.0 21.29 496.5 6.0 21.23 499.1 7.0 21.26 496.4 7.6 21.27 496.8 8.0 21.24 496.2 8.0 21.26 498.3 9.0 21.23 495.5 9.0 21.24 497.6 10.0 21.11 496.3 10.0 21.15 496.3 11.0 21.05 496.6 11.0 21.14 496.3 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 507. 12.5 19.93 541.6 542.5 543.5 543.5	5.0	21.32	496.7	5.0	21.24	499.7
7.0 21.26 498.4 7.0 21.27 498.8 8.0 21.24 496.2 8.0 21.26 498.3 9.0 21.23 495.5 9.0 21.24 496.3 10.0 21.11 496.3 10.0 21.15 496.3 11.0 21.05 496.6 11.0 21.14 496.4 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 507. 12.5 19.93 541.6 542.5 542.5 542.5	6.0	21.29	496.2	0.0	21.23	499.1
8.0 21.24 496.2 8.0 21.26 498.3 9.0 21.23 495.5 9.0 21.24 497.6 10.0 21.11 496.3 10.0 21.15 496.4 11.0 21.05 496.6 11.0 21.14 492.4 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 507. 12.5 19.93 541.6 542.5 542.5 543.5	7.0	21.26	498.4	1.0	21.27	498.8
9.0 21.23 495.5 9.0 21.24 497.6 10.0 21.11 496.3 10.0 21.15 496.3 11.0 21.05 496.6 11.0 21.14 496.3 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 507. 12.5 19.93 541.6 542.5 542.5 542.5	8.0	21.24	496.2	8.0	21.26	498.3
10.0 21.11 496.3 10.0 21.15 496.3 11.0 21.05 496.6 11.0 21.14 496.4 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 507. 12.5 19.93 541.6 547.5 547.5	9.0	21.23	495.5	9.0	21.24	497.8
11.0 21.05 496.6 11.0 21.14 496.4 12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 507. 12.5 19.93 541.6 542.5 542.5 542.5	10.0	21.11	496.3	10.0	21.15	498.3
12.0 20.93 499.0 12.0 21.09 499.5 12.3 20.21 530.1 12.3 20.64 507. 12.5 19.93 541.6 543.5 543.5	11.0	21.05	496.6	11.0	21.14	498.4
12.3 20.21 530.1 12.3 20.64 507. 12.5 19.93 541.6	12.0	20.93	499.0	12.0	21.09	499.5
12.5 19.93 541.6 3.5	12.3	20.21	530.1	12.3	20.64	507.
· · · · · · · · · · · · · · · · · · ·	12.5	19.93	541+6			
			·····································			

TIME 2030

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TIME 2350

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A5

Computer Plots of Measured Temperature Profiles.

Date and times for each symbol are as printed on the plots. The last profile of each plot appears on the next plot for comparison.



A5.2





'TEMPERATURE (C) 24.0 25.5 28.0 24.5 25.0 27.0 27.5 28.5 z z Y_Z XY XX XX XX XX XX xx z ۲ ^۲ z × z z 2 2.0 Z × z Z 185 DEPTH (METRES) 8.0 A 5.0 4.0 XXY ¥ XY DATE 03 02 76 ZY TIME 1600 HRS Z Y TIME 1700 HRS Y TIME 1800 HRS × TIME 2000 HRS Ж 10.0 12.0

A5.5

175



TEMPERATURE (C) 25.0 26.5 =24.0 = 25.5 25.0 24.5 27.0 27.5 28.0 28.5 ×××× ÷. × × 0. 2 DEPTH (METRES) B.0 6.0 4.0 DATE 05 02 76 × TIME 1530 HRS Ж TIME 1630 HRS 10.01 12.0 TEMPERATURE (C) 26.0 26.5 024.0 0 25.5 28.5 24.5 25.0 27.0 27.5 28.0 . ¥ x 5,0 3 x DEPTH (METRES) ŧ DATE 05 02 76 十翼 Ж TIME 1630 HRS X TIME 1730 HRS TIME 2010 HRS Į 10-0 12.0





A5.9



APPENDIX B: PROGRAM FLOWCHARTS



B1

Flowchart for Program FLUX





B2

Flowchart for the Model LAYER











- 201

SUBROUTINE STEP Compute new thermocline position. Reset TOLD, SOLD Same grid Yes to 'remembered' interval? values. No T_{OLD}, S_{OLD} assume WML Thermocline Yes retreated values. upward? No T_{OLD},S_{OLD} are T, S prior to One grid Yes point entrained? entrainment. No STOP More than one grid point entrained



188



SUBROUTINE NEWTON



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B2.7



SUBROUTINE TURB

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APPENDIX C: PROGRAM LISTINGS

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PROGRAM FLUX (INPUT . DUTPUT . TAPE 1 . TAPE 5 . TAPE 6 . TAPE 7)
       REAL L.K
INTEGER HH
с
        DATA Z3+Z4/3.0+4.0/
DATA CHWNlo+HL+P+CP+G+K/0_00135+2445++1013+25+1010++9+81++41/
        DATA CHW3MX+CC4MX/.00240.,00148/.ZLMAX/-0.99323/
C
        REWIND 1
       REWIND 5
REWIND 6
       READ(1.10) IDATE
   10 FORMAT(16)
READ(1.10) NI
        WRITE(5.10) IDATE
       WRITE(5.10) NI
WRITE(6.10) ICATE
       WRITE(6.10) NI
WRITE(7.10) ICATE
WRITE(7.10) NI
   WRITE(5,12)

12 FORMAT(/,2X,*TIME#+10X,*L+,7X,*Z/L*+6X,*RIBC#+6X,*RIBv*+7X,
      *#CD4#+6X+#CH#3#+/)
        WRITE(6:13)
   WRITE(7+13)
13 FORMAT(/+2X+#TIME#+5X+#ST=ES5#+2X+#SENSIBLE#+4X+#LATENT#+6X+
      *#EVAP#+3X+#FR+VEL+#+/+12X,#N/M2#+2(6X+##/H2#)+6X+#HH/+R#+
      *6X, # 2/5 x , / )
с
                     COPPUTE ROUGHNESS LENGTHS
       CDN10=0.0013
Z0=10.0/(EXP(K/(SQRT(CDN1:))))
ZS=10.0/(EXP(K*K/(CHWN10*ALOG(10./Z0))))
       G1=ALOG(10./20)
G2=ALOG(10./25)
        G3=ALOG(23/25)
        G5=ALOG(Z3/Z0)
       G6=ALOG(Z4/Z0)
С
       PRINT +, # 20, 25, G1-G6 #, 21, 25, G1, G2, G3, G5, G6
С
       DO 100 I=1.NI
с
       READ(1,20) HH.MM.U.AT.WT.CH
   20 FORMAT(5X+212+4F10.2)
                        WIND SPEED AT 2ND LEVEL
С
       U3=U*G5/G6
С
                        NEUTRAL 10M DRAG COEFF.
       IF(U.LE.5.) CDN10=.001
IF(U.GT.5.) CDN10=(1.0+0.67*(0-5.))/1000.
       INITIALISE CREFFICIENTS
CDN4=CDN10+(G1°G1)/(G6+G4)
С
        CDN3=CDN10+(G1+G1)/(G5+G5)
        CHWN=CHWN10*(C1*G2)/(G5*G3)
                                                       .
        CD4=CDN4
        CD3=CDN3
        CHW=CHWN
       PRINT ++ U3=+,U3++CDN4+CCN3+CHWN ++CDN4+CDN3+CHWN
                       ATMOSPHERIC DENSITY
С
       D=1.294+273./(AT+273.)
PARTIAL WATED VAPOUR PHESSURE
[T1=1--373.16/(AT+273.)
С
       T2=1.-373.16/(WT+273.)
                                                                                        15
    :
...
        ES1=SATVP(T1)
       E1=(RH+ES1)/100.
ES2=SATVP(T2)
С
                        SPECIFIC HUNTDITY
        Q=0.662/P*E1
                        VIRTUAL ATP TEMPERATURE
с
       TV=(AT+273.) 0(1.+0.610)
PRINT 0;≠ D;ES1+E1+ES2+0+AT+TV ≠;D+ES1+E1+ES2+0+AT+TV
```

C1

Program FLUX

```
c
c
                            FLUX COMPUTATION/ITERATION
         ZLO=U.
         ICOUNT=1
G0 T0 30
С
    25 CONTINUE
          IF((ABS((ZL-ZL0)/ZL)).LT.0.0001) GO TO 50
         ZL0=ZL
ICOUNT=ICGUNT+1
         IF(ICCUNT.GE.SD) STOP #TCC MANY ITEMATIONS#
С
    30 H=CHW+D+CP+U3+ (HT-AT)
         W=CHWODOUJO0.662/P+(ES2-Ei)
         S=CD4+D+U+U
c
c
                           FRICTION VELOCITY
         UX=SORT(S/D)
         IF (ICOUNT.NE.1) GO TO 45
         HN=H
         ₩N = ₩
         SN=S
         UXN=UX
HLFXN=WN#HL#1000.
         EWN= WN+3600.
    W.C.LENGTH
45 L=-D°UX¢UX°UX°TV/(K°G°(H/CP+n.61°(AT+273.)*₩))
RECOMPUTE TFANSFER COEFFICIENTS
с
c
         ZL=Z4/L
P4=PSIm(ZL)
         C=SQRT(CDN4)
         CD4=CDN4/(1.+CDN4*(P4*P4+2.*K*P4/C)/(K*K))
с
         ZL=23/L
         P1=PSIM(ZL)
         P2=PSIHW(ZL)
         C=SQRT (CDN3)
         CHW=CHWN/(1.+CHWN+(P1+P2-++P2/C-K+P1+C/CHWN)/(K+K))
с
         GO TO 25
c
c
                            COMPUTE BULK RICHARDSUN NO.S AT LEVEL Z3
    COMPUTE BILK RICHARDSON NO.5 AT LEVEL 25

50 RIB1=ZL*(K*C/CHNN-P2)/((K/C-P1)*(K/C-P1))

U3=U*(65-P1)/(66-P4)

PRINT ** CORRECTED U3= ±*U3*± ** ***

PRINT 99*H+*M**ICOUNT

99 FORMAT(/*5X*212*± NO. CF ITEPATIONS ±*I3*//)

RIB2=6*Z3/TV*(AT=WT+0*6)*TV*(A*62/**(E1=E52))//''3*U3)
c
c
   WRITE(5,110) FH,MM,L,ZL,STB1,PIB2,CD4,CHW
110 FORMAT(2X,212,2X,6F10,5)
         JF(ZL.GT.ZLMAX) GO TO 115
H=CHW3MX*D*CP*U3*(WT-AT)
         W=CHW3MX*C*U3*0.662/P*(E52-E1)
   S=CD4MX+D+U+U
115 CONTINUE
         HLFX=W+HL*1000.
         UX=SORT(S/D)
   WRITE(6:120) HH:MM:S.H.HLEX:E:UX
120 FORMAT(2X:212:2X:F10.5:2F10.2:2F10.5)
WRITE(7:120) HH:MM:SN:HK:HLEXX:EWN:UXN
c
   100 CONTINUE
с
         ENDFILE 5
         ENDFILE 6
         END
```

```
FUNCTION SATUP(T) - COMPLTES SATURATION VAPOUR PRESSURE IN MR
с
         SATVP=1013,25+EXP(T*(13.3185+T*(=1+750+T*(=0.6445=1.299*T)))
         RETURN
         END
c
c
c
      FUNCTION PSIM(ZL)
         REAL K
DATA K.A.PI/0.41.5.0.3.1415927/
c
c
         IF(ZL.LT.0.) GO TO 10
IF(ZL.GT.0.) GO TO 20
С
         PSIN=0.
         GO TO 30
С
    10 X=(1.-16.*ZL)**0.25
PSIM=2.*ALOG((1.*X)/2.)**LOG((1.*X**)/2.)-2.*ATAN(X)*FI/2.
G0 T0 30
с
    20 IF(ZL.GT.0.5) GO TO 21
PSIN=-A*ZL
GO TO 25
21 IF(ZL.GT.10.) GC TO 22
PSIM=0.5/(ZL*ZL)-4.25/7L-7.0*ALOG(ZL)-0.852
GO TO 25
22 PSIM=ALOG(ZL)+0.76*ZL-12.593
25 CONTINUE
С
    30 RETURN
         END
C
C
C
         FUNCTION PSIH#(ZL)
         REAL K
DATA K.A.PI/0.41.5.0.3.1415927/
c
c
         IF (ZL.LT.0.) GO TO 10
                                                  ۰.
         IF (ZL.GT.0.) GO TO 20
с
         PSIH#=0.
         GO TO 30
С
    10 X=(1.-16.*ZL)**0.25
PSIH#=2.*ALOG((1.+X*X)/2.)
GO TO 30
С
    20 IF(ZL.GT.0.5) GC TO 21
PSIM=-A*ZL
GO TO 25
21 IF(ZL.GT.10.) GO TO 22
PSIM=0.5/(ZL*ZL)-4.25/7L-7.0*ALOG(ZL)-0.852
GO TO 25
22 PSIM=ALOG(ZL)-0.76*ZL-12.093
    25 PSIHW=PSIM
С
    30 RETURN
         END
                        -
```

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C1.3

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PROGRAM LAYER (INPUT, OUTPUT, TAPE1=64, TAPE2=64, TAPE5=64, TAPE6, TAPE7 CONTOU • . TAPE01 000710 000120 c c C C C MODEL OF THE EPILIMNION MIXING IN A MEDIUM SIZE RESERVOIR. 000140 000150 000160 000176 EXTERNAL DIFF EXTERNAL UIFF LOGICAL OK+PRESS REAL INT INTEGER DDD0+FH0+DDD1+HH1;CD(20),CH(20)+CM(20) COMMON/SHQL7ZH,ZL+TS+US+S4-ES+H+TT)+TCLD+JQLD,TULD+S0LD+T1+S1+Z1 COMMON/STRUCTTT(2000)+S(2000) COHMON/FLUX/A(6)+INT+BRB(S) 000180 000190 000200 000210 000220 000230 COHMON/PARAH/C1+C2+C3+C4+C5+AL+8+CP+D+A1+81+A2+82+A3+83 000540 COMMON/UNPIX/NFLAG.MFLAG.PGRAD COMMON/JUPP/ST.SECEND.GRID 000250 COMMON/COUNT/ICOUNT + ADVECT + WW + TIME 000570 00280 С DATA ICOUNT, NFLAG, N/1+0+1/, MFLAG/0/+LFLAG/0/ DATA IBOM8+PRESS/0++FALSE, /+PGRAD/0+0/ DATA ST. MODI/0 -0 / 000100 000110 DATA ST. HODT/0. . 0./ С 000,30 REVIND 1 000-40 REVIND 2 000350 REWIND 5 000160 REWIND 6 000370 REWIND 7 000180 REWIND B 000390 с ¢ 000400 ENTER DATES AND TIMES 000410 C READ(1,5) DDD0, HH0, MM0, DDn1, HH1, HM1, DELT, NCHECK 000750 5 FORMAT (2(2X, I5+)X, 2I2), 3X, F5, 2, I5) READ(1,10) (CC(J), CH(J), CM(J), J=1, NCHECK) 10 FORMAT(I5+1X, 2I2) 000330 00040 000450 000260 С CALL START (DODD + HHO + MMO) 000370 CTIME=TIMES(CD(1),CH(1),CV(1)) 000480 ETIME=TIMES(DOD1+HH1+MH1) 000290 000-00 с с ENTER INITIAL WAL PARAMETERS PLUS OTHER CONSTANTS 000=10 100520 Ċ READ(1,15) T5.55.E5.US.ZF.ZL.NPT5.GHID.IINT 15 FORMAT(2F6.3.F8.8.3F8.3.17.F8.3.15) 000=30 000-40-READ(1,20) C1,C2,C3,C4,C5,AL,B,CP,U 20 FOPMAT(9FB.4) READ(1,25) A1,B1,A2,B2,A3,B3 000=50 000-60 000=70 000-80 25 FORMAT (6F10.4) 000590 С č LOAD THE TEMPERATURE AND SALINITY GRIDS 000200 000410 CALL LOAD (NPTS . GRID) 000+20 с INITIALISE PARAMETERS 000430 c TIME=TIMES(DDC0,HH0,MMA) ITIME=TIME/IINT-1 000440 000450 SECINT=DELT/8.0 000450 TSTEP=DEL1/8.0 INT=ISTEP/60.0 000470 000+80 SINT=DELT+0.00005 000290 ZLOLD=ZL 000700 H=ZH-ZL ... ADVECT=0.0 000720 000730 c c 000750 START OF LOOP с 100 CONTINUE 000760 000770 IF (ICOUNT.ED.1) GO TO 101 000780 С CHECK COMPATIBILITY OF DEEPENING PATE. INTEGRATION RANGE A 000790 с с GRID SPACING. HALVE OF DOUBLE INTEGRATION RANGE. 1F(LFLAG.EG.1) GO TO 121 IF(((TNEXT-TIME)*60.).LT.NELT) GO TO 122 000000 000610 000020 IF (111NCAT=11FC)+004.1.C1+NCLT1 00 10 12 IF (WW+LE+0.0.4ANC+MFLAG,EG,D) GO TO 122 GO TO 104 121 LFLAG=0 122 TSTEP=DELT+0.125 0000030 000440 000A50 000060 GO TO 103 000é70 104 IF (TSTEP.GT. (0.95+DELT)) no to 102 IF ((ZLOLD-ZL).GT. (0.2*GRIn)) GO TO 102 0000080 000090 TSTEP=TSTEP+TSTEP 000000 GO TO 103 102 IF(TSTEP.LT.(0.15*0ELT)) GO TO 163 000010 000020 IF (IZLOLD-ZL).GT. (0.8"GHID)) TSTEP=TSTEP+0.5 000030 103 INT=TSTEP/60.0 000640 IF(SECINT.GT.TSTEP) SECINT#TSTEP 000050 000660 ZLOLD=ZL 101 TIME=TIME+INT 000976

C2 Program LAYER

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С 000c80 COMPUTE INSTANTANEONS WETECRELIGAL FLUXES CALL FLUXES(ICOUNTITIME: MODT:ST.TNEAT) SECEND#ST.TSTEP Ċ 00990 001604 Colole RESET ENTRAINED GRID POINT VALUES с 001024 IF (ICOUNT.NE.1) CALL STEP (GPID) 001<u>0</u>30 001<u>0</u>40 С Ċ SOLAR SHORTWAVE HEATING OF ALL GPINPOINTS 001050 CALL SOLAR (TSTEP, GRID) 001660 С CO1070 CO1070 Ċ COMPUTE SIGMA (ENTRAINNENT POWER PARAMETER) CALL SIGMA(WW) IS THE LEVEL OF THE STILL +VE+ C01090 001100 с IF (W.GT.0.3) GG TO 40 IF (ES.LT.1.0E=10) GO TO 39 001110 ES32=SORT (ESPES*ES) 001130 DECAY=-((***-(C2+C3)*ES32)/H)*TSTEP IF(DECAY+LT+(0.5*ES)) GO tO 40 001<u>1</u>40 001<u>1</u>50 001<u>1</u>60 PRINT 38, TIME, ES, OECAY 38 FURMAT (/, 5X, #TIME #, F10.1, # ES#, E12.3, # DECAY#, E12.3) 001170 c c THE HAS DECAYED TO ZERO ; ITERATE A NEW H. 001190 39 T(JOLD+1)=TS 001200 5 (JOL D+1) = 55 US=0.0 001320 ES≂0.0 001230 ADVECT=0.0 001240 CALL NEWTON NFLAG=1 001260 IF (H.GT.0.05) GC TO 40 001570 H=0.05 001280 ZL=ZH=H С 001 100 č 001-10 c c SOLVE WPL EQUATIONS BY RUNGE KUTTA METHOD 001 20 001 30 40 CALL MERSI(ST.SECEND, 6.0. 000) SECINT, SINT, 0.0K, OIFF) 001340 IF (OK) GO TO 128 001-50 PRINT 127, TIME 127 FORMAT(//,5X, #TIMESTEP DIVISION LIMIT REACHED AT #,F10.1,//) PRINT +,# ST=#,ST,# ECEND=#,SECEND STOP 001-60 001-70 001-80 001-90 CECEND= # , SECEND С 001200 128 IF(ZL.LE.GRIO) STOP#MIXED TO BOTTOM OF LAYER# WRITE(7,976) TIME,WWYES'SFCINT,SECEND 976 FORMAT(SX.F12.1.2E12.3.2F15.0) UPDATE GRIC VALUES 001410 001430 001440 001450 001460 С H=2H-ZL J1=ZL/GRIO J1=J1+2 001 - 70 JJ=ZH/GRID 001280 001290 JJ=JJ+1 DO 130 J=J1,JJ 001200 T(J)=TS 130 S(J)=SS 001220 с 001=30 IF (NFLAG.NE.1) GO TO 133 001240 TJUMP=0.0 001=50 SJUMP=0.0 001=60 001=70 GO TO 134 133 CALL JUMP (SECEND, TJUMP, SJUMP) PRINTOUT FULL GRID STRUCTURE AT TIMES SPECIFIED 001280 С 001290 С 001 + 00 134 IF((TIME-CTIME).LE. (-0.4*TNT)) GO TO 200

 134
 IF((TIME-CTIME).LE.(-0.4*TNT)) GO TO 200
 001410

 WRITE(6,137)
 CO(N), CH(N), CM(N), TIME
 00120

 137
 FORMAT(1H1,//,5X, #MODEL DROFILE FOH DAY & TIME#, I4+1x,2I2,3X.
 001420

 14MODEL
 TIME#, I4+1x,2I2,3X.
 001440

 wRITE(6,138)
 ZH-2L, H+T<<\$5<,ES<US</td>
 001450

 138
 FORMAT(/,5X,#ZH=#,F6.3,3X,#ZL=#,F6.3,3X,#H=#,F6.3,3X,#TS=#,F5.2,3XC01460
 01470

 1.#SS=#,F6.2,3X:#ES=#*EI0.3,3X:#US=#*F6.4)
 001470

 wRITE(6,139)
 TJUMP,SJUWP
 001480

 129
 FORMAT(/,5X:#TUMP=#*,F6.2,3X:#SJUMP=#*,F6.2,//,4X)
 001290

 1400700
 14070001700
 001700

 001+10 001490 1#HEIGHT#,5X,#TEMPERATURE#,6X,#SALINITY#) 2=0.0 001710 DO 160 K=1,JJ,4 001720 WRITE (6,150) 2,T(K),S(K) 150 FORMAT (4X,F6.3)10X,F5.2,5X,F6.2) 001740 001750 00176° 001770 160 Z=Z+4.0°GRID N=N+1 IF (N.GT.HCHECK) GO TO 500 CTIME=TIMES(CD(N)+CH(N)+CN(N)) 001780 . .

	с			001790
j.	C	COMPUTE THERMOCLINE IT IT OVER 2NM IF LAYER IS DEEPENING		001000
	200	JF (NFLAG.E0.1) GO-TO 250		001419
		ADVECT=ADVECT+H4US#TSTFP		001020
		TILT=ADVECT+0.GO2		001030
	С	DIMENSIONLESS DENSITY JUMP		001440
		DELRHQ=AL*TJUMP		001450
	C	PRESS GRADIENT/RHOD CUER IKH HALF		001960
		DPDX=9.A1*DELRHG*TILT/100A.		001070
	C.	COMPARE STRESS AND PRESS GRADIENT		C01e80
		IF((A(6)*A(6)).GT.OPDX) Gn Tn 215		001=90
		IF (PRESS) 235+210		001000
	210	PGRAD=2,*CPDX		001410
		LFLAG=]		001420
		PRESS=.TRUE.		001430
		PRINT 4, # PRESSURE GRADIENT ON AT FITIME		001040
		60 10 235		001450
	215	15 (DDEcc) - 220, 235		001060
	220			001070
	220			001080
		DOTAT A P DRECSHOF GUARTELT AFF AT A TIME		001400
	275	PRINT WAR PREDUCE ORBUIEN OF AN EXITE		002200
	r 235	CONTINUE		002010
	ř P	RINT A SUMMARY WHEN LAYER OFEPENS		002620
	č	atel a boundar nort militer frem no		002030
	U	WRITE (5,24m) TIME. ZH.ZI .F. TS. SS. US. ES. WW. TJUMP. SJUMP. PGRAD		002640
	240	FOPMAT(1X,7F9.3,2F12.3,2F9.2,F12.3)		002750
		GO TO 300		002060
	с			002770
	Č P	RINT A SUMMARY WHENEVER LAVER PETREATS		002680
	ċ			002290
	250	WRITE(5+255) TIME, ZH, ZL, H, TS, SS, US, ES, WH, TJUMP, SJUMP		002100
	255	FORMAT(1X:7F9.3:2E12.3,2F9.2)		002110
	с			002120
	300	CONTINUE		002[30
	с	*		002140
	с р	RINT FLUXES		002150
		FL3=A(3)*3600000		002160
		FL6=A(6)/0,0343		002170
•		WRITE(0,270) TIME,A(1),A(2),FL3,A(4),A(5),FL6	-	002180
	270	FORMAT(3F10,1,F10,5,2F10,1,F10,5)		005140
	C R	ESET MODEL PARAMETERS AND CHECK TIME	•	005500
	¢			002210
		IF (MFLAG.E0.1.ANU.NFLAG.E0.0) 60 10 350		002220
		GO TO 380		002330
	350			002240
		IF (2L0[0.eT.2L) 60 10 38C		002250
	200	60 10 390 NELIG-NELAO		002200
	200			002580
	290	NELADES VELICETUES IT INT, CO TO ESS		002200
		TENTRETACTIVE (CONTA)		002200
				002310
	c	calatus -		002-20
	2			002330
	čτ	HATS IT FOLKSV		002-40
	č	And the second sec		002-50
	5 00	FNDFILF 5		002160
	200	ENDETLE 6	5	002370
	,	ENDEILE 7		002-80
	!	ENOFILE B	2.12	002-96
		PRINT SIGILCOUNT		002400
	510	FORMAT (// 5X, #FINAL ICOUNTE #.18)	-	002410
	Ċ	· · · · · · · · · · · · · · · · · · ·		002420
	-	END		002330
				-

~	SUMPOUTINE DIFFITIME, THUES	002488
	SUBBOLITINE CONTAINING THE D.E. S. FOR SOLUTION	002.4
ž	SOMOOLINE COMMINING THE STEAD FOR SECONDA	0021
L.	OTHENSION YDOT(6)	0.0218
	COMMON/WHI /OUWNY (6) +H+TT1. TTOL 0 + IOL()+TOLD+SOLD+T1+S1+71	002481
	COMMON/OFS/2H+7L+TS+US+SS.FS	C 0 2 4 6 8
		002418
	COMMON/FLUX/A(6)	002
	COMMON JUNN IX JAFLAG + MFLAG + PGRAD	0024
	COMMON/COUNT/I + AOVECT + WH + RTIME	002646
c		00266
•	DATA CC1/0.333333333/.G/9.A1/	00246
c	••••	002178
•	H=7H=71	00268#
c	COMPUTE INSTANTANEOUS FLUXES	0.02486
U.	CALL IFLUX (I + GUP1 + TIME + SCUM + DUM2)	0.02486
c		0.02414
č	HAS LAYER RETREATED.	002425
•	IF (NFLAG.NE.1) GO TO 50	002436
	19 YOOT(2)=0.0	002440
		00245
	YDOT(4) = 0.0	002460
	US=0.0	0.02,78
	YOOT(6)=0.0	002480
	ES=0.0	002491
	GO TO 20	002760
С		002710
с	COMPUTE TEMP A SAL JUMPS AT BOTTOM OF WML	002770
	50 CALL JUMP(TIME,TJUMP,SJUMP)	002730
ċ	COMPUTE SURFACE INPUT POWER	002740
	CALL SIGMA(WW)	002754 "
С		002760
С	TKE FLUX	002770
	IF(ES.GT.0.0.CR.WW.GT.0.0) GO TO 45	002780
	NFLAG=1	002790
	PRINT ●9≠ ENERGY OECAYFO AT TIME ≠9RTIME	002800
	ADVECT=0.0	002010
	GO TO 19	002020
	45 ES32=SQRT(ES+ES+ES)	002p30
С	COMPUTE THE DERIVATIVES	002,40 2
С		002 <u>4</u> 50
	30 YOOT{2}=CF+E532/(CS+U5+U++B+G+H+SJU ^k P+AL+G+H+TjUhP+ES)	002 <u>9</u> 60
	UE = Y00T (2)	002p70
	31 YOOT(6)=(#W-(CF+CE)*ES32)/H	.002,80,
	32 CONTINUE	002090
С	· · · · · · · · · · · · · · · · · · ·	002900
С	IS MIXING ESTABLISHED WELL ENOUGH TO INCLUGE SHEAR +	002c10
	IF(HFLAG.EG.1) GO TO 15	005450
	YOOT(4)=(A(6)*A(6)+US*UF:/H-PGRAO	002c30 🛔
	GO TO 20	002940
	15 YUU1(4)=0.0	002950
	20 YOOT(1)=A(3)	002960
	YOOT(3) = (TJUHP+UE=1.0/(D*CP)+(A(1)+A(2)+A(5)+A(4)+	002970
	1(1,-W(ZL+2H)))/H	002980
-	TUDI (3) # (SJUMP #UE+A (3) #SS) /H	002990
С		003000
		003010
	CNU	003050
		4

C2.4

_	SUBROUTINE LOAD (NPTS . GRIC)	003n30
с с	SUBHOUTINE TO LOAD ALL GOLG POINT VALVES (TEMP & SAL) FROM SPECIFIE	003450
C C	INITIAL STRUCTURE.	003760 003770
-	DIMENSION HT (20) TEMP (20) .SAL (20)	003780
	COMMON/WHL/2H, 2L, TS, US, SS, ES, H.TT1+TTOLD, JOLD, TOLD, SULD, T1+S1+21	003890
	COMHQN/STRUCT/T(2000)+5(2000)	003100
с	· · · · · · · · · · · · · · · · · · ·	013110
Ċ	READ THE SPECIFIED INITIAL STRUCTURE	003120
-	READ(1,10) (HT(K),TEMP(K),SAL(K),K=1,NPTS)	003330
	10 FORMAT(F5.2,2F10.1)	003140
	IF (EOF (1)) 11+12	003150
	11 STOP #EOF IN INITIAL STRUFTUPE FILE#	203760
	12 1F(HT(1).NE.0.0) STOP #INITIAL STRUCTURE SPECIFIED INCORRECT#	003170
С		003]80
Ċ	LOAD THE GRID	003190

С		003500
	7≠ā_0	003510
		003-26
		003330
		003240
		003350
<u>م</u>		003360
Ċ,	20 JE (Z. LE. (HT (K.))+0.01468 to)) 60 TO 30	003570
		003280
	1517.65.71 X 60 TO 20	003596
	= 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1	003-00
	SDASH2 (SA) (K+1) = SA (K) / (SA (K+1) = ST (K))	003-10
	GO TO 20	003-20
r		003-30
v	30 T(1)=TEMP(K)+(7=HT(K))/(HT(K+1)=HT(K))*(TEMP(K+1)=TEMP(K))	003240
	S(1) = SA(1/K) + (7 = HT(K))/(HT(K+1) = HT(K)) = (SA(1/K+1) = SA(1/K))	003350
		003260
		003970
	IFIK-FO-NETSI STOP ZION ZANY POINTS LOADERZ	003-80
	1F (7-GT-7HH) GO TO 50	003-90
	60 10 20	003200
r		003410
U.	50 K≖K+1	003420
	J=. - 1	003430
	PRINT 60. J.K	003240
	60 FORMAT(/+5X+14+# GRID POINTS LOADED FROM #+14+# LEVELS#)	003450
r		003460
č	RESET WHI BASE TEMP A CAL	003270
•	JEZI / GOID	003480
		003290
	T(1+1) =T(-1) + TCASH+GRID	003500
	(+1) + (-1) +	003510
		003~20
r		003430
Č.	RETURN	003=40
	END	003550
		¥

	SUBROUTINE FLUXES (I+T+TM+ <t+thext)< td=""><td>003-60</td></t+thext)<>	003-60
		C03=76
	; SUBROUTINE TO COMPUTE METEOROLOGICAL FLUXES BY LINEAR INTERPOLATION	003=8n
	BETWEEN KNOWN VALUES.	003-90
l l		003490
	DIHENSION F(2,6),FT(2)	003410
	INTEGER FC+FH+FM	003428
		003430
		003440
	ETRET THE THROUGH, HEID IN FURTH CLUYES	003450
	PIRST THE INCOUNT READ IN KNOWN FLOKES.	003460
,	TELL NE 11 GO TO 10	003470
		084600
		003490
	5 FORMAT (15-1) - 21 - 25 F10-2)	003700
		003710
	3 STOP #EMPTY FLUX FILE#	003720
	4 FT (K) = TIMES (FD, FH, FM)	003340
-	6 CONTINUE	003350
	TNEXT=FT(2)	003760
C		003770
	IF(T.GE.FT(1)) GO TO 10	003780
	PRINT 7,T,FT(1)	003790
	7 FORMAT(/+5X+≠MODEL TIME≠+F10.1+≠ PRECEEDS FIRST FLUX RECORD AT≠+	003àCO
	lflö.lø≠ minutes≠)	003álu
	· ·	
	STOP	003020
	INTERROLATE FOR FLUXES A TURE COORECT INTERNAL	003,30
	INTERFULATE FOR FLOXES WITHIN THE CORRECT INTERVAL	003040
L L L	10 IE/T LT (ET/2)+0 001)) 60 TO 30	003050
		003460
		003070
	15 F(1,J) = F(2,J)	003480
	READ(2.5) = FD = FH = FH = (F(2.5)) = J = 1.5)	003,000
	IF (EOF (2)) 16.17	003010
	16 STOP #INSUFFICIENT RECORDS IN FLUX FILE#	003620
	17 FT (2) = TIMES (FC + FH + FM)	003930
	TNEXT=FT(2)	003640
· · ·	ST≖0.0	003050
	GO TO 10	003660
. · . C		003670
	30 IF(I.EQ.1) ST=((T-TINT)-FT(1))*60.	003480
	DO 40 J=1,5	003990
• • • • •	40 B(J)=F(1,J)+((T=TINT/2,)T(1))/(FT(2)-FT(1))+(F(2,J)-F(1,J))	004ñ00
· C	WHERE B1=SPEED,B2=A.TEMP,B3=q.H.,B4=L.*.IN,B5=S.W.IN	004_010
· · ·	60 10 200	004120
· · · · · · · · · · · · · · · · · · ·	ENTRY TELLIN	004130
	DO 50	004140
	50 50 54175 50 51 1145/1. 114/10/2011/10/257/11/9/5/3. 11-5/1. 111	004050
	30 0(3)+************************************	004060
	60 4(3)=4(3)/(1000_)	0104010
		004000
·.	QL0=5.669E-80.96+(TS+273)+44	0040400
	$A(5) = Q_{L}O + B(4)$	004110
	A(4)=8(5)	004720
ċ		004130
	/ RETURN	004140
	END	004150

```
203
         SUBROUTINE STEPIGEID)
                                                                                             004160
004179
 С
      SUBROUTING TO RESET WHL MASE TEMP A SAL VALUES TO FACILITATE COMPUTATION OF GRADIENTS BELOW THE MAL
 c
c
                                                                                             004184
 č
                                                                                            004200
         COMMON/STRUCT/T (2000) +5 (2000)
         CONMON/WHL/ZH:ZL:TS:US:SS:ES:H:TT1:TTOLD:JOLD:TULD.SOLD:T1.S1.Z1
                                                                                             004270
 c
                                                                                            004330
004240
004250
         J#71/GPTD
         J≃J+l
        J=J+1

IF(J+EQ+JOLD) GO TO 10

IF(J+GT+JCLD) GO TO 30

IF(J+EQ+(JOLD+1)) GO TO 57

STOP #ENTRAINED MORE THAN I GRIDPO[NT#
                                                                                            C04260
004278
                                                                                            004280
                                                                                            004790
 С
                             - 72
     10 T(J+1) = TOLD
                                                                                            004110
        S(J+1) ×SOLD
RETURN
                                                                                            004-20
                                                                                            014330
 С
                                                                                            004-40
    30 JOI 0=J
                                                                                            004-50
        RETURN
                                                                                            004-60
 ċ
                                                                                            004370
    50 JOLD≏J
        T(J+1)=T1
                                                                                            004390
        S(J+1)=S1
        RETURN
                                                                                            004410
        END
                                                                                            004420
        SUBROUTINE SOLAR (TINT+GRID)
                                                                                            004430
С
                                                                                            004440
004450
С
      SUBROUTINE TO INPUT HEAT TO ALL GRIDPCINTS FROM SOLAR SHORTWAVE
С
        RADIATION ABSORPTION
                                                                                            004260
Ċ
                                                                                            004470
        COMMON/FLUX/A(6)
                                                                                            004480
004490
        CONHON/WHL/ZH,ZL,TS,US,SS,ES,H,TT1.TT0LD,JOLD,T0LD,SDLD+T1,S1.ZI
        COMMON/STRUCT/T(2000) +5(200)
COMMON/PARAM/C1+C2+C3+C4+C5+AL+B+CP+D+A1+B1+A2+H2+A3+B3
                                                                                            004500
с
                                                                                            004=20
        TT1=T(JOLO)
                                                                                            004230
        TTOLO=T(JOLD+1)
                                                                                            004540
С
                                                                                            004550
c
c
          HEAT ALL GRIOPOINTS FRCM THE BOTTOM UP
                                                                                            004560
                                                                                            004570
004580
        JJ=ZH/GRID
        JJ=JJ+1
D0 20 J=1+JJ
Z=(J=1)*GRID
                                                                                            004298
                                                                                            004400
                                                                                            004410
    T(J) = T(J) = TINT*A(4)*ODASH(Z,ZH)/(D*CP)
20 CONTINUE
                                                                                           004420
004430
с
                                                                                            004440
        T1=T(JOLD)
                                                                                           004450
        TOLD=T(JOLD+1)
S1=S(J0LD)
                                                                                            004460
                                                                                           004670
        SOLD=S(JOLD+1)
                                                                                           004480
        Z1=(JOLD-1)*GRIO
                                                                                           004490
ć
                                                                                           004700
004710
       RETURN
       END
                                                                                           004720
        SUBROUTINE SIGMA(WW)
                                                                                            004930
c
c
                                                                                           004740
            SUBROUTINE TO COMPUTE THE SURFACE INPUT POWER
С
                                                                                           004760
004770
004780
        COMMON/FLUX/A(6)
        COMMON/PARAM/C1,C2,C3,C4,C5,A1,8,CP+D,A1,81,A2,82,A3,83
COMMON/PML/ZH,ZL,T5,U5,S5,E5,H,TT1,TT0LD,J0LD,T0LD,S0LD,T1,51,Z1
                                                                                           004790
ċ
                                                                                           004000
        H9= (A (1) + A (2) + A (5) ) + A (4) + (1. 0+Q(ZL+2H) -QQ(ZH+ZL))
                                                                                            004410
        W9=(9.81*AL*H)/(D*CP)*H9=(9.81*8+H)*A(3)*55
                                                                                           004020
       ₩#=(₩9+(C1+A(6)) **3)
                                                                                           004630
с
                                                                                            004648
       RETURN
                                                                                           004#50
       ENTRY NEWSIG
                                                                                           004660
C
C
C
                                                                                           004 470
     THIS SECTION COMPUTES THE CERIVATIVE OF SIGNA USING THE PREVIOUSLY
                                                                                           004680
       STORED VALUE CF H9.
                                                                                           004:90
č
                                                                                           004900
         ##AL*9.81/(D+CP)*(-H9-A(4)*(-QDASH(2L+ZH)*H+GQ(ZH+ZL)-2.0*
                                                                                           004616
      10(ZL+ZH1))+B+5+81+A(3)+S5
                                                                                           004020
с
                                                                                           004030
       RETURN
                                                                                           004940
```

END

	204	
	SURROUTINE NEWTON	004060
с с с	SUBROUTINE TO ITERATE A NEW SOLUTION FOR ZL SUCH THAT SIGNA . 0. USES A NEWTON RAPHSON PROCEDURE.	004970 004980 004990
c	CONHON/WHL/ZH,ZL.TS,US.SS,ES,H.TT1.TTOLD.JOLD.TOLD.SOLD.T1.S1.Z1	005010 005010
с. С	DATA ACC/0.0005/	005730
Ŭ	Isi	005750
	10 CALL SIGHA(FZL) CALL NEWSIG(DFZL) ZLNEW=ZL-FZL/CFZL IF(A95((ZLNEW-ZL)/ZL)/LE.ACC) G0 T0 20 I=t+1	005760 005770 005770 005740 005700
	IF(I.GE.50) STOP #TOO MANY ITERATIONS# ZL=ZLNEW H=ZH-ZL	005110 005120 005130
с	GU TU 10	005140
•	20 ZL=ZLNEW	005160
	RETURN	005170
•	END	005190
	FUNCTION TIMES (D+H+M)	005200
c	FUNCTION TO CALCULATE HODEL TIME (HINUTES AFTER START).	005210
c	INTEGER D+H	005230
د ح	T1HES=H+60+ (H+24#D)-ST	005350
c	RETURN	005280 005290
с	ENTRY START	005-100
ŕ	ST±N+60*(H+24*D) TIMES=ST	005120
	RETURN END	005150
	FUNCTION Q(Z+ZH)	005-170
с с	FUNCTION FOR FRACTION OF SHORTWAVE PENETRATIING TO 2.	005-80 005-90
c	COMMON/PAFAM/C1,C2,C3,C4,75,AL,B,CP,D,A1,B1,A2,B2,A3,B3	005400 C05410
С	X=Z-ZH	005420
	0=a1*PEX(81+X)+A2*PEX(82+x)+A3*PEX(83+X) Return	005ã40 005ã50
	END Function QDASH(Z+ZH)	005460
000	CALCULATES DO/DZ FOR HEAT APSORPTION CALCULATION	005480
c	COMMON/PARAM/C1,C2,C3,C4,C5,AL,8,CP+0,A1,81,A2,82,A3,83	005-10
	X=Z-ZH 'QDASH=A1+81*PEX(81,X)+A2*p2*PEX(82+X)+A3*83*PEX(83+X)	005230
	RETURN END	005550
с	N FUNCTION VQ(2094L)	005580
, c c	CONMON IDADALICS CO.	005400
Ċ	UUNNUNYTAN AMJUISUZEUSSUTEUSSATEUSSUTEUSSATESUTEUSAISUTEUSAISUTEUSAISUS	005420
	GO=-2.0/X*(A1/B1*(1.=PEX(PI+X))+A2/82*(1.=PEX(B2+X))+ 1A3/B3*(1.=PEX(B3+X))) RETURN END	005440 005450 005460 005470
	FUNCTION PFX(P.X)	005480
. c	COMPUTES EXPONENT IF ARGUEMENT NOT TOO SHALL	005490
v	Υ×8+χ	005710
	IF(T.GT.=<25.) GO TO LV PEX=0.0	005720
	RETURN	005740
	RETURN	005760
	END	005770

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.4
	SUNROUTIN	E MERSI (X+XEND+N+ACC+H+HMIN+JTEST+OK+DIFF)	005780
c c	CERN LIBR	ARY NO D. 208.	005790 / 005400
C C	REVISED VI	ERSICN JULY 1971.	005#10 005#20
Ċ	THIS VERS	ION OF MERSON IS A MODIFICATION OF THE PROGRAM RECEIVED	005a36 005a40
Ċ	FROM KJEL	LER COMPUTER INSTALLATION MORNAY.THE MAIN DIFFERENCE CHANGE OF THE TEST FOR STEPLENGTH HALVING.	005650 005660
č			005470 005480
č	PURPOSE =	STEP BY STEP INTEGRATION OF A SYSTEM OF FIRST ORDER	005490 005600
č		DURING THE PARTY AND	005910
c		WITE AUTOMATIC BORDA CONTROL USING THE RETHED DUE TO	005030
c		MERSON.	005650
с с	PARAMETER	5	005670
с с	X =	START VALUE FOR THE DOMAIN OF INTEGRATION (INPUT POINT)	.005490
с с	XEND = Y =	END VALUE FOR THE DOMAIN OF INTEGRATION (OUTPUT POINT). ARRAY CONTAINING THE DEFENDENT VARIABLES. HEN ENTERING	006010
с с		THE ROUTINE THE FUNCTION VALUES YK(X),K=1(1)N AND WHEN RETURNING TO THE CALLING PROGRAM THE COMPUTED FUNCTION	006020
с с	N =	VALLES YK(XEND).K=1(1)N. THE NUMBER OF DIFFERENTIAL FQUATION,EQUAL OF LESS 100.	006740 006750
č	ACC =	PRESCRIBED RELATIVE ACCURCY (TO BE OBTAINED FOR ALL FUNCTION VALUES IN THE ARMAY Y).	006860 006870
č	H = HMÍN ⊒	INITIAL STEPLENGTH. ABSCLUTE VALUE OF MINIMUM STEPLENGTH WANTED.	006ñ80 006ñ90
č	JTEST =	TEST PARAMETER BELATED TO THE STEPLENGTH IN THE FOLLOW	006100
č		JTEST = 0 . IF DURING THE CALCULATION WE GET	006120 006130
č		STEPLENGTH) THEN AN ERROR MESSAGE IS PRINT-	006140
c		TURN TO THE CALLING PROBAM.	006160
с С		WILL CONTINUE WITH THE FIVED STEPLENGTH HMI	N006780
	THE FOLL LOGICAL OF	WING LINE INSERTED F.J.WRIGHT 26/02/74 TO ALLOW COPULA	006200
C C	0K =	TERING THE ROUTINE THE VALUE LATER IS DEPENDING OF JTES	1006220
c c		IN THE FOLLOWING WAY JTEST = 1 ; OK = .TPUE. ALWAYS.	006240
с с		JTEST = 0 • OK + .FALSE. IF THE STEPLENGTH RECOMES TOO SMALL (SEE DESCRIPTION FOR JTEST).	006250
c	DIFF =	USER SUPPLIED SUBROUTINE FOR THE CALCULATION OF THE RIGHT HAND SIDES OF THE SYSTEM OF DIFFERENTIAL EQUATION:	006270 5006280
Č.		(I.E. THE FIRST ORDER DERIVATIVES) .CALLING SECTIONCE	006990
			•
с	•	CALL DIFF (XINIFI , WHERE	006300
č		X = THE CURRENT VALUE OF THE ARGUMENT = AN ARRAY WITH THE ELEMENTS WK(X),K=1(1)N I.E. THE	006110
č		FUNTION VALUES FOR WHICH THE DERIVATIVES ARE TO BE	006330
č		F # AN ARRAY WITH THE ELEMENTS FK(X) +K=1(1) K (WE HAVE	006350. 006360
c j		BY DIFF AND RETURNED TO MERSON.	006-70
č,		STATEMENT IN THE PROGRAM CALLING HERSON,	006190
Ċ.	THE ARRAY	S IN THE COMMON BLOCK BELD + ARE ONLY USED INTERNALLY IN	006410
с ¢	THE MAXIM	ND DIFFY AND ARE TO FREE DISPUSAL OUTSIDE REFSON. UM NUMBER OF EQUATIONS WHICH MAY BE INTEGRATED ARE 100.	006430
c c	COMMON BL	ER MAY RE CHANGED BY CHANGING THE DIMENSION IN THE Ock below accordingly.	006450
с	DIMENSION	YZ (6) +A (6) +B (6) .F (6)	006470
c	COMMON/WM	L/ Y(6)	006480
с	COMMON/DE	\$/ w(6)	006=00 006=10
č	RZERO IST	A NUMBER WITH A WAGNITUDE OF ORDER EQUAL TO THE NOISF THE MACHINE I.E. IN THE RANGE OF THE ROUNDING OFF EPPORS	006=20 .006=30
č	DATA S7FD	0 / 1.6-13 /	00640 006450
c	CHECK MIN	RER OF FOUNTIONS FOUND OR LESS THAN 100.	006260 006270
c	TE IN -T	NEAL OF THE RECEIPTE ON CESS THEM 1004	006680 006690
c	AF INAGIA	1007 00 10 00	006400
c	UK=,TRUE.		006420
с	STOPE INT	ERNALLY PARAMETERS IN LIST	400k-10

,

c 0044** tiiv≖N 00 1 K#1+5N 006688 W(K)=Y(K) 1 006478 - --Z≈X 006481 ZEND¤XFND 006496 BCC=ACC 006908 ZMIN=HMIN ITEST#JTEST ×Η 006931 ISWH#0 С 006355 2 HSV=S 006948 IF (HSV.GT.RZERO) GO TO 4 PRINT 3 FORMAT (# ***** SUBROUTINE MERSON - STEPLENGTH LESS THAN MACHINE RODOS 3 IUNDING ERROR LEVEL ****** C06468 STOP 006415 COF = ZENC - Z IF (ABS(S).LT.ABS(COF)) Gn TO B 006426 006438 S=COF IF (ABS(COF/HSV).LT.RZERC) GO TO 50 00644 0064% • ----с с с 006#76 006## IF ISHH=1 THEN S IS EQUAL TO MAXIN'IM POSSIBLE STEPLENGTH WITHIN THE REMAINING PART OF THE DOMAIN OF INTEGRATION. 006499 ċ 006900 8 DO 10 K=1+NN 006616 10 YZ(K)=W(K) 006924 12 HT=,3333333333333333*S 006938 с 006945 CALL DIFF(Z,F) 006950 Ċ 006948 Z=Z+HT 006070 DO 20 K=1+NN A(K)=HT+F(K) 006980 006990 20 W(K)=A(K) +YZ(K) 007-06 С 007616 CALL DIFF(Z.F) 007620 С 0.07030 D0 22 K=1+NN 007040 A(K)=.5+A(K) 22 W(K)=.5+HT+F(K)+A(K)+YZ(K) 007650 007664 С 007:70 CALL DIFF(7.F) 007680 007690 ٤ Z=Z+.5+HT 007104 D0 24 K=1+NN B(K)=4,5*HT*F(K) 007110 007120 24 W(K)=.25*B(K)+.75+A(K)+YZ(K) 007130 с 007140 CALL DIFF(Z,F) 007150 С 007160 Z=Z+.5+5 D0 26 K=1+NN 007176 007180 A(K)=2.+HT+F(K)+A(K) 26 W(K)=3,+A(K)-B(K)+YZ(K; 007200 Ċ 007210 007220 007230 CALL DIFF(Z,F) с D0 28 K=1+NN 007240 i B(K)=-.5*FT*F(K)-B(K)+7.*A(K) W(K)=W(K)-B(K) 17 007260 A(K)=485(5.*8CC**(K)) 007270 B(K)=ABS(2(K)) IF (ABS(W(K)).LE.RZERO) 60 TO 28 007590 IF (B(K), GT, A(K)) GO TO 60 007:00 28 CONTINUE 007310 С 007 120 007 130 c c REQUIRED ACCURACY OBTAINED FOR ALL COMPUTED FUNCTION VALUES. 007:40 IF (ISWH,ER.1) GO TO 50 007:50 C C C 007-00 TEST IF STEPLENGTH DOURLING IS POSSIBLE. 007570 007-80 40 D0 42 K=1+NN IF (B(K) . GT. .03125+A(K)) NO TO 2 007400 42 CONTINUE S=S+S 007124 GO TO 2 007230 С 00744 Ĉ CALCULATION FINISHED. REPLACE INPUT FUNCTION VALUES WITH THE FUNC-TION VALUES CCMPUTED FOR THE OUTPUT POINT XEND.PEPLACE INPUT STEP-007460 Length H with New Computer Steplength. 007470 c c С 00748 . 50 HeHSV 00749 X=Z D0 52 K=1:NN 007605 007-10 52 Y(K)=W(K) 007670 С 007:30 -----

1.

~ ~ ~ ~ 007240 RETURN . 007450 007460 0000 REQUIRED ACCURACY NOT OUTAINED. 007270 0074A0 007290 60 COF=.5+5 IF (ABS(COF).GE.ZMIN) AO TO BO IF (ITEST.EQ.0) GO TO B4 007,00 007410 007420 000 JTEST-1, CONTINUE WITH CONSTANT STEPLENGTH EQUAL HMIN. 007,30 007640 007450 S=ZMIN 007460 IF (HSV.LT.0.) S==S IF (ISWH.EQ.1) GO TO 50 007480 GO TO 2 007/90 c DO CALCULATIONS RELATED TO HALVING OF STEPLENGTH. 007510 č 80 D0 82 K=1+NN 82 W(K)=YZ(K) 007730 Z=Z-S 007750 007760 007770 S=COF 1SVH=0 GO TO 2 007580 c JTEST=0 AND ABS(S).LT.HMIN.PRINT ERHOR MESSAGE.SET OK=.FALSE. AND 00790 RETURN TO CALLING PROGRAP. 007600 000 007-10 84 PRINT 88 + ITEST + S + ZMIN + Z OK*+FALSE+ GO TO 50 007220 007630 007p40 007p50 С 86 PRINT 90 . N 007-60 007070 STOP 007680 С

 607840

 88 FORMAT (//.5X,31H*** SURRCHTINE MERSON ERRON ***,2X,8HJTEST = .12, 007490

 12X,4HH = .E12.5.2X.7HHMIN = .E12.5.2X.4HX = .E12.5.//)

 00 FORMAT (//.5X,31H*** SURPCLTINE MERSON ERROR ***.4HX = .E12.5.//)

 90 FORMAT (//.5X,31H*** SURPCLTINE MERSON ERROR ***.4HX = .E12.5.//)

 12X,4HH = .E12.5.2X.4HX = .E12.5.//)

 007500

 90 FORMAT (//.5X,31H*** SURPCLTINE MERSON ERROR ***.4HX N.L.14.1X.55HGR007310

 1EATER THAN THE MAXIMUM NUMBER OF EQUATIONS PERMITTED...//)

 00720

 007630 ¢ END 007940 007950 ¢ ٦. 007660 ¢ SUBROUTINE JUPP (TIME, TJUPP, SJUMP) 007c70 007c80 ċ SUBROUTINE TO CONPUTE TEMP AND SAL JUHPS BELOW WHE. 007490 c c 008100 COMMON/JUMP/ST, SECEND, GRID 008510 COMMON/WML/ZH,ZL,TS,US,SS.ES.H,TT1.TTOLD.JOLD.TOLD.SOLD.: 1,S1.Z1 008720 008430 008430 ċ TB=TT1+(T1-TT1)+(TIME=ST)/(SECEND=ST) TA=TTOLD+(TOLD-TTOLD)*(TIME-ST)/(SECEND-ST) TDASH=(TA-TB)/GRID 008750 008ñ60 008ñ70 TJUMP=TS-TB-TEASH= (2L-71) 008n80 008n90 008100 С SDASH= (SOLD-S1)/GRID SJUMP=SS+S1=SDASH# (ZL=Z1) 008710 С 008120 008130 RETURN 1 END 008140 c

008760 SUBROUTINE TURB (ICOUNT) C08170 008180 c c SUBROUTINE TO COMPUTE FLUXES FROM HET DATA 008190 С REAL L.K 008510 COMMON/FLUX/H+HLFX+W+A4+A5+UX+TINT+U+AT+RH+84+85 CONMON/WEL/DUW2.WT ONTA H.+P+CP+6+K/245+1013+25+1010+9+61+41/ DATA ZL0/0.0/+JOG/0/ 0.08230 008240 008250 С IF(ICOUNT.NE.1) GO TO 15 IF(JOG.EQ.1) GO TO 15 008260 008580 **J**0G¤1 READ(1,10) 23,24, CHWN10, CHW3MX+CO4MX+ZLMAX 0.08590 READ(1+10) 23+27,000 20 10 FORMAT(6F10.3) IF(EOF(1)) 11+12 11 STOP# EOF IN TAPE1-OETECTED IN S/H TURB# COMPUTE ROUGHNESS LENGTAS 008:00 008-11 008-20 С 008-30 12 CON10=0.0013 Z0=10.c/(EXP(K/(SQRT(CON10)))) Z5=10.c/(EXP(K*K/(CHWN)0*ALOC(10./Z0)))) 008-40 608150 008 160 G1=ALOG(10./Z0) 008170 G2=ALOG(10./ZS) G3=ALOG(Z3/ZS) 008-80 008:90 G5=ALOG(Z3/Z0) C08400 G5=ALUG(24/ZO) G6⇒ALOG(24/ZO) INITIALISE CREFFICIENTS 008210 С 008220 CON10=0.001 CON4=CON10+(G1+G1)/(G5+G4) 008230 00840 CON3=CDN10+(G1+G1)/(G5+G5) 008250 008460 008470 CHWN=CHWN10*(G1*G2)/(G=*G1) CD4=CDN4 CD3=CDN3 008380 CH#=CHWN 008290 C08200 Ċ 15 CONTINUE 008310 008220 c WIND SPEED AT 2ND LEVEL 008530 U3=U#G5/G6 008=40 0.08250 С NEUTRAL 10M NRAG COEFF. IF(U.LE.5.) CCN10=.001 IF(U.GT,5.) CCN10=.10.001 008560 008278 CDN4=CON10*(G1*G1)/(G6*G4) CON3=CON10*(G1*G1)/(G5*G4) 008280 008590 ATMOSPHERIC DENSITY 008400 С Daj.294+273./(AT+273.) PARTIAL WATED VAPOUR PRESSURE 014800 с T1=1-=373.16/(AT+273.) 008430 T2=1.-373.16/(WT+273.) ES1=SATVP(T1) E1=(RH+ES1)/100. 008440 008450 008460 ES2=SATVP(T2) 008,70 SPECIFIC HUNTDITY 008-A0 С 0¤0.662/P*E1 C08490 С VIRTUAL AIR TEMPERATURE TV= (AT+273.) + (1.+0.61+0) 008700 008720 c c FLUX COMPUTATION/ITERATION 008730 008740 NCOUNT-1 008751 GO TO 30 ċ 008760 008770 25 CONTINUE 4 ۰. 008780 IF((ABS((ZL-ZL0))).LT.0.02) GO TO 50 008796 ZL0=ZL NCOUNT=NCOUNT+1 008400 IF (NCOUNT.GE.15) STOP #TCC MANY ITE=ATIONS IN SR TURB# RECOMPUTE TRANSFER COEFFICIENTS 008414 008629 с 008430 ZL=Z4/L P4=PSIM(ZL) C=SQRT(CON4) 00844 00855 CD4=CDN4/(1.+CON4+(P4*P4-2.***P4/C)/(K*K)) 008.65 008670 С ZL=Z3/L 008286 P1=PSIM(ZL) 008:90 P2=PSIHW(ZL) C=SQRT(CON3) 0.08400 008910 CHW=CHWH/(1.+CHHH#(P1*P2-x*P2/C-K*P1*C/CHWN)/(K*K)) 008458 008030 С 008944 С 30 H=CH×+0+CP+U3+(WT+AT) 008c56 ₩=CH#+D+U3+0.662/P+(ES2=E1) S=CD4+D+U+U 008668 008478

		• • • • • • • • • • • • • • • • • • •		
с				008689 -
С		FRICTION VELOCITY		008440
		UX=SORT(S/D)		009000
С		M.C.LENGTH		009010
	45	T==D+0X+0X+0X+1A1(K+C+(H1+D+0*01+(H1+513*)+A))		009020
		ZL=Z3/L		009130
-		60 10 25		660150
Ç	* -			009650
	50	CONTINUE		009270
C		15 (7) of 7 HAYS CO TO SIE		889280
		IF (IL.G) (ILMAA) OU (U (IT Necholaryadacheular)		007000
		N=CN#3MATCTCFFU3=(#1781/ W=CN#3NATCTCFFU3=(#1781/		00700
		<pre>c=cp.usp.de.de.de.de.de.de.de.de.de.de.de.de.de.</pre>		017900
	115			009120
	110			009130
		HY_COD+(C/O)		009740
~		0XE3GK1(3/0)		009150
¢		OFTION		009160
		END		009170
c				009180
ř		· inclusion in the second s		009190
ž				009500
•		FUNCTION SATUR(T)		009210
c		COMPLIES SATURATION VAPOUR PRESSURE IN MR		009520
ų		SATVP=1013_254EXP(T+(13.3)85+T*(-1.4760+T*(-0.6445-1.299+T)))	1	009530
		RETURN		009540
		END		009250
с				009260
č				009270
c				009280
-		FUNCTION PSIN(ZL)		009390
		REAL K		009-00
		DATA K,A,PI/0.41,5.0,3.1415927/		009-10
с				009720
č				009330
		IF(ZL+LT+0+) GO TO 10		009,40
		IF(ZL.GT.0.) 60 TO 20		009-50
С		-		009-60
		PSiH=0.		009-70
		GO TO 30 .		009780
С				0.09190
				005200
	10	X=(116.*ZL)**0.25		009400
	10	X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.+X)/2.)*ALOG((1.+X*X)/2.)-2.*ATAN(X)*PI/2.		009400 009410
	10	X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.*X)/2.)*ALOG((1.*X*X)/2.)-2.*ATAN(X)*PI/2. G0 T0 30		009400 009410 009420
с	10	X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.*X)/2.)*ALOG((1.*X**)/2.)~2.*ATAN(X)*PI/2. GO TO 30		009400 009410 009420 009430
с	10	X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.*X)/2.)*ALOG((1.*X**)/2.)-2.*ATAN(X)*PI/2. GO TO 30 IF(ZL.GT.0.5) GO TO 21		009400 009410 009420 009430 009440
с	10	X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.*X)/2.)*ALOG((1.*X**)/2.)-2.*ATAN(X)*PI/2. GO TO 30 IF(ZL.GT.0.5) GO TO 21 PSIM=-A*ZL		009400 009410 009420 009430 009440 009450
c	10	X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.+X)/2.)*ALOG((1.+X*X)/2.)-2.*ATAN(X)*PI/2. GO TO 30 IF(ZL.GT.0.5) GO TO 21 PSIM=-A*ZL GO TO 25 FF(Z) - Z - D - CO TO 22		009400 0094120 0094120 009440 009440 009440 009440 009440
с	10 20 21	X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.+X)/2.)*ALOG((1.+X*)/2.)-2.*ATAN(X)*PI/2. GO TO 30 IF(ZL.GT.0.5) GO TO 21 PSIM=-A*ZL GO TO 25 IF(ZL.GT.10.) GC TO 22 DFCN=0.5(ZL #3L)-0.25(ZL = 3.064.06(ZL)-0.852)		009400 0094200 0094200 0094240 0094240 0094440 0094440 00944780 00944780
c	10 20 21	X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.*X)/2.)*ALOG((1.*X**)/2.)-2.*ATAN(X)*PI/2. G0 T0 30 IF(ZL.GT.0.5) G0 T0 21 PSIM=-A*ZL G0 T0 25 IF(ZL.GT.10.) GC T0 22 PSIM=0.5/(ZL*2L)-4.25/ZL-7.0*ALOG(ZL)-0.852 PSIM=0.5/(ZL*2L)-4.25/ZL-7.0*ALOG(ZL)-0.852		009400 009410 009420 009440 009440 009440 009440 009440 009440 009440 009440
с	10 20 21	X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.*X)/2.)*ALOG((1.*X*A)/2.)-2.*ATAN(X)*PI/2. GO TO 30 IF(ZL.GT.0.5) GO TO 21 PSIM=-A*ZL GO TO 25 IF(ZL.GT.10.) GC TO 22 PSIM=0.5/(ZL*2L)-4.25/ZL-7.0*ALOG(ZL)-0.852 GO TO 25 PSIM=0.05(ZL)-0.74*ZL=12.503		009400 009400 009400 00940 00940 00940 00940 00940 00940 00940 00940
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c	10 20 21 22 25	X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.*X)/2.)*ALOG((1.*X*X)/2.)-2.*ATAN(X)*PI/2. GO TO 30 IF(ZL.GT.0.5) GO TO 21 PSIM=-A*ZL GO TO 25 IF(ZL.GT.10.) GC TO 22 PSIM=0.5/(ZL*2L)-4.25/ZL-7.0*ALOG(ZL)-0.852 GO TO 25 PSIM=ALOG(ZL)-0.76*ZL-12.593 CONTINUE		0000 999343 99934450 0099934450 0099934450 0099934450 0099934450 0099934450 0099934450 0099934450 009993 009993 009993 000999 0009999 0009999 000999990 00099999000 00099999000000
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ο ουο ο ου ^τ ευ	10 20 21 22 25 30	<pre>X={116.*ZL}**0.25 PSIM=2.*ALOG((1.*X)/2.)+ALOG((1.*X*A)/2.)-2.*ATAN(X)*PI/2. G0 T0 30 IF(ZL.GT.0.5) G0 T0 21 PSIM=-A*ZL G0 T0 25 IF(ZL.GT.10.) GC T0 22 PSIM=0.5/(ZL*2L)-4.25/ZL-7.0*ALOG(ZL)-0.852 G0 T0 25 PSIM=ALOG(ZL)=0.76*ZL-12.793 CONTINUE RETURN END FUNCTION PSIM*(ZL) REAL K DATA K,A.PI/0.41.5.0.3.1475927/</pre>		0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
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ບ ບບບ ²⁰ ບບ	10 20 21 22 25 30	<pre>X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.*X)/2.)*ALOG((1.*X**)/2.)-2.*ATAN(X)*PI/2. G0 T0 30 IF(ZL.GT.0.5) G0 T0 21 PSIM=.A*ZL G0 T0 25 IF(ZL.GT.10.) GC T0 22 PSIM=0.5/(ZL*2L)-4.25/ZL-7.0*ALOG(ZL)-0.852 G0 T0 25 PSIM=ALOG(ZL)*0.76*ZL-12.793 CONTINUE RETURN END FUNCTION PSIME(ZL) REAL K DATA K,A.PI/0.41.5.0.3.1475927/ IF(ZL.LT.0.) G0 T0 10 IF(ZL.GT.0.) G0 T0 20</pre>	· · · ·	00000000000000000000000000000000000000
ο ουο ^{ος} ου ο	10 20 21 225 30	<pre>X=(116.*ZL)**0.25 PSIM=2.*ALOG((1.*X)/2.)*ALOG((1.*X**)/2.)-2.*ATAN(X)*PI/2. G0 T0 30 IF(ZL.GT.0.5) G0 T0 21 PSIM=-A*ZL G0 T0 25 IF(ZL.GT.10.) GC T0 22 PSIM=0.5/(ZL*2L)-4.25/ZL-7.0*ALOG(ZL)-0.852 G0 T0 25 PSIM=ALOG(ZL)*0.76*ZL-12.593 CONTINUE RETURN END FUNCTION PSIM*(ZL) REAL K DATA K.A.PI/0.41.5.0.3.1455927/ IF(ZL.LT.0.) G0 T0 10 IF(ZL.GT.0.) G0 T0 10</pre>	•	0 U 0 C C O C U O O C O D O U O U O U O U O C C O C O O O O O O O
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0 0 000 ^{2,5} 00 0 0	10 20 21 225 30	<pre>X={116.*ZL}**0.25 PSIM=2.*ALOG((1.*X)/2.)*ALOG((1.*X**)/2.)-2.*ATAN(X)*PI/2. G0 T0 30 IF(ZL.GT.0.5) G0 T0 21 PSIM=A*ZL G0 T0 25 IF(ZL.GT.10.) GC T0 22 PSIM=0.5/(ZL*2L)-4.25/ZL-7.0*ALOG(ZL)-0.852 G0 T0 25 PSIM=ALOG(ZL)=0.76*ZL-12.593 CONTINUE RETURN END FUNCTION PSIM*(ZL) REAL K DATA K.A.PI/0.41.5.0.3.145927/ IF(ZL.GT.0.) G0 T0 10 IF(ZL.GT.0.) G0 T0 10 IF(ZL.GT.0.) G0 T0 120 PSIM#=0. G0 T0 30 X=(1.*16.*ZL)**0.25 </pre>		0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
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ט טיט ^י נט ט ט	10 20 21 22 30 ; ; ;	<pre>X={116.*ZL}**0.25 PSIM=2.*ALOG((1.*X)/2.)*ALOG((1.*X**)/2.)-2.*ATAN(X)*PI/2. G0 T0 30 IF(ZL.GT.0.5) G0 T0 21 PSIM=A*ZL G0 T0 25 IF(ZL.GT.10.) GC T0 22 PSIM=0.5/(ZL*2L)-4.25/ZL-7.0*ALOG(ZL)-0.852 G0 T0 25 PSIM=ALOG(ZL)-0.76*ZL-12.*93 CONTINUE RETURN END FUNCTION PSIM*(ZL) REAL K DATA K.A.PI/0.41.5.0.3.1475927/ IF(ZL.GT.0.) G0 T0 10 IF(ZL.GT.0.) G0 T0 10 IF(ZL.GT.0.5) G0 T0 21 PSIM*=2.*ALOG((1.*X*X)/2.) G0 T0 30 IF(ZL.GT.0.5) G0 T0 21</pre>		0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
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υ υυυ ^{τε} υυ υ υ	10 20 21 22 30 ; ; ; 10 20 21	<pre>X={116.*2L}**0.25 PSIM=2.*ALOG((1.*X)/2.)+ALOG((1.*X*X)/2.)-2.*ATAN(X)*PĪ/2. G0 T0 30 IF(2L.GT.0.5) G0 T0 21 PSIM=A2L G0 T0 25 IF(2L.GT.10.) GC T0 22 PSIM=0.5/(2L*2L)-4.25/2L-7.0*ALOG(2L)-0.852 G0 T0 25 PSIM=ALOG(2L)-0.76*2L-12.793 CONTINUE RETURN END FUNCTION PSIM*(2L) REAL K DATA K,A,PI/0.41.5.0.3.1475927/ IF(2L.GT.0.) GO T0 10 IF(2L.GT.0.) GO T0 20 PSIM*=0. G0 T0 30 X=(116.*2L)**0.25 PSIM*=2.*ALOG((1.*X*X)/2.) G0 T0 30 IF(2L.GT.0.5) GO T0 21 PSIM*=2.*ALOG((1.*X*X)/2.) G0 T0 30 IF(2L.GT.0.5) GO T0 21 PSIM=A*2L G0 T0 25 F(2L.GT.0.5) GO T0 21 PSIM=A*2L G0 T0 25 F(2L.GT.0.5) GO T0 21 PSIM=A*2L G0 T0 25 PSIM=0.5/(2L*2L)-4.25/7L-7.0*ALOG(2L)-0.852 F(2L.GT.0.5) GO T0 21 PSIM=0.5/(2L*2L)-4.25/7L-7.0*ALOG(2L)-0.852 F(2L.GT.0.5) GO T0 22 PSIM=0.5/(2L*2L)-4.25/7L-7.0*ALOG(2L)-0.852 F(2L.GT.0.5) GO T0 22 PSIM=0.5/(2L*2L)-4.25/7L-7.0*ALOG(2L)-0.852 F(2L.GT.0.5) GO T0 21 PSIM=0.5/(2L*2L)-4.25/7L-7.0*ALOG(2L)-0.852 F(2L.GT.0.5) GO T0 22 PSIM=0.5/(2L*2L)-4.25/7L-7.0*ALOG(2L)-0.852 F(2L.GT.0.5) GO T0 22 PSIM=0.5/(2L*2L)-4.25/7L-7.0*ALOG(2L)-0.852 F(2L.GT.0.5) F(2L.GT.0.5) F(2L.GT.0.5) F(2L*2L)-4.25/7L-7.0*ALOG(2L)-0.852 F(2L.GT.0.5) F(2L*2L)-4.25/7L-7.0*ALOG(2L)-0.852 F(2L.GT.0.5) F(2L*2L) F(2L*2L*2L)-4.25/7L-7.0*ALOG(2L)-0.852 F(2L*2L*2L) F(2L*2L) F(2L*2L*2L) F(2L*2L) F(2L*2L*2L) F(2L*2L) F(2L*2L*2L) F(</pre>		0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
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APPENDIX D: MODEL RESULTS







D1.3







D1.6



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D1.10



D1.11



D1.12





1.20



D2.2



D2.3



D2.4